

E-Learnig Materials  
On  
**Thermal Engg. II**  
Branch –Mechanical  
4<sup>th</sup> Semester



Prepared  
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# Thermal Engineering

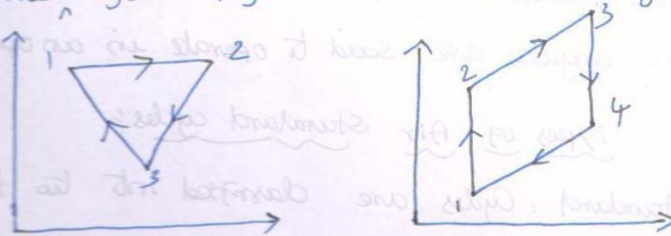
## Unit-I : Gas power Cycles:

Cycle: (what is meant by cycle)

\* It is defined as a repeated series of operations occurring in a certain order.

\* (ii) It may be repeated by repeating the process in the same order.

The <sup>DIFF TYPES OF</sup> cycle may be as shown in Fig below.



The cycle may be of

(1) imaginary perfect engine  $\rightarrow$  ideal cycle

(2) Actual engine  $\rightarrow$  Actual cycle.

Thermodynamic Cycle: (First law & Second law suggests)

\* The method of producing mechanical power by transferring heat from reservoir to a working fluid is done through a thermodynamic cycle.

\* A part of heat received by fluid is rejected to the sink. These cycles are termed as power cycles.

Power Cycles are classified as follows:

(1) Vapour power cycles

(2) Gas power cycles.

NOTE:

## unit - II . IC Engines:

### 2) Classification:

IC engines may be classified on following basis

- (A). According to type of fuel used.
  - i) Petrol engine.
  - ii) diesel "
  - iii) Gas turbine .
- (B). According to method of ignition.
  - i) Spark ignition.
  - ii) Compression ignition.
  - iii) hot-spot ignition.
- (C). According to number of strokes Per Cycle.
  - i) Four stroke engine.
  - ii) Two "
- (d). Working Cycle:
  - i) otto cycle engine.
  - ii) Diesel cycle "
  - iii) Dual Combustion: "
- (e). number of cylinder used.
  - i) single cylinder.
  - ii) multi cylinder.
- (f). Arrangement of cylinder :
  - i) horizontal Engine.
  - ii) Vertical "
  - iii) Radial "
  - iv) opposed cylinder Engine .
  - v). V-Engine.
- (g). Fuel Injection.
  - i) Carburettor
  - ii) Air injection
  - iii) airless injection
- (h). Cooling System.
  - i) air cooled engine.
  - ii) water cooled engine .
- (i) Valve location :
  - (i) overhead valve engine.
  - (ii) Side valve engine.

## 2.2 Components & function:

19

The Main Parts of an I.C engines are.

**Cylinder:** It is the main body of the engine in which the piston reciprocates to develop power. The cylinder has to withstand very high pressure and temperature because there is a direct combustion inside the engine cylinder. Heavy duty engines are made of alloy steel. Sleeves (or) liners inserted into cylinder when the engine block is heavy.

**Cylinder head:** One end of the cylinder is closed by cylinder head. The cylinder head contains inlet & exhaust valve through which the fresh charge is admitted inside the engine cylinder and burnt gases are exhausted from the cylinder to atmosphere.

**Piston:** It is the heart of the engine. It is a gas tight movable cylinder disc which slides up & down in the cylinder. Its function is to compress the fresh charge during the compression stroke & to transmit the force produced due to combustion of the charge to the connecting rod & then to the crank during the power stroke.

**Crank gear:** It is the principal mechanism of the reciprocating engine. The mechanism consists of piston assembly, connecting rod, crank shaft and flywheel.

The crank gear transmits the force of explosion, produced by combustion of fuel with air in the engine cylinder to the output shaft.

## Valves and Valves Operating Mechanism:

It Permits at the right moment the entry of fresh Charge into the Cylinder and exhaust the Products of Combustion into the atmosphere.

In the Case of SI engines, Correct Quantity of air fuel mixture is supplied to the Cylinder by Carburetor.

## Fuel Filters:

It filter the foreign Particles that may be Present in the fuel.

**Air filter:** It removes dust, dirt and other foreign Particles Present in the air supplied to the engine.

**lubricating system:** It supplies lubricating oil to the various Parts of an engine where there is relative motion. This reduce friction between the Parts and wear and there by increase engine life.

**Cooling system:** It's used to abstracts excess heat from the various Parts of engine which are heated due to Combustion. The Coolants are air (or) liquid (or) it may be Cooled by lubricating oil.

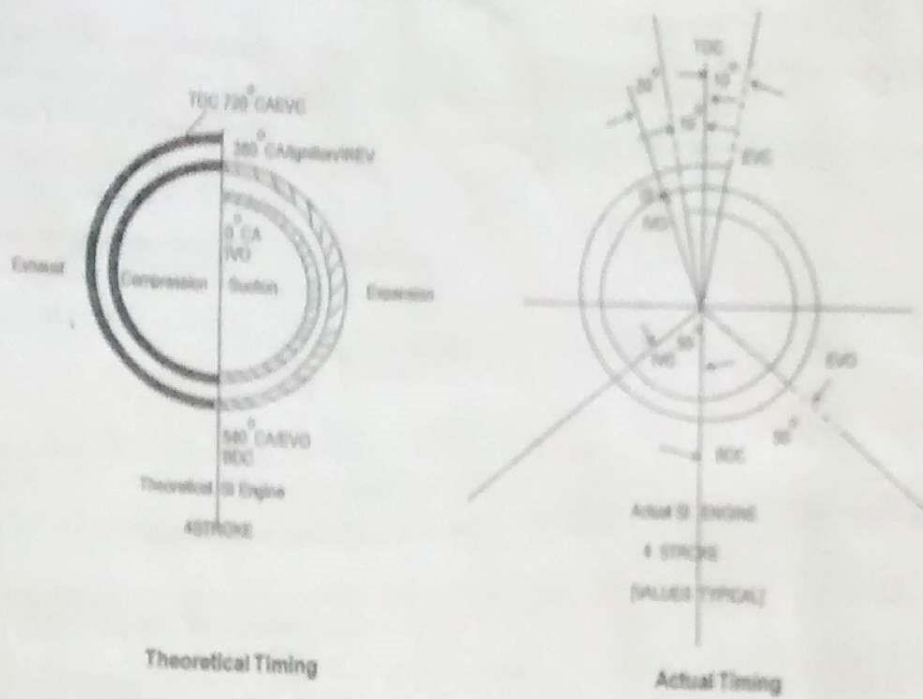
## 2.3. Engine timing & Valve timing diagram: 21

A diagram of the actual Pressure Variation with respect to the Volume Changes of the Cylinder Contents as the piston moves from BDC to TDC and from TDC to BDC is also obtained. This diagram is called an Indicator diagram.

Let us Consider the valve timing diagrams one by one.

1. Theoretical Diagram.
  - i) Valve timing diagram of a 4 Stroke Petrol Engine.
  - ii) valve timing diagram of a 4 Stroke Diesel Engine.
2. Actual Engine Diagram
  - i) Actual Engine Valve timing diagram for 4 Stroke Petrol engine.
  - ii) Actual Engine Valve timing diagram for a 4 Stroke Diesel engine.
3. Theoretical Valve timing & P-V Diagram.
  - i) For a 2 Stroke Petrol engine
  - ii) For a 2 Stroke Diesel engine.
4. Actual Engine P-V, P-T
  - i) For a 4 Stroke & 2 Stroke Petrol engine.
  - ii) for a 4 Stroke & 2 Stroke Diesel engine.

### 3.5.7 Valve Timing Diagram - SI Engine



Figs. 3.12 : Valve Timing Diagram - 4 Stroke SI Engine

Table 3.3 : Comparison between Theoretical and Actual Valve Timing-4S SI Engine

	Theoretical	Actual	
IVO [Inlet Valve Open]	TDC	10° Before TDC	[Typical]
IVC [Inlet Valve Close]	BDC	50° After BDC	[1 Rev]
IS [Ignition Start]	TDC	20° Before TDC	[Typical]
EVO [Exhaust Valve Open]	BDC	50° Before BDC	[1 Rev]
EVC [Exhaust Valve Close]	TDC	10° After TDC	[Typical]
Value Overlap	0	20° [10° + 10]	

Let us take Inlet valve first

It is opening 10° BDC and close 50° CA after BDC.

Inlet valve opens earlier than TDC:

The Purpose is to get max. air-fuel mixture inside the cylinder within the available time. The inlet valve is opened early so that the air charge is given time to gain momentum.

## Extending beyond the BDC for Intake Valve

23

### Closing:

The Purpose of this action can be explained as the means to utilize the kinetic energy of the following air charge into the cylinder.

### Start of Ignition Earlier:

The spark is advanced well before TDC to allow enough time for the air-fuel mixture for flame development and entering into rapid burning stage. Since flame development & flame propagation are functions of time, spark advance is restored to. The spark advance can be even  $35^\circ\text{CA}$  before TDC. The burning process is dependent on the mixture quality (i.e) air fuel ratio, its homogeneity, residual gas present in the cylinder etc.

Depending on all the factors and the speed the spark is advanced (or) retarded.

Advance spark discharge - Introducing spark discharge earlier to TDC.

Retarded spark discharge - Spark discharge taking place closer to TDC.



## Exhaust Valve:

**opening early:** In a theoretical engine exhaust valve opens at BDC in the second revolution. Referring to the actual engine valve diagram we find valve opens much early.

The purpose of exhaust valve early is to ensure efficient expulsion of all the products of combustion. When exhaust valve opens, the working fluid is at a higher pressure than atmosphere. This enables exhaust gases to be discharged early.

## Closing of exhaust valve after TDC:

When the piston is nearing TDC, it has attained considerable kinetic energy keeping the exhaust valve open even beyond TDC there is a means of providing an uninterrupted flow path for the combustion products & thus by increases the  $\eta$  of exhaust.

**Overlap:** This is the duration, in degree crank angle in which both inlet & exhaust valve are open.

# valve timing diagram for CI engine

## 2. Valve Timing Diagram - Compression Ignition or Diesel Engine:

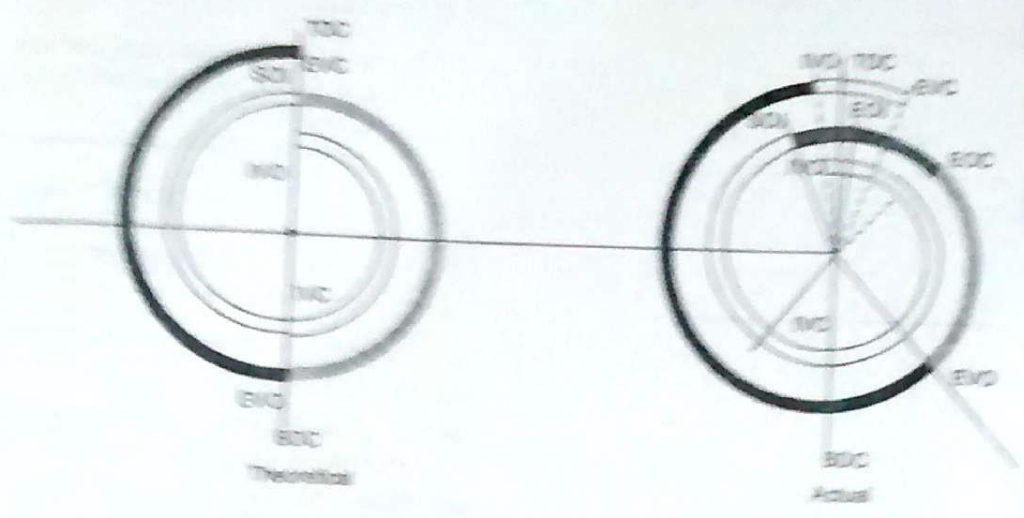


Fig. 3.15: Valve Timing Diagram (upright) Diesel Engine

- BDC - Bottom Dead Centre
- TDC - Top Dead Centre
- IVO - Inlet Valve Open
- IVC - Inlet Valve Close
- EVO - Exhaust Valve Open
- EVC - Exhaust Valve Close
- SOI - Start Of Injection
- EOI - End of Injection
- EOC - End of Combustion
- Valve Overlap - IVO to EVC.

Events	Theoretical	Actual
IVO	TDC	10° BTDC
IVC	BDC	40° ABDC
SOI	TDC	20° BTDC
EVO	BDC	45° BBDC
EVC	TDC	20° ATDC
Valve Overlap	0	30° CA

The Purpose of Inlet Valve Opening before TDC, Closing after BOC and Exhaust Valve Opening before BDC and Closing after TDC are nearly the same for the SI & CI engine.

The Process of Combustion of Petrol fuel in the CI engines are entirely different while spark advances in the case of the SI engine may be for allowing time for Pre-flame reactions to take place, the SOI earlier in the CI engine is to allow enough time for the Combustion Process and to complete ignition delay Period well in advance of TDC, in the Process of auto-ignition of delay in the CI engine usually, the ignition delay is split into two Parts the Physical delay and the Chemical delay.

## Port Timing diagram :

27

In a Crank Case two stroke Cycle engine, we had identified the three types of Ports as;

Scavenge Ports

Exhaust Port

Inlet Port.

Scavenge Ports as inlet Ports which creates Confusion. It is better to refer to the port filling air/air-fuel mixture into the Cylinder as Scavenge Ports and the Port filling air/air fuel mixture into the Crank Case as Inlet Ports.

Port timing diagram for Crank Case scavenged symmetrical two stroke cycle, SI & CI engine.

In the case of SI engine, the spark discharge initiates the process of combustion & the case of CI engines SOI in the high temperature air of the cylinder initiates the process of combustion.

The end of combustion occurs more or less about  $35^\circ$  ADTC in both the engines.

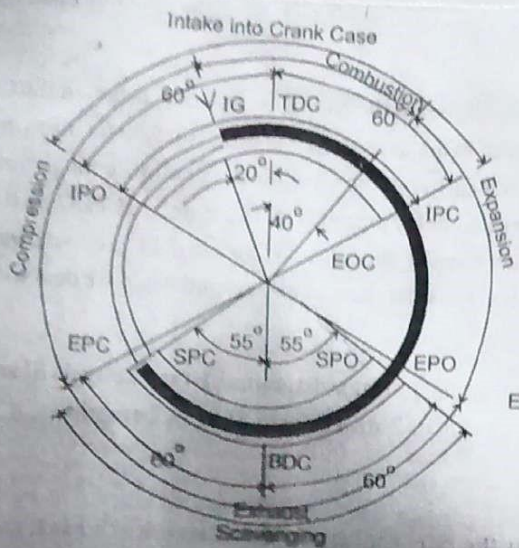


Fig. 3.16 (a): Typical port timing diagram  
2 stroke SI engine

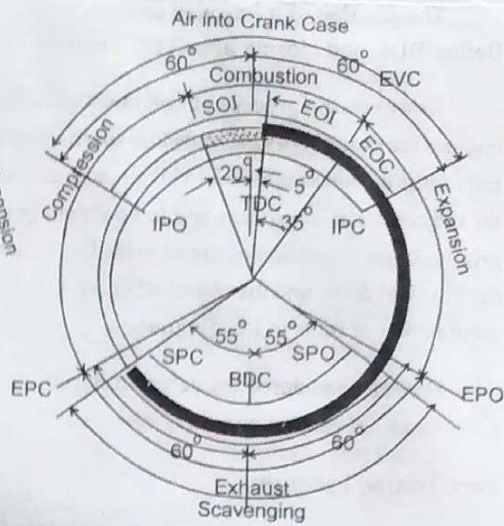


Fig. 3.16 (b): Typical port timing diagram  
2 stroke CI engine

Legend:

TDC - Top Dead Centre

BDC - Bottom Dead Centre

SPO - Scavenging Port Open

SPC - Scavenging Port Close

IG - Ignition Start

EOI - End of Injection

EPO - Exhaust Port Open

EPC - Exhaust Port Close

IPO - Inlet Port Open

IPC - Inlet Port Close

SOI - Start of Injection

EOI - End of Injection

Since it is a case of Symmetrical Crank Case Scavenged engines Port opening & Closing are symmetrical about BDC/TDC Exhaust port opens  $60^\circ$  before BDC and closes  $55^\circ$  after BDC and likewise inlet port to fill case opens  $60^\circ$  before TDC and close  $60^\circ$  after TDC.

## 2.4. Actual and Theoretical P-V diagram: 29

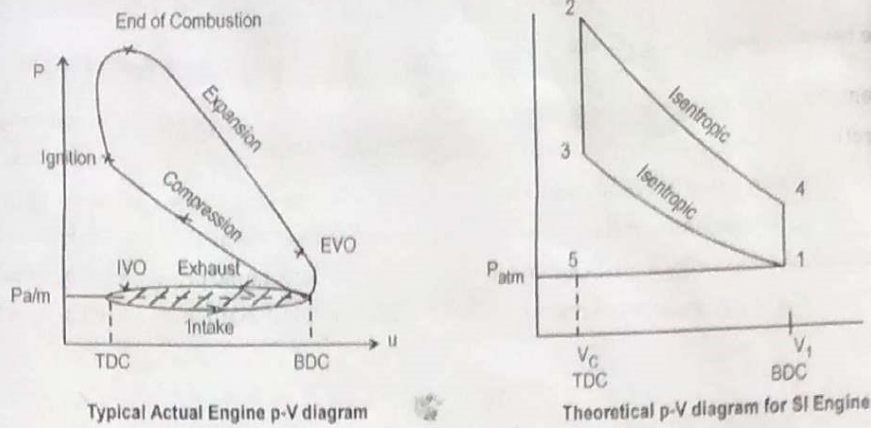
From the above discussion on the Valve timing diagram it is clear that there is departure from the theoretical process in the actual engine. Moreover we have observed during our consideration of engine operation, that there should be Pressure difference for fresh charge to fill up the cylinder during intake & similarly Pressure difference across exhaust valve to discharge the products of combustion efficiently. our understanding of thermodynamics principles state that work is done by an agency to push a volume of a fluid at a Pressure.

$$P(V_2 - V_1)$$

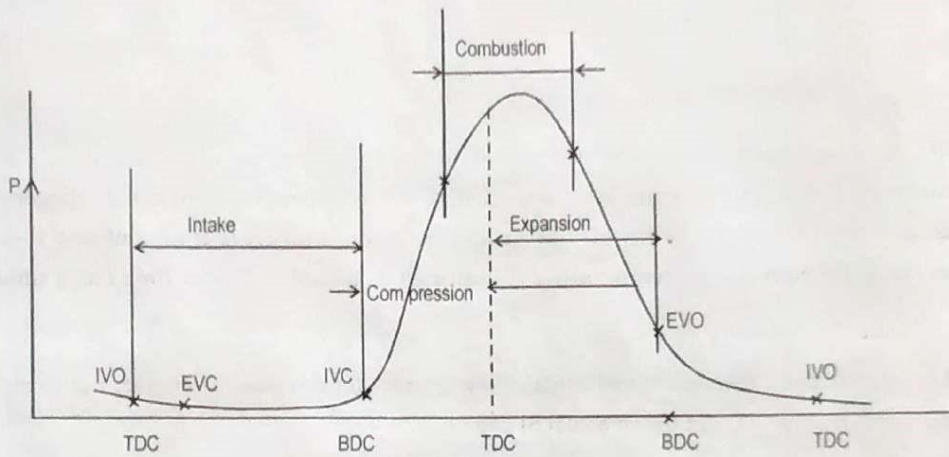
$P$  = the Pressure in N. ;  $V_1$  = the initial volume.

$V_2$  = the final volume

Comparison of theoretical P-V diagram with actual P-V diagram.



Figs. 3.13 : Theoretical and Actual p-v Diagram for SI Engine-4S.



Figs. 3.14 : Typical p-t Diagram for Actual 4-SI Engine

When the drum is given a reciprocating movement, it records the p - v diagram.

we obtained a complete history of the pressure existing in the cylinder at any instant and with this details of a complete cycle is drawn. Such a diagram which gives the instantaneous value of the pressure inside the cylinder with respect to the piston of the piston is known as Indicator diagram.

### 3.5.8 $p - v$ and $p - t$ Diagrams

We shall now consider the  $p - v$  diagrams of theoretical and actual engine cycles of SI and CI engines.

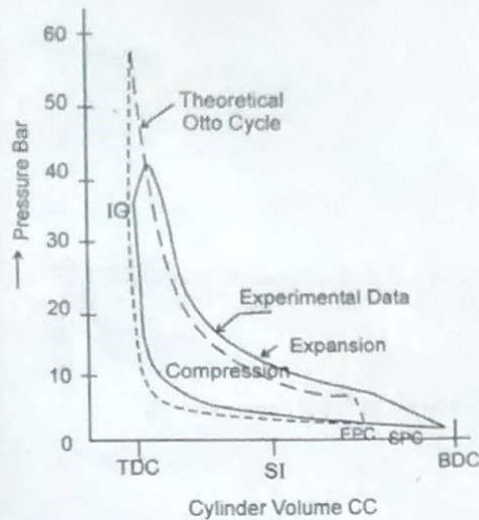


Fig. 3.17 (a) : 2S SI Engine Experimental data compared with OTTO cycle (Typical)

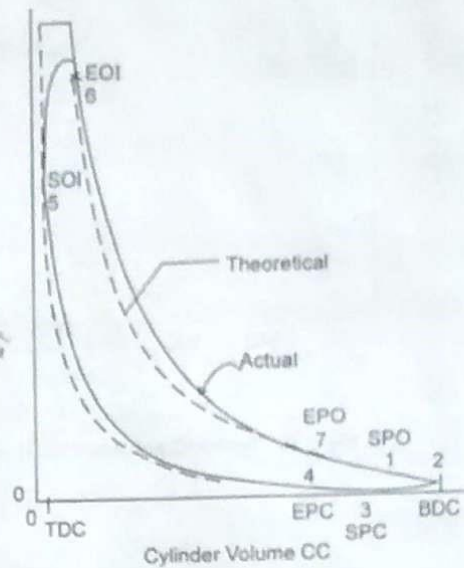


Fig. 3.17 (b) : 2S CI Engine Indicator diagram compared with theoretical Diesel cycle (Typical)

Theoretical and experimental data for the Pressure more (or) less look similar and the values do approach the theoretical values. Compression & the expansion curve do not follow the  $\gamma = 1.4$  value for the ideal Otto cycle.

Similar comments will hold good for the Compression ignition engines also. It can be observed from the figure that there is a constant pressure movement of the piston between Point 5 and Point 6 from where the expansion takes place upto the Point 7 when the exhaust port open.

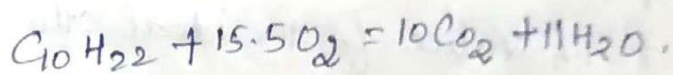
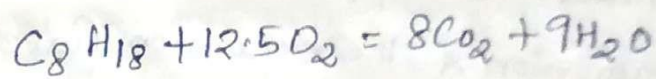


## 25 Car burettor:

A mixture of air and fuel in which the fuel is mixed with the Chemically Correct Quantity of air is known as Stoichiometric mixture.

↳ A mixture in which air is in excess of the Chemically Correct requirement is known as lean (fuel) mixture.

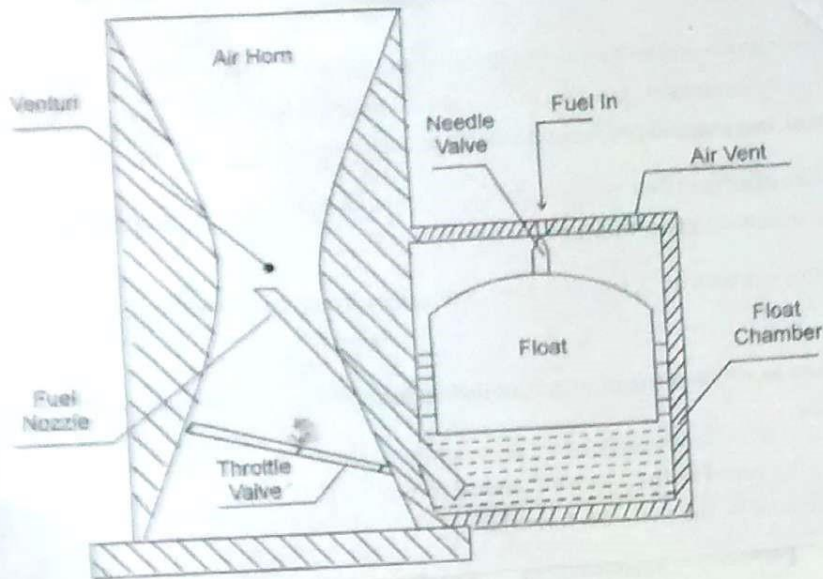
Considering Petrol as fuel whose Chemical formula is  $C_8H_{18}$ , it can be worked out to find the Oxygen requirement by the Chemical formula.



There is a limit within which the mixture burns and sustain Combustion that is if the ratio is too rich will not sustain Combustion it will not find fuel to carry the flame forward.

# Principle of a Carburettor:

33.



The Components are

- i) air duct (or) air horn
- ii) Float Chamber.
- iii) throttle body.

A venturi is created inside the air duct. The venturi is a restriction in the air flow passage. By applying continuity eqn it can be found that the velocity increases at the venturi and because of this pressure drop.

Petrol in the float chamber is connected by a fuel nozzle to the venturi through a meter. When the pressure drop below atmospheric the petrol in the float chamber is forced by the atmospheric pressure towards the venturi space.

The mixture passes through the throttle valve fixed in the throttle body.

## 2.5 Battery Ignition Systems

It is known as the Coil-ignition System.

It can also be considered as the Magnetic Discharge ignition system. The Principle is that when the ignition switch is inserted, the Primary Circuit of MIS close & the Primary gets charged and also result the magnetic field in the iron core also build up. This process is not instantaneous but takes few micro seconds.

The system consists of a 6 to 12 V ammeter, ignition switch, ignition coil, with a Primary and secondary winding as a fund in a Step up transformer, Contact breaker, Capacitor distributor rotor, distributor Contact Point. But it works on mutual electromagnetic induction Principle.

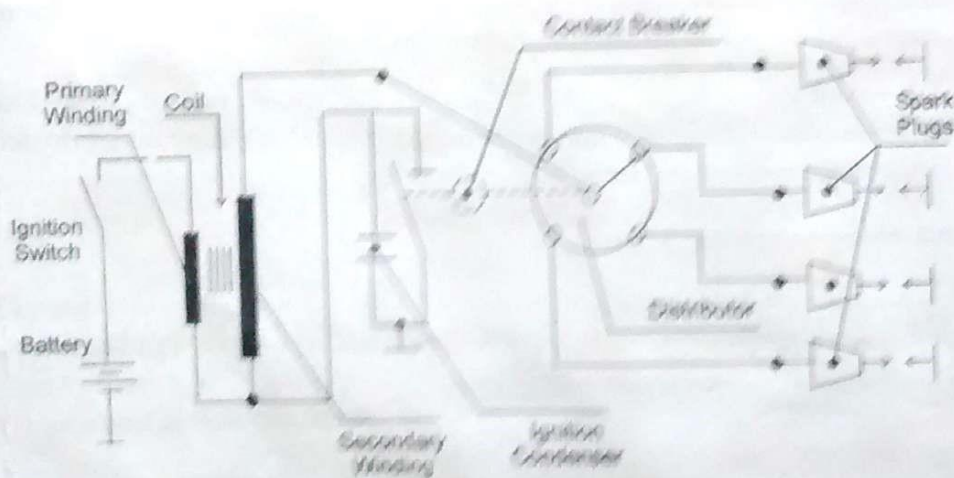


Fig. 3.48 : Wiring Diagram for a Typical Battery Ignition System (Conventional)

It has two circuits.

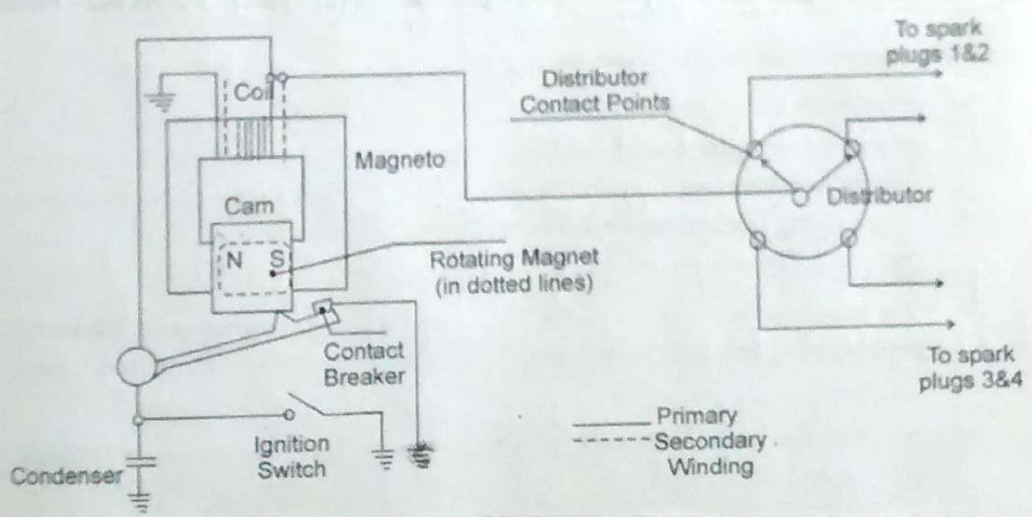
- i) a Primary Circuit . ; ii) Secondary Circuit .

Primary Circuit consists of 6 (or) 12 v battery , ammeter , ignition switch , Primary winding , Contact breaker .

Secondary Circuit consists of secondary winding , distributor rotor , Contact Points

### Magneto ignition system:

In magneto ignition, the magneto works as an energy source and produces and supplies the required current to the primary winding. Two type of magneto are available , a rotating magneto fixed coil (or) a rotating coil with fixed magneto . It also works on same principle .



The breaker points are subjected to wear required frequent maintenance . Because of arcing , pitting of contact breaker point takes place which leads to regular maintenance schedule .

## 26 Combustion and knock:

The process of Combustion takes place in a SI engine is differ from that in the CI engine. In a Conventional SI engine, petrol is inducted into the cylinder during the suction stroke and around the end of compression stroke a spark discharge is made of take place in the Combustion Chamber.

So, in a normal Combustion in the SI engine spark discharge signals the start of the Combustion Process.

The Combustion Process in a CI engine comprises four phases.

- i) Ignition delay Period.
- ii) Premixed Combustion.
- iii) mixing Controlled Combustion.
- iv) late Combustion Phase.

### SI engine Combustion:

It Contains four phases.

- i) Spark Ignition ; ii) development of early Flame front
- iii) Flame Propagation iv) Flame termination.

Flame is the evidence of a chemical reaction takes place between fuel and  $O_2$  that liberates energy with the subsequent increase in Pressure and temp Combustion begins at the spark plug where the fuel molecules are energized by the

spark to a level where reaction becomes self sustaining. Here the reaction zone is erratic and once the reaction zone is being established the turbulent spherical flame front & burned gas is behind the flame front.

Abnormal Combustion has been divided into two categories.

- i) Knock
- ii) Surface ignition.

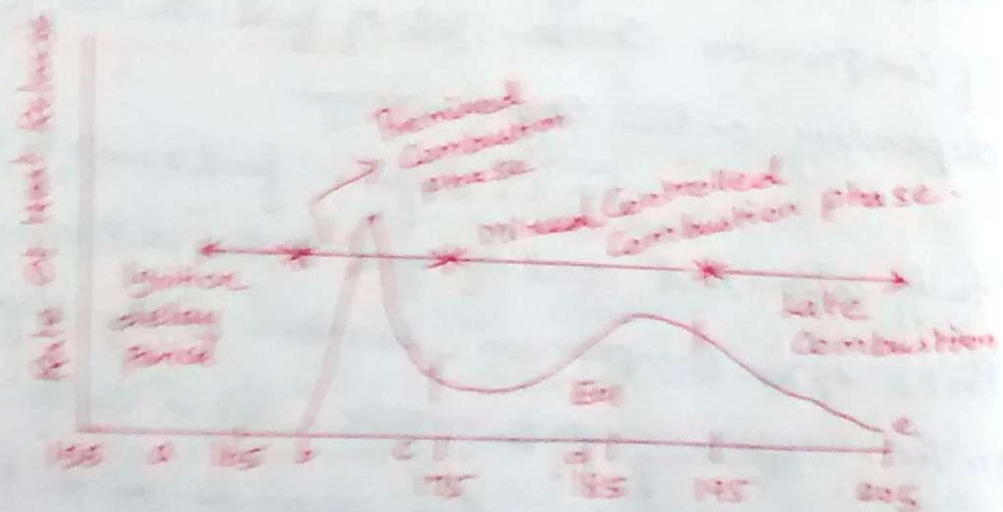
The foremost criterion for good Combustion is that it must occur very near the TDC so that full work output is realized. It has been found that spark advances play a critical role in developing the max. torque from an given engine.

### CI Engine Combustion:

In CI engine air alone compressed and raised to a high temperature. Near the end of compression stroke, jets of fuel are no<sup>g</sup> depending on the engine design.

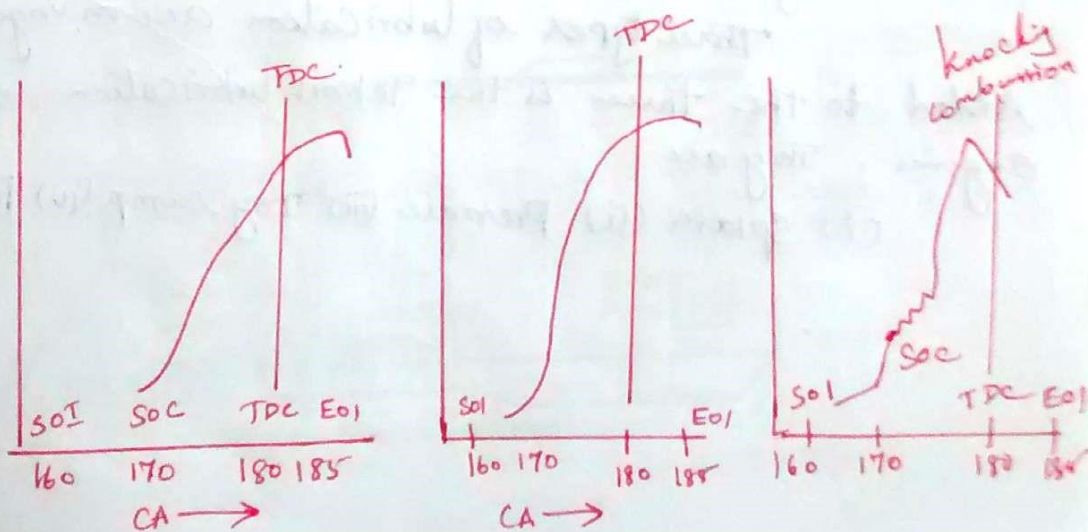
In CI engine fuel needs to be fully atomized and sprayed to the different parts of the compression chamber solely depend on the efficiency of the nozzle. It is easily to realize the good Combustion depends on the <sup>g</sup> of the nozzle.

The spray from an nozzle creates an envelope of fuel surrounded by fuel. The temperature of air is conducted for auto-ignition and oxidation of fuel become imminent. This period when the fuel is atomized, vaporized, find enough air is mixed with air and is raised in temperature is the Physical delay Period. In the next phase called Chemical delay reaction starts slowly and accelerates until inflammation or ignition takes place. This period that elapse between the injection of diesel fuel and the start of combustion is known as ignition delay. Ignition delay is the combination of Physical delay and Chemical delay Periods.



# Knock in CI engine & SI engine.

In the CI engine injection process is time bound. Injection is continuing as the first few drops are injected and are passing through the period of ignition delay. If the ignition delay is short, for by the time the additional fuel droplets arrive actual burning would have started. And the accumulate fuel is likely to be a small amount. This means the mass rate of mixed burned will be such as to produce a smooth force on the piston. On the other hand if the ignition delay is longer on more fuel will accumulate and burn resulting in too rapid a pr. rise causing a jamming action on the piston. If the ignition delay is still longer than the quality of accumulate fuel will also give rise to extreme pressure dist x violent variation evidence by an audible knock. SI engine occurs later in knock but CI engine occurs earlier in the combustion.





## 2-7. Lubrication and Cooling System:

### Lubrication System

Lubrication system is to reduce the wear between the two metals (or) the to reduce the friction loss due to relative motion.

Lubrication method and systems can be classified as follows:

For bearing and bushes:

i) Gravity feed.

ii) By wicks and

iii) By a ring.

Gravity feed is employed for a shaft rotating in stationary bearings.

wick (or) siphon lubrication is also installing a cup filled with lubricating oil over the hole in the bearing housing.

For other Engine Parts,

Three types of lubrication are in vogue.

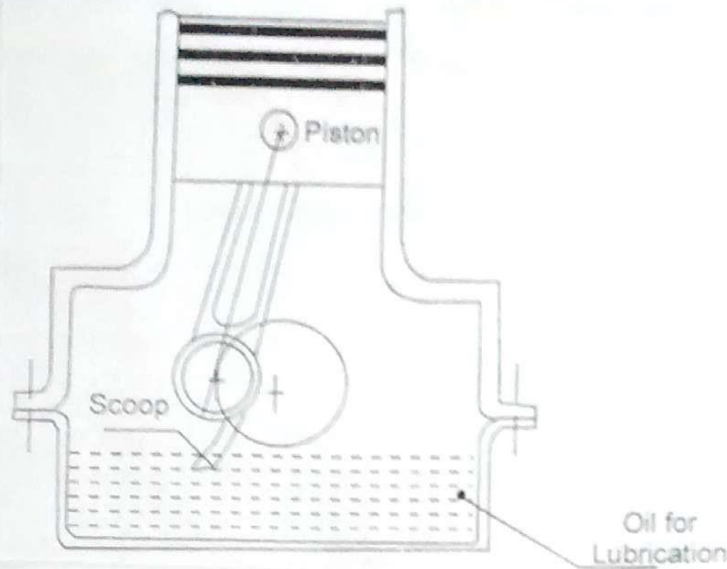
Added to the three is the Petroil lubrication for 2s Engine. They are:

- (i) Splash
- (ii) Pressure
- (iii) Dry sump
- (iv) Petroil.

## Splash lubrication:

39

A Scoop is attached to the lower part of the big end of the Connecting rod. A trough of oil is stored below the Connecting rod. When the engine runs, the Scoop collects the oil & splashes over the Piston, wrist pin, big end bearings etc.



## Pressure lubrication:

In this a Pump is employed to achieve required Pressure to lubrication. A Strainer/Filter is employed for the Pressure lubrications.

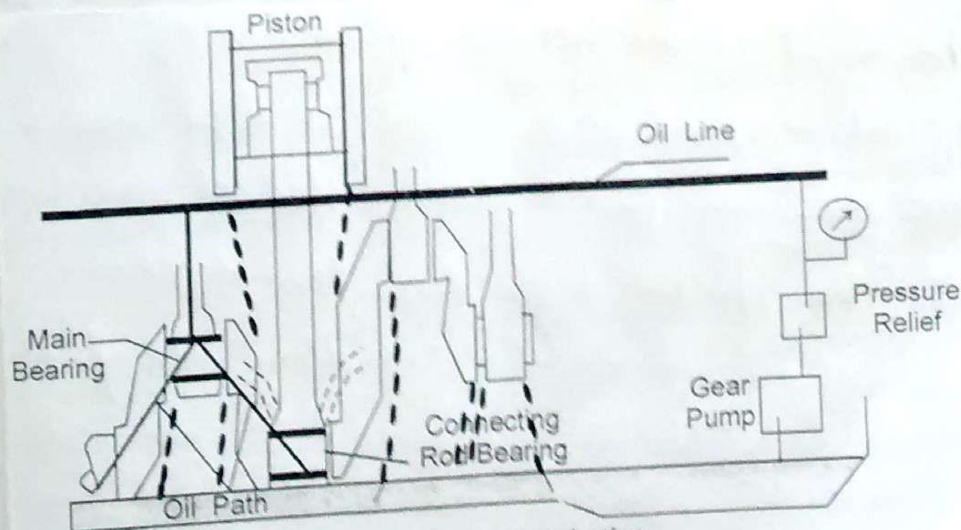
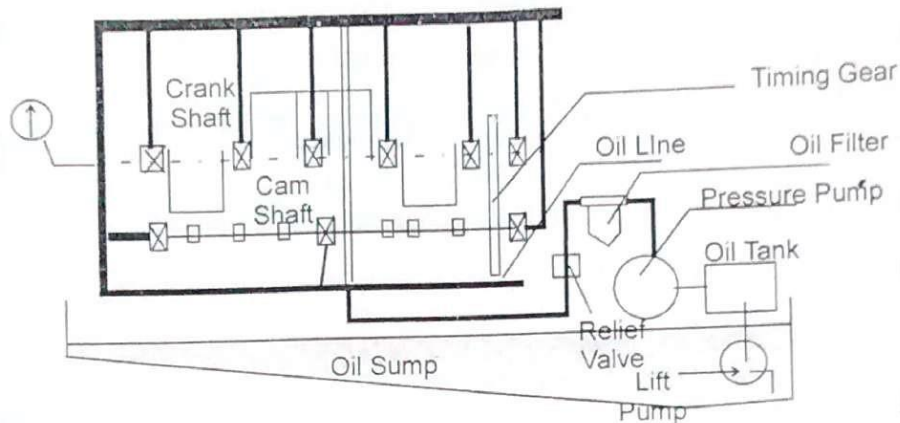


Fig. 3.56 : Pressure Lubrication

## Dry Sump Method:

When a vehicle is moving up a gradient (or) climbing a steep slope, there is all the likelihood of the Pump suction not finding oil level. In such situation two Pumps employed. One Pump is to lift oil from the lowest level. Another Pump is to Main gallery.



## Petroil Method:

Petrol + oil makes Petroil. This type is used for SI engines. Since Crank gas case cannot be used as the oil sump. 3-6% of lubricating oil is mixed with Petrol and is introduced along with the air-fuel mixture. The oil serve to lubricate the Piston & Cylinder. This system consume lot of oil since it burns along with fuel.

## Cooling System:

It is about 30 to 35% of heat supplied to the IC engine wasted as heat carried away by cooling medium. Normal cooling medium used is water. The cooling system in use we know is Air cooled and water cooled.

## Air Cooling Method:

The basic air cooling methods are.

- i) Cooling fins and (ii) Blast of air provided by a blower or moving vehicle.

Cooling fins increase the area of exposure of the heated surface to the blast of air thereby increase the  $\eta$  of cooling.

## Water Cooling Method:

In the water cooling system, the cooling water is circulated around the engine so that it absorbs the heat from the engine components, mainly the engine cylinder & head.

Types:

- i) Non-Return System.
- ii) Thermo syphon.
- iii) Impeller Thermo syphon.
- iv) Full Pump Circulation and
- v) Evaporative cooling.

### Thermosyphon:

When we boil the water in a vessel the bottom layer of water heated up and rise upwards and cooler water goes down. This is known as Convection Current.

In such a way that Cylinder Jacket and Radiator Connected. hot water rises up and flows into Radiator where it cooled and naturally flows into the Cylinder jacket.

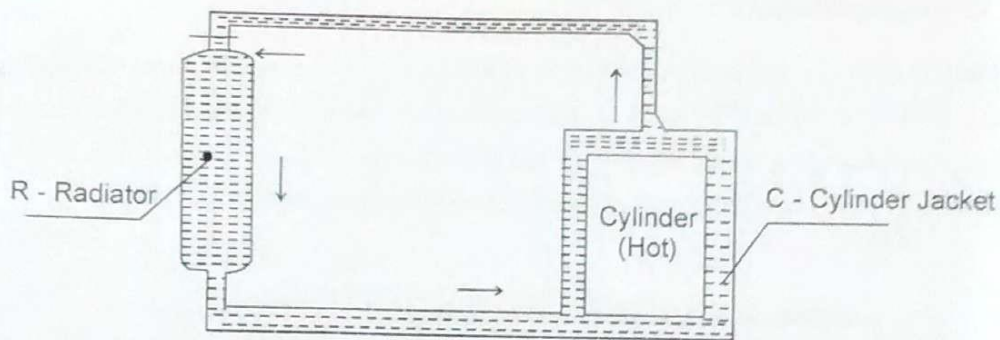


Fig. 3.61 : Simple Thermosyphon

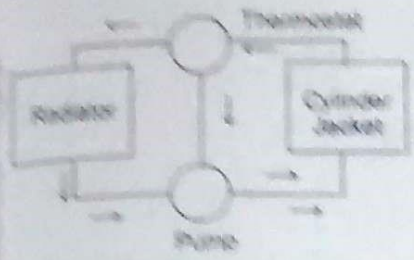
### Impeller Thermosyphon:

The water circulation is still by convection though assisted by a pump.

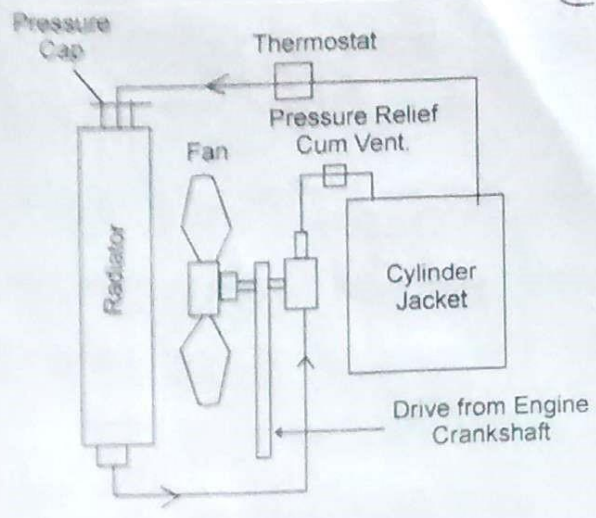
The radiator cools the hot water from the engine cylinder jacket.

- i) Tubular type
- ii) Cellular type.

Tubular Core consists of tinned tube covered with brass fins to increase the heat area.



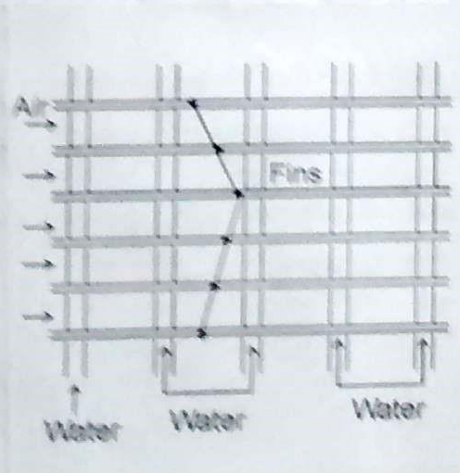
(a) Impeller Thermostyphon  
 Inside Arrows - Cool Engine  
 Outside Arrows - After attaining operating temperature.



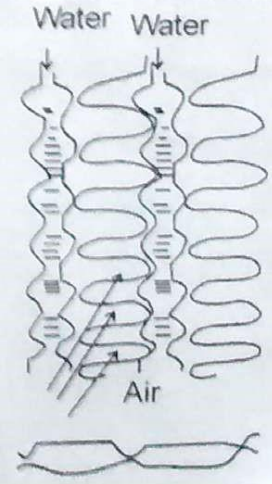
(b) Forced Cooling

The materials for radiators must have good corrosion resistance and thermal conductivity. Copper and Iron are common materials and aluminium is used when weight is of consideration.

Radiators are associated with the Fans. The Fans blow air across the cores for faster cooling. Thermostat controls the water flow below a given temperature.



(a) Tubular Core



(b) Cellular Core [absolute]

## 2s Diesel Pump

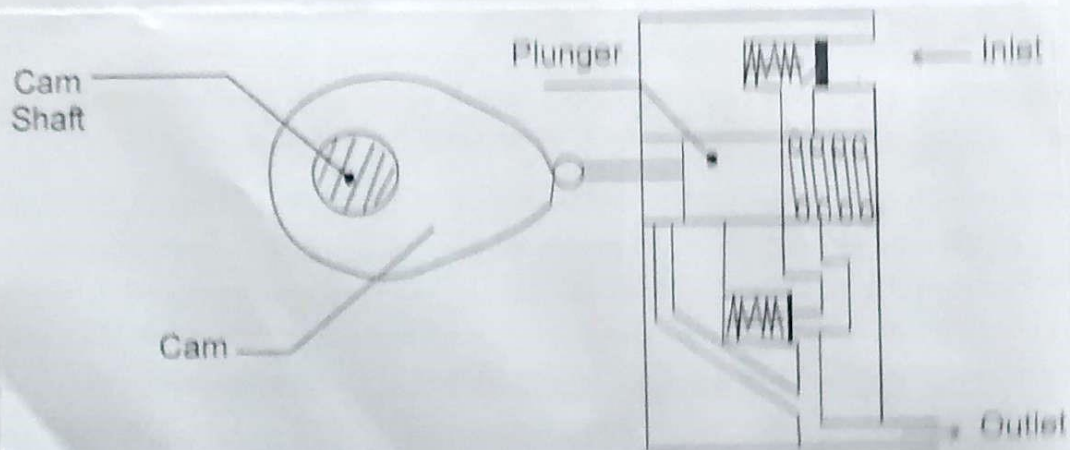
There are many methods of erecting and many types of fuel pumps (or) it may be erected separately outside the injection pump.

It may be driven from the main engine camshaft (or) by the cam in the injection pump drive.

The type of pumps include gear pumps, Vane pumps, diaphragm pumps, plunger pumps etc.

Since we are familiar with the other type of pumps let us describe the plunger pump briefly.

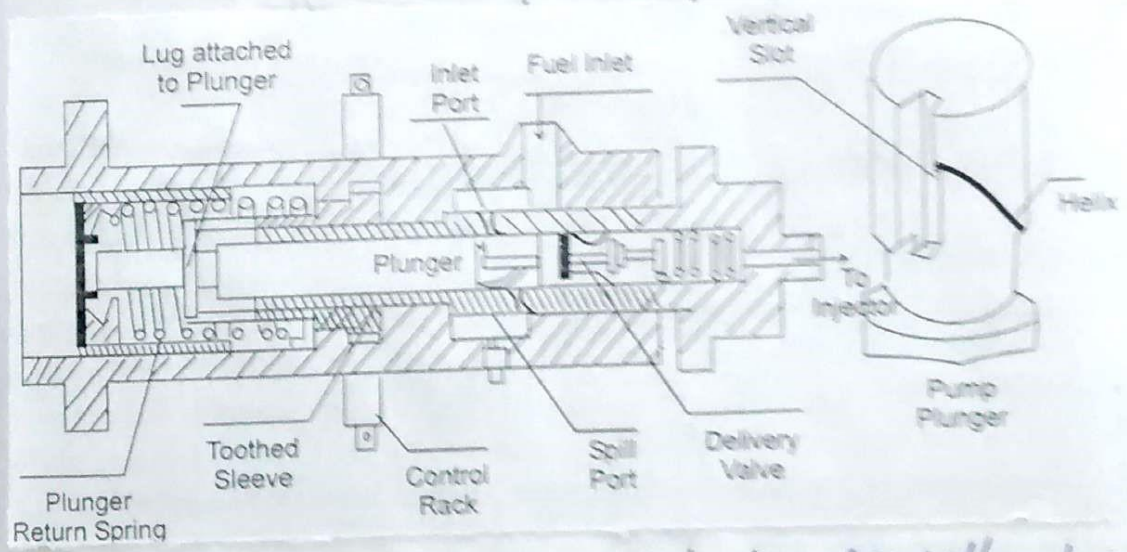
In this plunger pump one movement is forward movement for the plunger is provided by the minimum position of the cam on the camshaft. The return movement is effected by the spring. The forward movement lets fuel inside the cylinder of the pump body through a suction valve & the backward movement lets fuel inside the cylinder of the spring forces the fuel out through the delivery valve.



# Jerk type Injection Pump:

A Pump must have suction, delivery, a Premixing Mechanism and a drive. Additionally the Injection mechanism must have a metering device to allow correct amount of fuel for the speed & load on the engine.

In a jerk pump, a plunger operates inside a cylinder with an inlet port and a spill way port. Inlet port admits fuel from the Feed Pump and the spill way offers passage to excess fuel back to the tank.



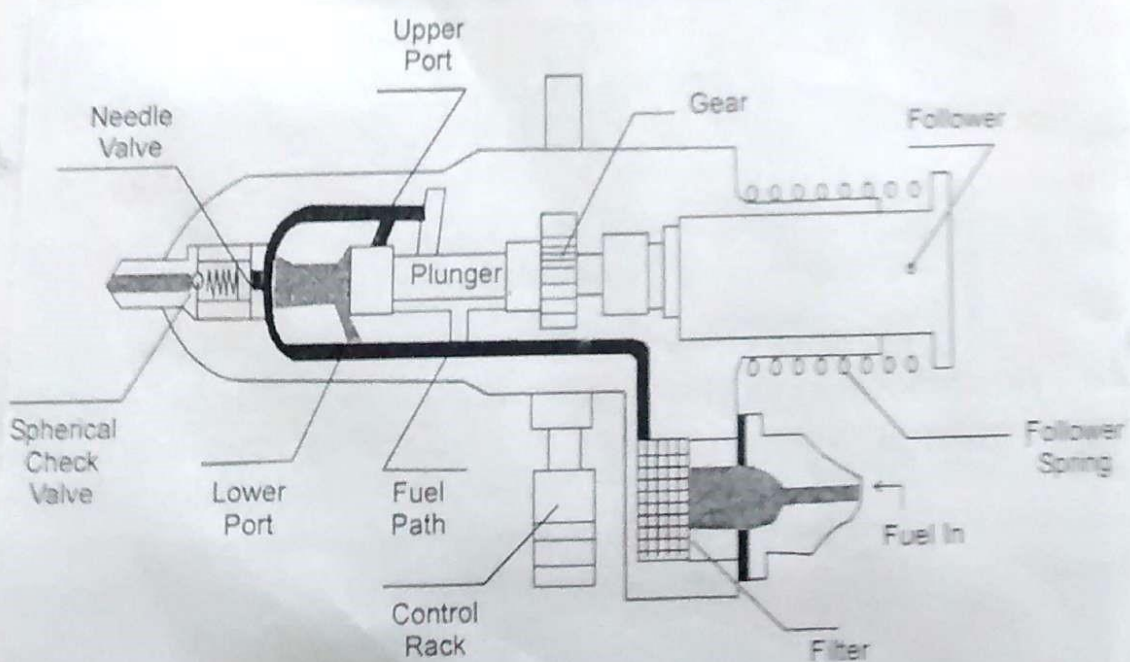
When the fuel is premixed the specially designed delivery valve operating against a spring force and supplies fuel at high pressure to the injector.



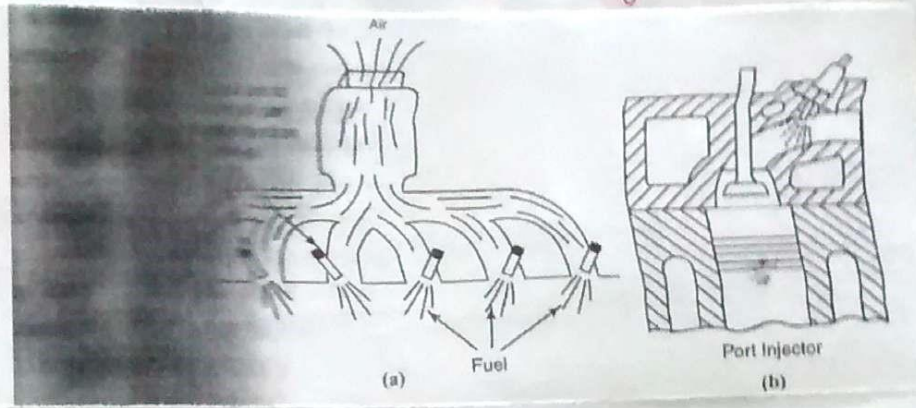
## 2.9. Fuel Injector:

It's been the heart of the IC engine.

The Injector consists of a fuel supply arrangement, a spring loaded well valve and a nozzle. The spring loaded needle valve performs the function of allowing and stopping the flow of fuel. into droplets is to increase the area for mixing and heat transfer and ultimately aimed to achieve good combustion. At the time of injection fuel at a high pressure acts against the spring force and moves the needle upwards. The upward movement of the needle allows the port to be open for fuel to escape through nozzle in a fine spray. Lubrication of the nozzle valve and guided are by leakage fuel.



## 2-10. MPFI (OR) Multi port Fuel Injection system: 47



A low pressure fuel transfer pump, a fuel injection pump and a nozzle are the essential components of the system. Usually injection takes place during the early stage of suction mode. Modern

fuel injection systems use sensors, computer and solenoid operated injectors for achieving metered fuel injection. These electronic devices form part of an electronic fuel injection system.

The computer is also known as ECU and receives signals from the sensors. The data so received are processed and are used to operate the injectors and other devices. The typical sensors used in EFI are  $O_2$  sensor, air flow sensor.

It injects into the individual manifold. If it is an 8 cylinder engine there has to be 8 injectors for the cylinders. 1 injector for each cylinder.

Reviewed  
22/10/2024

## UNIT-3

# STEAM NOZZLES AND TURBINES

### Nozzle:

Nozzle is a duct of varying cross-sectional area in which the velocity increases with corresponding drop in pressure.

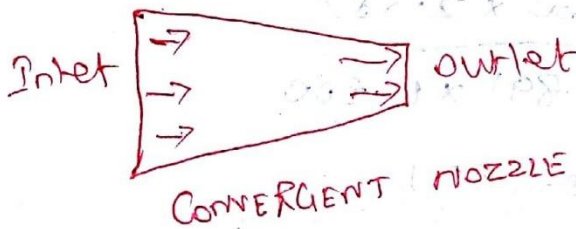
Its main function is to produce a jet of steam with high velocity.

### SHAPES OF NOZZLE:

The following three types of nozzles are important.

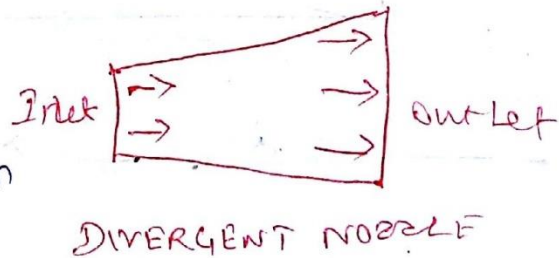
#### 1. Convergent nozzle:

In convergent nozzles, cross sectional area decreases from inlet section to outlet section.



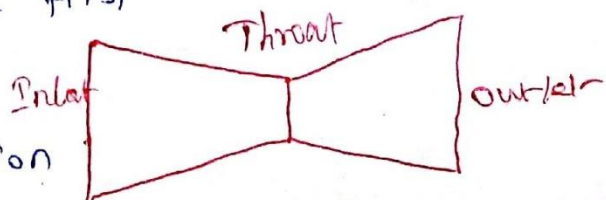
#### 2. Divergent nozzle:

In divergent nozzles, cross sectional area increases from inlet section to outlet section.



#### 3. Convergent-divergent nozzle:

When the cross section of a nozzle first decreases from the inlet section to throat and then it increases from its throat to outlet section. It is called a convergent-divergent nozzle.



## STEAM FLOW THROUGH NOZZLES:

Steam flow through nozzle may be assumed as adiabatic flow. Since no heat is supplied (or) rejected by steam during flow through a nozzle and there is no work done during flow of steam.

$$\text{i.e., } Q=0 \text{ and } W=0$$

### Velocity of Steam:

Steam enters nozzle with high pressure and low velocity, and leaves with high velocity and low pressure.

The outlet velocity ( $V_2$ ) of steam can be found as follows.

Consider a small unit mass flow of steam through a nozzle.

Let,  $V_1$  - Velocity of steam at entrance of nozzle - m/s

$V_2$  - velocity of steam at any section - m/s.

$h_1$  - Enthalpy of steam entering nozzle - kJ/kg.

$h_2$  - Enthalpy of steam at any section - kJ/kg.

For steady flow process:

The steady flow energy equation can be written as,

$$h_1 + \frac{1}{2} m V_1^2 = h_2 + \frac{1}{2} m V_2^2 + \text{Losses} \quad [\because Q=0, W=0]$$

k.k.s, for unit mass flow rate of steam,

$m=1$ , and neglecting losses in nozzle.

$$\text{So, } h_1 + \frac{1}{2} V_1^2 = h_2 + \frac{1}{2} V_2^2$$

$$h_1 + \frac{V_1^2}{2000} = h_2 + \frac{V_2^2}{2000} \quad [\because \text{unit is kJ/kg}]$$

$$(h_1 - h_2) = \frac{1}{2000} [V_2^2 - V_1^2]$$

$$V_2^2 - V_1^2 = 2000(h_1 - h_2)$$

$$V_2^2 = V_1^2 + 2000(h_1 - h_2)$$

$$V_2 = \sqrt{V_1^2 + 2000(h_1 - h_2)}$$

Inlet velocity  $V_1$  is negligible as compared to outlet velocity  $V_2$ . So,

$$V_2 = \sqrt{2000(h_1 - h_2)}$$

$$V_2 = 44.72 \sqrt{h_1 - h_2}$$

### MASS OF STEAM DISCHARGED THROUGH NOZZLES :

The isentropic <sup>Process</sup> in nozzle may be approximately represented by an equation.

$$pV^n = \text{constant}$$

Where,  $n = 1.135$  for Saturated Steam  
 $n = 1.3$  for Superheated Steam.

Let,  $p_1$  - Inlet pressure of steam.

$V_1$  - Specific volume of steam at entry.

$p_2$  - pressure of steam at throat or exit.

$V_2$  - Sp. volume of steam at pressure  $p_2$ .

$V_1$  - Velocity of steam at entry.

$V_2$  - Velocity of steam at exit

As steam passes through the nozzle, its pressure is dropped. So enthalpy is also reduced. This reduction in enthalpy must be equal to increase in K.E. Hence workdone by steam is equal to

The workdone is given by equation  $\frac{n}{n-1} (P_1 V_1 - P_2 V_2)$

Gain in K.E = Workdone during Isentropic process.

$$\frac{V_2^2}{2} - \frac{V_1^2}{2} = \frac{n}{n-1} (P_1 V_1 - P_2 V_2)$$

Since,  $V_1$  is very less than compared to  $V_2$ . It can be neglected. So, the eqn reduces to

$$\frac{V_2^2}{2} = \frac{n}{n-1} P_1 V_1 \left[ 1 - \frac{P_2 V_2}{P_1 V_1} \right]$$

$$P_1 V_1^n = P_2 V_2^n$$

$$\frac{V_2}{V_1} = \left( \frac{P_1}{P_2} \right)^{1/n}$$

Substituting  $\frac{V_2}{V_1}$  value in above eqn,

$$\frac{V_2^2}{2} = \frac{n}{n-1} P_1 V_1 \left[ 1 - \frac{P_2}{P_1} \left( \frac{P_1}{P_2} \right)^{1/n} \right]$$

$$\frac{V_2^2}{2} = \frac{n}{n-1} P_1 V_1 \left[ 1 - \left( \frac{P_2}{P_1} \right) \left( \frac{P_2}{P_1} \right)^{-1/n} \right]$$

$$\frac{V_2^2}{2} = \frac{n}{n-1} P_1 V_1 \left[ 1 - \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]$$

$$V_2 = \sqrt{\frac{2n}{n-1} P_1 V_1 \left( 1 - \frac{P_2}{P_1} \right)^{\frac{n-1}{n}}}$$

W.K.T,

Mass of steam discharged through nozzle per second.

$$m = \frac{\text{Volume of steam flowing per sec}}{\text{Specific volume of steam.}}$$

$$\begin{aligned} \text{Volume of steam flowing per sec} &= \text{Area} \times \text{velocity of steam} \\ &= A \times V_2 \end{aligned}$$

$$\text{Specific volume of steam} = \frac{1}{V_2}$$

$$\therefore m = \frac{A \times V_2}{\frac{1}{V_2}}$$

Substituting  $V_2$  Value of in. above eqn,

$$m = \frac{A}{V_2} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ 1 - \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

W.K.T,

Specific volume,  $V_2 = V_1 \left( \frac{P_1}{P_2} \right)^{1/n}$

$$m = \frac{A}{V_1 \left( \frac{P_1}{P_2} \right)^{1/n}} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ 1 - \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

$$m = \frac{A}{V_1} \left( \frac{P_1}{P_2} \right)^{-1/n} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ 1 - \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

$$m = \frac{A}{V_1} \times \left( \frac{P_2}{P_1} \right)^{1/n} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ 1 - \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

$$= \frac{A}{V_1} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{2/n} \left[ 1 - \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right] \right]}$$

$$= \frac{A}{V_1} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{2/n} - \left( \frac{P_2}{P_1} \right)^{2/n + \frac{n-1}{n}} \right]}$$

$$= \frac{A}{V_1} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{2/n} - \left( \frac{P_2}{P_1} \right)^{\frac{n+1}{n}} \right]}$$

$$= A \sqrt{\frac{2n}{n-1} \frac{P_1 V_1}{V_1^2} \left[ \left( \frac{P_2}{P_1} \right)^{2/n} - \left( \frac{P_2}{P_1} \right)^{\frac{n+1}{n}} \right]}$$

$$m = A \sqrt{\frac{2n}{n-1} \frac{P_1}{V_1} \left[ \left( \frac{P_2}{P_1} \right)^{2/n} - \left( \frac{P_2}{P_1} \right)^{\frac{n+1}{n}} \right]}$$

## EFFECT OF FRICTION IN A NOZZLE:

When the steamy flow through a nozzle, the final velocity of steam for a given pressure drop is reduced due to following reasons.

1. Due to friction between nozzle surface & steam.
2. Due to internal fluid friction in steam.
3. Due to shock losses.

Most of these frictional losses occur bet throat & exit in a convergent-divergent nozzle.

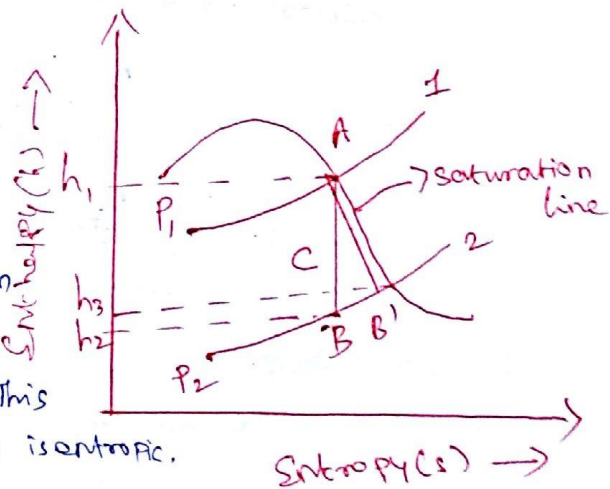
The effects of these frictional losses are listed below

1. The expansion is no more isentropic and enthalpy drop is reduced by resulting lower exit velocity.
2. The final dryness fraction of steam is increased as part of K.E gets converted into heat due to friction and absorbed by steam with increase in enthalpy.
3. The specific volume of steam is increased as steam becomes drier due to this frictional reheating.

The point A represents initial condition of steam. It is a point where the saturation line meets initial pressure ( $P_1$ ) line.

If friction is neglect, the expansion of steam from entry to throat is represented by vertical line AB. This is done, as flow through nozzle is isentropic.

The enthalpy drop ( $h_1 - h_2$ ) is known as isentropic enthalpy drop.



NOZZLE EFFICIENCY.

$$\eta = \frac{\text{Actual enthalpy drop}}{\text{Isentropic enthalpy drop}} = \frac{AC}{AB} = \frac{h_1 - h_3}{h_1 - h_2}$$



## CRITICAL PRESSURE RATIO:

There is only one value of ratio ( $P_2/P_1$ ) which produces the maximum discharge from nozzle. This ratio is called critical pressure ratio.

Where,  $P_1$  - Inlet pressure

$P_2$  - Throat pressure

(i) For saturated steam,  $n = 1.135$

The critical pressure ratio is given by

$$\frac{P_2}{P_1} = \left( \frac{2}{n+1} \right)^{\frac{n}{n-1}} = \left( \frac{2}{1.135+1} \right)^{\frac{1.135}{1.135-1}}$$

Critical pressure ratio,  $\frac{P_2}{P_1} = 0.577$

(ii) For superheated steam  $n = 1.3$ ,

$$\frac{P_2}{P_1} = \left( \frac{2}{n+1} \right)^{\frac{n}{n-1}} = \left( \frac{2}{1.3+1} \right)^{\frac{1.3}{1.3-1}}$$

Critical pressure ratio,  $\frac{P_2}{P_1} = 0.526$

(iii) For gases,  $n = 1.4$ ,

$$\text{Critical pressure ratio, } \frac{P_2}{P_1} = \left( \frac{2}{n+1} \right)^{\frac{n}{n-1}}$$

$$\frac{P_2}{P_1} = \left( \frac{2}{1.4+1} \right)^{\frac{1.4}{1.4-1}}$$

$\frac{P_2}{P_1} = 0.5282$

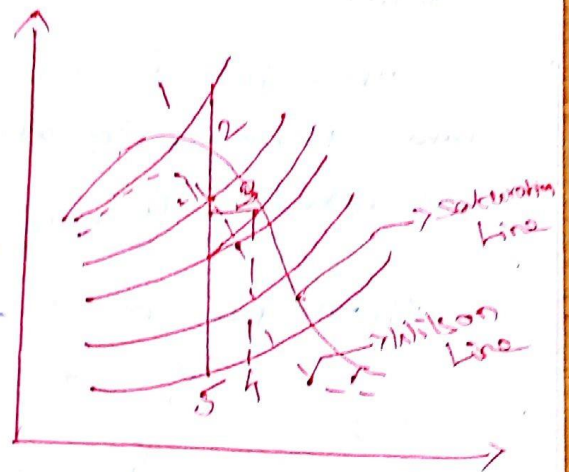
## SUPERSATURATED FLOW (OR) METASTABLE FLOW OF STEAM IN A NOZZLE:

When the superheated steam expands in nozzle, the condensation will occur in nozzle. Since, the steam has more velocity, the condensation will not take place at the saturated state. So equilibrium between liquid and vapour phase is delayed and steam continues to expand in a dry state.

The steam in such set of condition is said to be superheated "Supersaturated" (or) "Metastable flow".

The ideal expansion of superheated steam from pressure  $P_1$  to  $P_4$  can be represented by a line 1-5 on mollier diagram.

During the expansion, the change of phase must start to occur at pressure  $P_2$  as shown where expansion line meets the saturation line (Point 2).



But in nozzles under certain conditions, this phenomenon of condensation does not occur at point 2 as time available is very short due to high velocity of steam passing through nozzle.

The equilibrium bet liquid & vapour phase is therefore delayed and vapour continues to expand in dry state even beyond point (2).

The vapour bet pressure  $P_2$  &  $P_3$  is said to be supersaturated and this type of flow in nozzle known as "Supersaturated (or) metastable flow of steam". A limit to supersaturated state was observed by Wilson & a line drawn on chart through observed point is known as Wilson line.

The flow is also called as supercooled flow because at any pressure bet  $P_2$  &  $P_3$  the temp of vapour is always lower than saturation temp corresponding to pressure. The diff in this temp is known as degree of "Under-cooling".

### Problem:

Dry saturated steam at a pressure of 11 bar enters a convergent-divergent nozzle and leaves at a pressure of 2 bar. If flow is adiabatic and frictionless, determine:

- (i) Exit velocity of steam
- (ii) ratio of cross-section of exit and that at throat.

### Given:

$$P_1 = 11 \text{ bar}$$

$$P_2 = 2 \text{ bar}$$

### Soln:

The critical pressure ratio when steam is initially dry

$$\text{Saturated, } \frac{P_t}{P_1} = 0.577$$

Throat pressure of steam,

$$P_t = 0.577 \times P_1 = 0.577 \times 11$$

$$P_t = 6.38 \text{ bar}$$

Properties of steam at 11 bar and  $250^\circ\text{C}$

$$h_1 = 2780 \text{ kJ/kg}$$

Since, expansion is isentropic, from  $h_1 = 2780 \text{ kJ/kg}$ , a vertical line is drawn in mollier diagram up to 6.38 bar pressure line. Now, following values are noted at point,

$$h_t = 2679 \text{ kJ/kg}, \quad v_t = 0.285 \text{ m}^3/\text{kg}$$

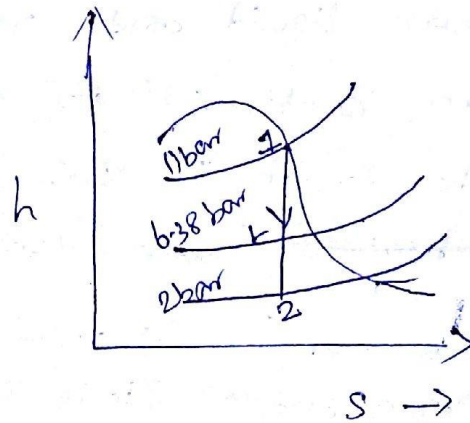
Velocity of steam at throat,

$$V_t = \sqrt{2000(h_1 - h_t)} = \sqrt{2000(2780 - 2679)}$$

$$V_t = 449.44 \text{ m/s}$$

mass flow rate of steam / nozzle.

$$m = \frac{A_1 V_t}{v_t}$$



h-s diagram.

$$\text{Throat Area, } A_t = \frac{m v_t}{V_t}$$

$$A_t = \frac{m \times 0.285}{249.44}$$

$$A_t = 6.34 \times 10^{-3} \text{ m}$$

Similarly, a vertical line is drawn in mollier diagram up to 2 bar pressure line from  $h_1 = 2780 \text{ kJ/kg}$ . Now following values are noted at that point.

$$h_2 = 2480 \text{ kJ/kg}$$

$$v_2 = 0.7965 \text{ m}^3/\text{kg}$$

$$\text{Velocity of steam at exit, } = \sqrt{2000(h_1 - h_2)}$$

$$= \sqrt{2000(2780 - 2480)}$$

$$V_2 = 774.6 \text{ m/s}$$

$$\text{Exit Area, } A_2 = \frac{m \cdot v_2}{V_2} = \frac{m \times 0.7965}{774.6}$$

$$A_2 = 1.028 \times 10^{-3} \text{ m}$$

Ratio of exit area to throat area:

$$\frac{A_2}{A_1} = \frac{1.028 \times 10^{-3} \text{ m}}{6.34 \times 10^{-3} \text{ m}} = 0.162$$

$$\frac{A_2}{A_1} = 0.162$$

## Problem

A convergent-divergent nozzle is required to discharge 2 kg of steam per sec. The nozzle is supplied with steam at 7 bar and 180°C and discharge takes place against a back pressure of 1 bar. The expansion up to throat is isentropic and friction resistance bet throat and exit is equivalent to 63 kJ/kg of steam. Taking approach velocity of 75 m/s and throat 4 bar, estimate:

- (1) Suitable areas for throat & exit and
- (2) overall efficiency of nozzle based on enthalpy drop between the actual inlet pressure and temp and exit pressure.

## Given data:

$$m = 2 \text{ kg/s}, P_1 = 7 \text{ bar}, T_1 = 180^\circ\text{C}, P_t = 4 \text{ bar}, P_2 = 1 \text{ bar}$$
$$h_2 - h_{2s} = 63 \text{ kJ/kg}, V_1 = 75 \text{ m/s}.$$

## Soln:

Properties of steam from steam tables,  
At 7 bar and 180°C

$$h_1 = 2888.5 \text{ kJ/kg}; S_1 = 6.975 \text{ kJ/kg}\cdot\text{K}$$

$$v_1 = 0.3146 \text{ m}^3/\text{kg}.$$

$S_1$  is more than  $S_{gt}$ . Therefore, the steam is again in superheated condition.

From mollier diagram, comes to 4 bar.

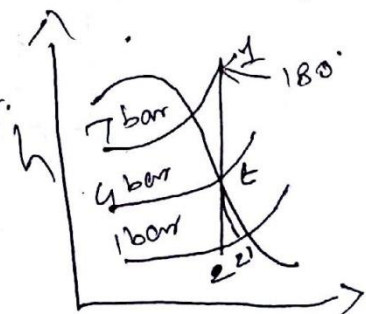
$$h_t = 2780 \text{ kJ/kg}, v_t = 0.462455 \text{ m}^3/\text{kg}.$$

At 1 bar,

$$h_f = 417.4 \text{ kJ/kg}, h_g = 2675 \text{ kJ/kg}$$

$$S_f = 1.303 \text{ kJ/kg}\cdot\text{K}, S_g = 7.359 \text{ kJ/kg}\cdot\text{K}$$

$$v_f = 0.001043 \text{ m}^3/\text{kg}, v_g = 1.694 \text{ m}^3/\text{kg}.$$



$h \rightarrow$  diagram

1-2  $\Rightarrow$  Isentropic Expansion

$$s_1 = s_2 = 6.975 \text{ kJ/kg}$$

$$s_2 = s_{f2} + x_2 \cdot s_{fg2}$$

$$6.975 = 1.303 + x_2 \times (7.359 - 1.303)$$

$$x_2 = 0.937$$

$$h_2 = h_{f2} + x_2 \cdot h_{fg2}$$

$$= 417.4 + 0.937 \times (2675 - 417.4)$$

$$h_2 = 2532.77 \text{ kJ/kg}$$

But,  $h_2' - h_2 = 63 \text{ kJ/kg}$ .

$$h_2' = 2532.77 + 63 = 2595.77 \text{ kJ/kg}$$

Velocity of steam at throat,

$$V_t = \sqrt{2000(h_1 - h_t) + \frac{V_1^2}{2000}}$$

$$= \sqrt{2000(2888.5 - 2180) + \frac{75^2}{2000}}$$

$$V_t = 465.62 \text{ m/s}$$

Throat Area,  $A_t = \frac{m \cdot V_t}{V_t} = \frac{2 \times 0.462455}{465.62}$

$$A_t = 0.0001986 \text{ m}^2$$

Velocity of steam at throat,

$$V_2 = \sqrt{2000(h_1 - h_2') + \frac{V_1^2}{2000}}$$

$$= \sqrt{2000(2888.5 - 2469.77) + \frac{75^2}{2000}}$$

$$V_2 = 915.13 \text{ m/s}$$

To calculate  $x_2'$ ,

$$h_2' = h_{f2} + x_2' \cdot h_{fg2}$$

$$h_{\max} = 2V_b \left[ v_i \cdot \frac{2V_b}{v_i} - V_b \right]$$

$$= 2V_b (2V_b - V_b)$$

$$h_{\max} = 2V_b^2$$

## VELOCITY DIAGRAM FOR MULTISTAGE TURBINES:

### Pressure Compounding:

When four simple impulse turbines are connected in series, the total enthalpy drop is divided equally among stages. So, the pressure drop only occurs in nozzle whereas there is no pressure drop in blades. Therefore, the corresponding h-s diagram for 4-stage pressure compounding steam turbine is given below:

Enthalpy drop in each stage  $h$  will be equal,

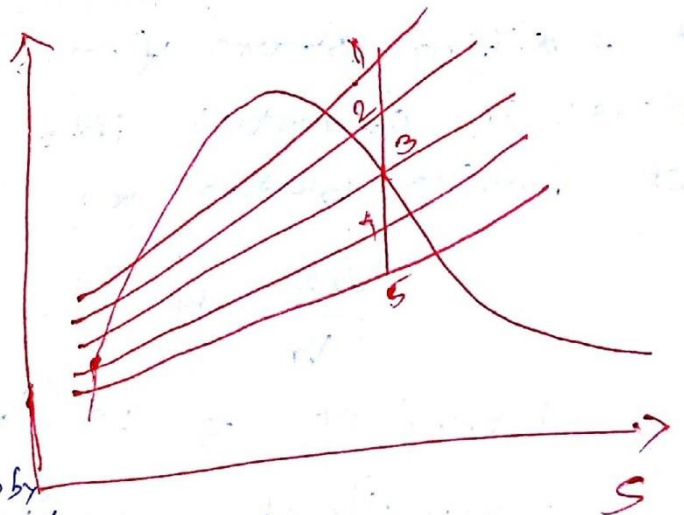
$$h_1 - h_2 = h_2 - h_3 = h_3 - h_4 = h_4 - h_5$$

$$\text{So, } h_1 - h_2 = \frac{h_1 - h_5}{4}$$

The velocity of steam at exit from first row of nozzle is given by,

$$\begin{aligned} V_1 &= \sqrt{2000(h_1 - h_2)} \\ &= \sqrt{2000 \left( \frac{h_1 - h_5}{4} \right)} \\ &= \frac{1}{2} \sqrt{2000(h_1 - h_5)} \end{aligned}$$

But for a single stage turbine, the velocity of steam at exit of nozzle,  $V_1 = \sqrt{2000(h_1 - h_5)}$ .



h-s diagram.

For n-stage, enthalpy drop per stage will be

$$(\Delta h)_{\text{Stage}} = \frac{(\Delta h)_{\text{Total}}}{n} = \frac{h_1 - h_n}{n}$$

(or)

$$\text{No. of stages} = \frac{(\Delta h)_{\text{Total}}}{(\Delta h)_{\text{Stage}}}$$

... ..

### Velocity Compounding :-

The K.E of steam jets ( $\frac{1}{2} m v_1^2$ ) at nozzle exit is partially converted into work in 1st row of moving blades with velocity diff from  $v_1$  to  $v_2$ . Again K.E ( $\frac{1}{2} m v_2^2$ ) of exiting steam from first row of moving blades is converted into work in next row of moving blades and so on.

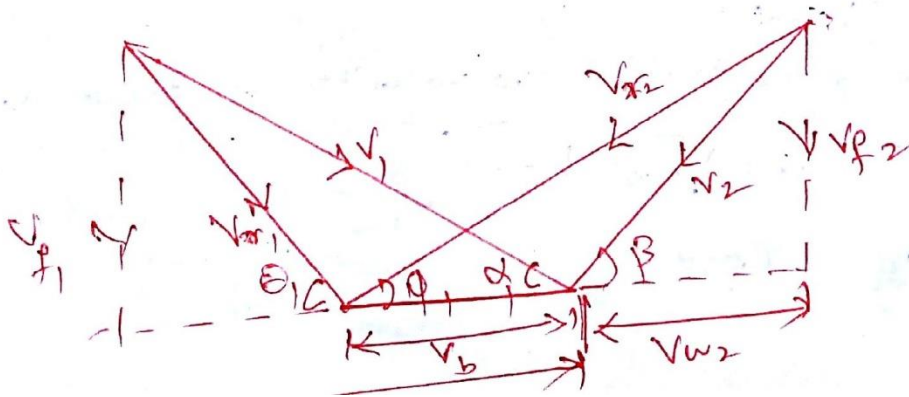
$$\frac{v_{r2}}{v_{r1}} = k \dots$$

$$\text{Work done} = m (v_{w1} + v_{w2}) V_b$$

$$\text{Axial Thrust} = m (v_{f1} - v_{f2})$$

K.E of steam supplied for first stage,

$$K.E_1 = \frac{1}{2} m v_1^2$$





Same friction factor is considered for next row of moving blades.

$$\frac{V_3}{V_2} = k \text{ and also } \frac{V_{r4}}{V_{r3}} = k.$$

$$\text{Work done}_{II} = m (V_{w3} + V_{w4}) V_b.$$

$$\text{Axial Thrust} = F_{yII} = m (V_{f3} - V_{f4})$$

$$k \cdot E = \frac{1}{2} m V_3^2$$

∴ Total efficiency of steam turbine,

$$\eta = \frac{\text{Work done}_I + \text{Work done}_{II}}{k \cdot E_I + k \cdot E_{II}}$$

$$= \frac{m (V_{w1} + V_{w2}) V_b + m (V_{w3} + V_{w4}) V_b}{\frac{1}{2} m V_1^2 + \frac{1}{2} m V_3^2}$$

$$\eta = \frac{2 V_b (V_{w1} + V_{w2} + V_{w3} + V_{w4})}{V_1^2 + V_3^2}$$

$$\text{Total axial Thrust, } F_y = F_{yI} + F_{yII}$$

$$= m (V_{f1} - V_{f2} + V_{f2} - V_{f4})$$

$$= m [(V_{f1} + V_{f3}) - (V_{f2} + V_{f4})]$$

→ x —

### Problem:

The following data refer to a single stage impulse turbine: Isentropic nozzle enthalpy drop =  $200 \text{ kJ/kg}$   
Nozzle efficiency =  $90\%$ , Nozzle angle =  $25^\circ$ .

Ratio of blade speed to whirl component of steam speed =  $0.5$   
Blade Co-eff =  $0.9$ , The velocity of steam entering the nozzle is  $30 \text{ m/s}$ ,  
Find (i): the blade angles at inlet and outlet if steam enters blade without shock & leaves the blade in axial direction.

(ii) blade efficiency.

(iii) power developed.

(iv) axial thrust if steam flow rate is  $10 \text{ kg/s}$ .

### Given data:

$$h_i = h_{e'} = 200 \text{ kJ/kg}, \quad \eta_N = 90\%, \quad \alpha = 25^\circ, \quad \frac{V_b}{V_{w1}} = 0.5$$

$$\frac{V_{f2}}{V_{w1}} = 0.9, \quad V_1 = 30 \text{ m/s}, \quad V_2 = V_{f2}, \quad V_{w2} = 0, \quad \beta = 90^\circ$$

### Soln:

Actual enthalpy drop,

$$h_i - h_e = (h_i - h_{e'}) \times \eta_N$$

$$h_i - h_e = 200 \times 0.9 = 180 \text{ kJ/kg}.$$

Exit velocity of nozzle,

$$V_e = \sqrt{2(h_i - h_e) + V_1^2}$$

$$= \sqrt{2(180 \times 1000) + 30^2}$$

$$V_e = 600.75 \text{ m/s}.$$

Inlet velocity of steam to turbine,

$$V_1 = V_e = 600 \text{ m/s}.$$

From  $\Delta ABC$ ,  $V_{w1} = V_1 \cos 25^\circ = 600.75 \cos 25^\circ = 544.46 \text{ m/s}.$

$$V_{f1} = V_1 \sin 25^\circ = 600.75 \sin 25^\circ = 253.89 \text{ m/s}.$$

$$\frac{V_b}{V_{w1}} = 0.5$$

$$\therefore V_b = 0.5 \times 544.46 = 272.23 \text{ m/s}$$

From  $\triangle ACE$ ,  $V_{r1} = \sqrt{V_{f1}^2 + (V_{w1} - V_b)^2}$

$$= \sqrt{253.89^2 + (544.46 - 272.23)^2}$$

$$= 372.25 \text{ m/s}$$

$$\tan \theta = \frac{V_{f1}}{V_{w1} - V_b} = \frac{253.89}{544.46 - 272.23}$$

$$\theta = 43^\circ$$

$$V_{r2} = 0.9 \times V_{r1} = 0.9 \times 372.25 = 335.03 \text{ m/s}$$

From  $\triangle ADB$ ,  $\cos \phi = \frac{AB}{AD} = \frac{V_b}{V_{r2}} = \frac{272.23}{335.03}$

$$\phi = 35^\circ 39'$$

$$V_L = \sqrt{V_{r2}^2 - V_b^2} = \sqrt{335.03^2 - 272.23^2} = 195.28 \text{ m/s}$$

$$\therefore V_f = V_L = 195.28 \text{ m/s}$$

Power developed,  $P = m (V_{w1} + V_{w2}) \times V_b$

$$= 10 (544.46 + 0) \times 272.23$$

$$P = 1482.18 \text{ kW}$$

Blade efficiency,  $\eta_b = \frac{(V_{w1} + V_{w2}) V_b}{1/2 V_1^2}$

$$\eta_b = 82.14 \%$$

Axial Thrust,  $F_y = m (V_{f1} - V_{f2})$

$$= 10 (253.89 - 195.28)$$

## UNIT-4

### AIR COMPRESSORS

W. V. Shukla

#### INTRODUCTION-

The process of increasing the pressure of air, gas or vapour by reducing its volume is called compression and device used to carry out this process is called a Compressor.

Compressed air is mostly used in pneumatic brakes, pneumatic drills, pneumatic jacks, pneumatic lifts, spray painting, shop cleaning, injecting fuel in diesel engines. etc.

#### CLASSIFICATION OF AIR COMPRESSOR:

(1) According to design & principle of operation

(a) Reciprocating Compressors

(b) Rotary Compressors.

(2) According to action

(a) Single acting compressors

(b) Double acting compressors.

to no. of stages.

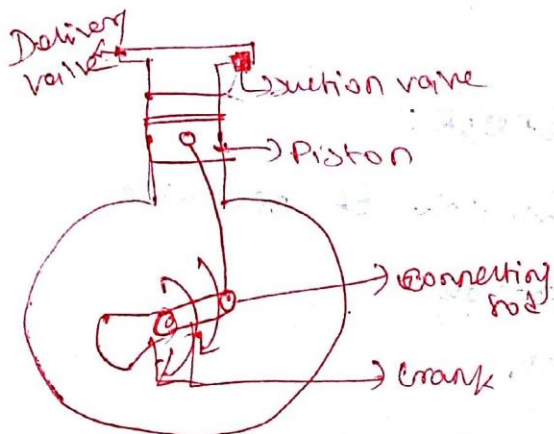
# WORKING OF SINGLE STAGE RECIPROCATING AIR

## COMPRESSOR:

In a single stage compressor, the compression of air from the initial pressure to final pressure is carried out in one cylinder only.

It consists of a cylinder, piston, connecting rod, crank, inlet & discharge valves.

When the piston moves downwards i.e. during suction stroke, the pressure of air inside the cylinder falls below atm pressure.



AIR COMPRESSOR

So, the inlet valve opens and air from atm is sucked into cylinder until piston reaches bottom dead center.

So during this stroke, the delivery valve remains closed. When piston moves upwards, both valves are closed. So, the pressure inside the cylinder goes on increasing till it reaches required discharge pressure.

At this stage, discharge valve opens and compressed air is delivered through this valve. This cycle is repeated.

# WORK DONE BY A SINGLE STAGE RECIPROCATING AIR COMPRESSOR WITHOUT CLEARANCE VOLUME.

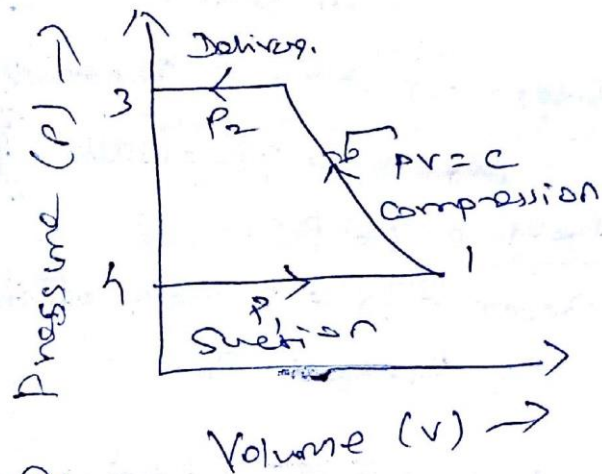
(a) Work done during Isothermal compression ( $PV=c$ )

$P-v$  diagram for air

Process 4-1 = Suction of air @ pressure  $P_1$

Process 1-2 = Isothermal compression

Process 2-3 = Discharge of air @ pressure  $P_2$



Work done = Area 1-2-3-4-1

$$W = W_{\text{comp}} + W_{\text{del}} + W_{\text{sue}}$$

$$= P_1 v_1 \ln\left(\frac{v_1}{v_2}\right) + P_2 v_2 - P_1 v_1$$

$$= P_1 v_1 \ln\left(\frac{v_1}{v_2}\right) + P_2 v_2 - P_1 v_1$$

[ $\because P_1 v_1 = P_2 v_2$  for isothermal process.]

$$\therefore W = P_1 v_1 \ln\left(\frac{v_1}{v_2}\right)$$

$$\frac{v_1}{v_2} = \frac{P_2}{P_1} \quad \left[ \because P_1 v_1 = P_2 v_2 \right]$$

$$\therefore W = P_1 v_1 \ln\left(\frac{P_2}{P_1}\right)$$

$Pv = mRT$

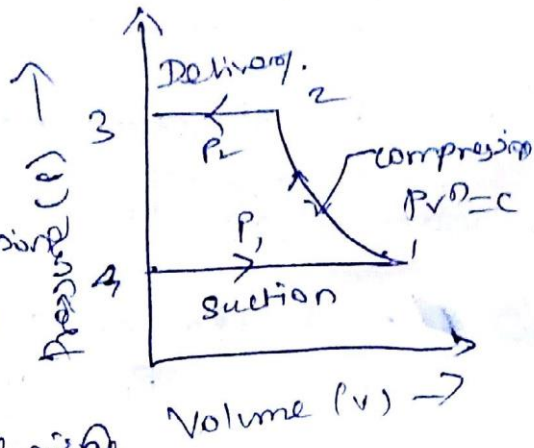
$$W = mRT_1 \ln\left(\frac{P_2}{P_1}\right)$$

(b) Work done during polytropic compression ( $PV^n = c$ )

Process 4-1 - suction of air at pressure  $P_1$

Process 1-2 represents compression of air polytropically from  $P_1$  to  $P_2$ .

Process 2-3 - delivery of air @ pressure  $P_2$ .



Work done = Area 1-2-3-4-1

$$W = W_{comp} + W_{del} - W_{sue.}$$

$$W = \frac{P_2 V_2 - P_1 V_1}{n-1} + P_2 V_2 - P_1 V_1$$

$$= \frac{P_2 V_2 - P_1 V_1 + (n-1) P_2 V_2 - (n-1) P_1 V_1}{n-1}$$

$$= \frac{P_2 V_2 - P_1 V_1 + n P_2 V_2 - P_2 V_2 - n P_1 V_1 + P_1 V_1}{n-1}$$

$$= \frac{n P_2 V_2 - n P_1 V_1}{n-1} = \frac{n (P_2 V_2 - P_1 V_1)}{n-1}$$

$$\therefore W = \frac{n}{n-1} (P_2 V_2 - P_1 V_1)$$

$$P_1 V_1 = m R T_1, \quad P_2 V_2 = m R T_2$$

$$W = \frac{n}{n-1} [m R T_2 - m R T_1]$$

$$= \frac{n}{n-1} m R (T_2 - T_1)$$

$$W = \frac{n}{n-1} m R T_1 \left( \frac{T_2}{T_1} - 1 \right)$$

For polytropic process,  $\frac{T_2}{T_1} = \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}}$

$$W = \frac{\gamma}{\gamma-1} m R T_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

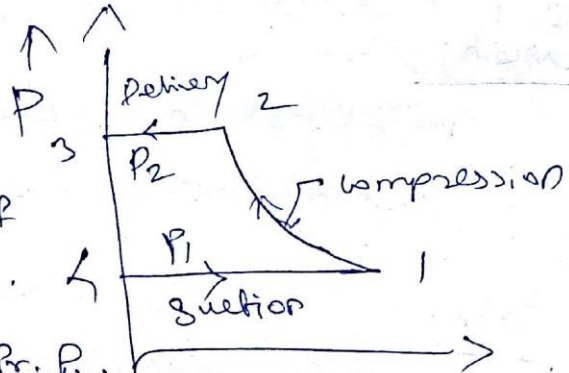
$$W = \frac{\gamma}{\gamma-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \quad (\because P V = m R T)$$

c) Work done during isentropic compression: ( $P V^\gamma = c$ )

Process 4-1 - Suction of air at pressure  $P_1$

Process 1-2 - isentropic comp of air from  $P_1$  to  $P_2$ .

Process 2-3 - delivery of air @ Pr.  $P_2$ .



Work done = Area 1-2-3-4-1

Isentropic compression.

$$W = W_{\text{comp}} + W_{\text{del}} - W_{\text{suc}}$$

$$= \frac{P_2 V_2 - P_1 V_1}{\gamma-1} + P_2 V_2 - P_1 V_1$$

$$W = \frac{P_2 V_2 - P_1 V_1 + (\gamma-1) P_2 V_2 - (\gamma-1) P_1 V_1}{\gamma-1}$$

$$W = \frac{\gamma (P_2 V_2 - P_1 V_1)}{\gamma-1}$$

$$\therefore W = \frac{\gamma}{\gamma-1} (P_2 V_2 - P_1 V_1)$$

$$P_1 V_1 = m R T_1, \quad P_2 V_2 = m R T_2$$

$$W = \frac{\gamma}{\gamma-1} (m R T_2 - m R T_1)$$

$$W = \frac{\gamma}{\gamma-1} m R T_1 \left( \frac{T_2}{T_1} - 1 \right)$$

$$W = \frac{\gamma}{\gamma-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \quad (\because P V = m R T)$$



## Problem:

A single stage air compressor is required to compress  $0.75 \text{ m}^3$  of air from 1.2 bar to 9 bar at  $27^\circ \text{C}$ . The compression takes place according to law  $pV^{1.35} = c$ . Determine work done by compressor and temp at end of compression.

## Given:

$$V_1 = 0.75 \text{ m}^3, P_1 = 1.2 \text{ bar} = 120 \text{ kPa}.$$

$$P_2 = 9 \text{ bar}, T_1 = 300 \text{ K}, n = 1.35$$

## Soln.

Work done on a single stage reciprocating air compressor without clearance volume.

$$W = \frac{n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} - 1 \right]$$

$$W = \frac{1.35}{1.35-1} \cdot 120 \times 0.75 \cdot \left[ \left( \frac{900}{120} \right)^{\frac{1.35-1}{1.35}} - 1 \right]$$

$$W = 238.15 \text{ kJ}.$$

w.k.t

$$\frac{T_2}{T_1} = \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}}$$

$$T_2 = 300 \times \left( \frac{900}{120} \right)^{\frac{0.35}{1.35}}$$

$$T_2 = 505.812 \text{ K}$$



$$\beta = \frac{V_a}{V_s}$$

from P-V diagram

$$V_a = V_s - x$$

$$x = V_4 - V_c$$

$$b_{vol} = \frac{V_s - s}{V_s} = \frac{V_s - (V_4 - V_c)}{V_s}$$

$$= \frac{V_s - V_c \left[ \frac{V_4}{V_c} - 1 \right]}{V_s}$$

$$b_{vol} = 1 - \frac{V_c}{V_s} \left[ \frac{V_4}{V_c} - 1 \right]$$

Both compression & expansion follow the law  $pV^n = \text{const}$

$$P_3 V_3^n = P_4 V_4^n$$

$$\frac{V_4}{V_3} = \left( \frac{P_3}{P_4} \right)^{1/n}$$

from P-V diagram,

$$V_3 = V_c, P_4 = P_1, P_3 = P_2$$

$$\frac{V_4}{V_3} = \left( \frac{P_3}{P_4} \right)^{1/n}$$

$$\frac{V_4}{V_c} = \left( \frac{P_2}{P_1} \right)^{1/n}$$

$$b_{vol} = 1 - \frac{V_c}{V_s} \left[ \left( \frac{P_2}{P_1} \right)^{1/n} - 1 \right]$$

Clearance ratio,  $C = \frac{V_c}{V_s}$

$$b_{vol} = 1 - C \left[ \left( \frac{P_2}{P_1} \right)^{1/n} - 1 \right]$$

$$b_{vol} = 1 + C - C \left[ \left( \frac{P_2}{P_1} \right)^{1/n} \right]$$

Actual  $\eta$ ,

$$\eta_{\text{act}} = \frac{V_a}{V_s}$$

$$0.75 = \frac{25}{V_s}$$

$$V_s = 33.33 \text{ m}^3/\text{min.}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$T_2 = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}} \times T_1$$

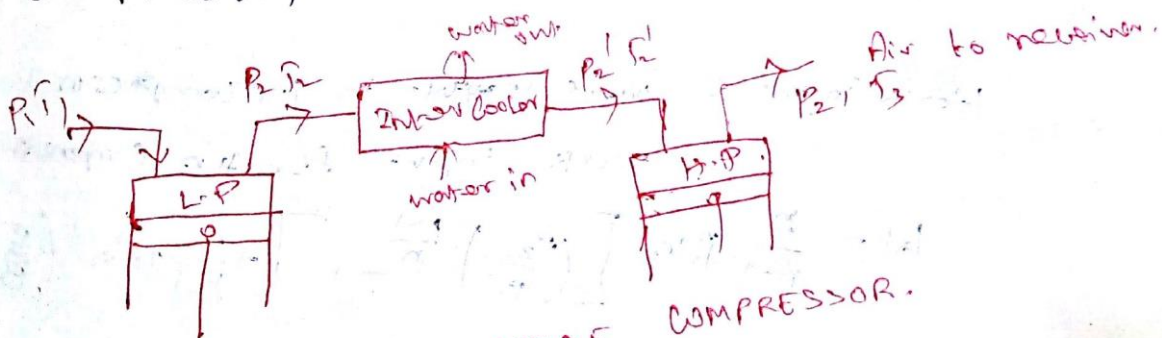
$$T_2 = 288 \times \left(\frac{1500}{100}\right)^{\frac{1.4-1}{1.4}}$$

$$T_2 = 581.17 \text{ K}$$

### MULTI STAGE AIR COMPRESSOR WITH INTERCOOLING

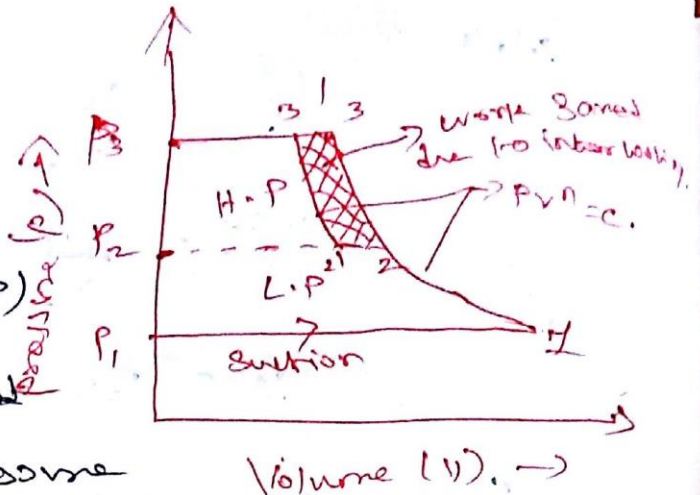
In a multistage compressor, compression of air from initial pressure, to final pressure is carried out in more than one cylinder.

It is used to get high-pressure air. In a compressor, when compression ratio exceeds 5.



MULTI STAGE COMPRESSOR.

It consists of a low-pressure cylinder (LP) an inter cooler and a high-pressure cylinder (HP). The fresh air is sucked



from atm in low-pressure cylinder during its suction stroke at intake pressure  $P_1$  and temp  $T_1$ .

The air after compression in LP cylinder is delivered to intercooler at pressure  $P_2$  and temp  $T_2$ .

In inter cooler, the air is cooled at constant pressure by circulating cold water. The cooled air from intercooler is then taken to high-pr cylinder.

In high pressure cylinder, air is further compressed to final delivery pressure ( $P_3$ ) and discharged to receiver.

WORK DONE BY A TWO-STAGE COMPRESSOR WITH INTERCOOLER

Work input = Work input in LP compressor + Work input for HP compressor.

$$W = \frac{n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} - 1 \right] + \frac{n}{n-1} P_2 V_2 \left( \frac{P_3}{P_2} \right)^{\frac{n-1}{n}}$$

$$W = \frac{n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right] + \frac{n}{n-1} P_1 V_1 \left[ \left( \frac{P_3}{P_2} \right)^{\frac{n-1}{n}} \right]$$

$$W = \frac{n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} + \left( \frac{P_3}{P_2} \right)^{\frac{n-1}{n}} - 2 \right]$$

Problem.

A Two stage single acting reciprocating air compressor takes  $6 \text{ m}^3$  of air at 1 bar &  $23^\circ \text{C}$  and compresses it into 20 bar.

The intermediate receiver cools the air to  $25^\circ \text{C}$  and 8.5 bar pressure. The law of comp.  $PV^{1.35} = C$ .  
Calculate work done.

Given.

$$V_1 = 6 \text{ m}^3, P_1 = 1 \text{ bar}, T_1 = 300 \text{ K}, P_3 = 20 \text{ bar},$$

$$T_2' = 298 \text{ K}, P_2' = 8.5 \text{ bar}, n = 1.35$$

Soln.:

$$W = \frac{n}{n-1} P_1 V_1 \left[ \left( \frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right] + \frac{n}{n-1} P_2 V_2 \left[ \left( \frac{P_3}{P_2} \right)^{\frac{n-1}{n}} \right]$$

$$V_2 = V_1 \left( \frac{P_1}{P_2} \right)^{\frac{1}{1.35}} = 6 \left( \frac{110}{850} \right)^{\frac{1}{1.35}} = 1.319 \text{ m}^3$$

$$T_2 = T_1 \left( \frac{P_2}{P_1} \right)^{\frac{0.35}{1.35}} = 300 \times \left( \frac{850}{110} \right)^{\frac{0.35}{1.35}} = 509.74 \text{ K}$$

$$\frac{V_2}{T_2} = \frac{V_2'}{T_1} \Rightarrow V_2' = V_2 \times \frac{T_2'}{T_2}$$

$$V_2' = 1.319 \times \frac{298}{509.7} = 0.771 \text{ m}^3$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$V_2 = \frac{P_1 V_1 T_2}{P_2 T_1} = \frac{110 \times 6 \times 298}{850 \times 300} = 0.771 \text{ m}^3$$

$$W = \frac{1.35}{1.35-1} \times 110 \times 6 \times \left[ \left( \frac{850}{110} \right)^{\frac{1.35-1}{1.35}} - 1 \right]$$

$$+ \frac{1.35}{1.35-1} \times 850 \times 0.771 \times \left[ \left( \frac{2000}{850} \right)^{\frac{1.35-1}{1.35}} - 1 \right]$$

$$W = 2407.64 \text{ kJ}$$

A three stage air compressor delivers  $5 \text{ m}^3$  of free air per min. The suction P & Temp are 1 bar and  $20^\circ\text{C}$ . The pressure & Temp are 10.13 bar and  $20^\circ\text{C}$  at free air condition. The air is cooled at  $30^\circ\text{C}$  after each stage of compression. The delivery pressure of compressor is 150 bar. Rpm of the compressor is 300. The diameters of L.P, I.P & H.P cylinders are 5% of respective strokes. The index of comp & expansion is 1.35. Neglecting fri losses, find the R.P of motor required to run compressor. If mechanical efficiency is 80%.

Given data:

$V_0 = V = 5 \text{ m}^3/\text{min}$

$P_1 = 1 \text{ bar}, P_2 = 1.013 \text{ bar}, P_3 = 2 \text{ bar}, P_4 = 3 \text{ bar}$

$P_0 = 1 \text{ bar}, n = 1.3, \gamma = 1.4, \gamma_0 = 1.4, \gamma_1 = 1.3, \gamma_2 = 1.4$

$n_1 = 1.3, h_{max} = 86 \%$

Soln:

Interim value pressure  $\left(\frac{P_2}{P_1}\right) = \left(\frac{P_4}{P_1}\right)^{1/3}$

$\left(\frac{P_2}{P_1}\right) = 5.31$

$\therefore \frac{P_2}{P_1} = \frac{P_3}{P_2} = \frac{P_4}{P_3} = 5.31$

Work of 1,  $V_0 = 5 \cdot 2 \text{ m}^3/\text{min} = \frac{52}{60} = 0.867 \text{ m}^3/\text{s}$

$\frac{P_0 V_0}{T_0} = \frac{P_1 V_1}{T_1}$

$\frac{103 \times 0.867}{293} = \frac{100 \times V_1}{303}$

$V_1 = 0.8923 \text{ m}^3/\text{s}$

$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \Rightarrow \frac{103 \times 0.867}{293} = \frac{531 \times V_2}{303}$

$\therefore V_2 = 0.0174 \text{ m}^3/\text{s}$

$\therefore V_3 = 0.0328 \text{ m}^3/\text{s}$

$W = \frac{n}{n-1} P_1 V_1 \left[ \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} \right] + \frac{n}{n-1} P_2 V_2 \left[ \left(\frac{P_3}{P_2}\right)^{\frac{n-1}{n}} \right] + \frac{n}{n-1} P_3 V_3 \left[ \left(\frac{P_4}{P_3}\right)^{\frac{n-1}{n}} \right]$



$$\dot{W} = \frac{1.35}{1.35-1} \times 103 \times 0.0923 \times \left[ (5.71)^{\frac{0.35}{1.35-1}} - 1 \right]$$

$$+ \frac{1.35}{1.35-1} \times 531 \times 0.0177 \times \left[ (5.71)^{\frac{0.35}{1.35-1}} - 1 \right]$$

$$+ \frac{1.35}{1.35-1} \times 2819.61 \times 0.00328 \times \left[ (5.71)^{\frac{0.35}{1.35-1}} - 1 \right]$$

$$\dot{W} = 57.91 \text{ kW}$$

Mechanical Efficiency,

$$\eta_m = \frac{BP}{IP}$$

$$0.8 = \frac{BP}{57.912}$$

$$\therefore BP = 46.33 \text{ kW}$$

unit - 2.

## Refrigeration & Air Conditioning

### 5.1 Refrigeration:

It is the science of producing and maintaining temperature below that of the surrounding atmosphere. This means the removing of heat from a substance to be cooled.

The equipment employed to maintain the system at a low temperature is termed a Refrigerating system.

Refrigeration is generally produced in one of the following three ways.

- i) By melting of a solid,
- ii) By sublimation of a solid,
- iii) By evaporation of a liquid.

### Major Components:

- Evaporator,
- Compressor,
- Condenser,
- Expansion Valve.

## 5.2. Refrigerants:

The Refrigerants is defined as any substance that absorbs heat through expansion (or) vapourisation and loses its through Condensation in a Refrigeration system.

### Classification:

- i) Primary Refrigerants.
- ii) Secondary Refrigerants

### Primary Refrigerants:

These are working mediums or heat Carriers which directly take Part in the refrigeration system and Cool the substance by the absorption of latent heat. Eg: Ammonia,  $\text{CO}_2$ ,  $\text{NH}_4$ , Sulphur dioxide.

### Properties:

- Completely non-toxic.
- Completely safe.
- low volumetric displacement.
- low weight of liquid Circulated Per tonne of refrigeration.
- They mostly have specific gravity (for liquid) of 1.38.
- works at low Pressure.
- High efficiency (Ammonia).

## Secondary Refrigeration:

These are first cooled with the Primary Refrigerants and then they are employed for cooling purposes.

### i) Halocarbon:

In this they contain one or more of three halogens, chlorine and bromine.

R-10 - Carbon tetrachloride.

R-11 - Trichloro-monofluoro methane.

### ii) Azeotropes:

They consist of mixture of different substances.

Ex: R-500, it contains 73.8% of R-12 & 26.2% of R-152.

### iii) Hydrocarbons:

They contain organic components. Several hydrocarbons are used successfully in commercial & industrial installation.

R-50 - Methane.

R-170 - Ethane.

R-290 - Propane.

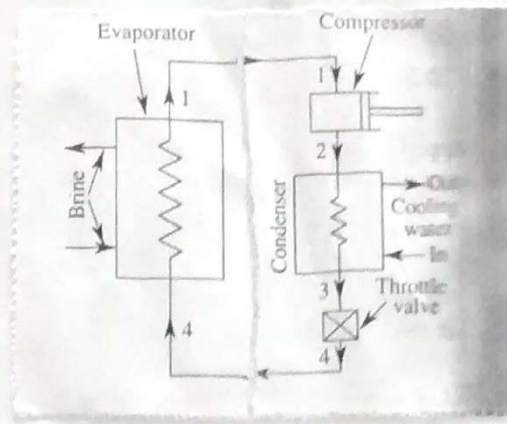
### iv) Inorganic Compounds:

R-717 - Ammonia ( $\text{NH}_3$ ).

R-718 - Water.

R-729 - Air.

## 5.3: Vapour Compression System:



### Compressor:

The function of a Compressor is to remove the Vapour from the evaporator, and to raise its temperature and Pressure to a Point.

### Condenser:

The function of a Condenser is to provide a heat transfer surface through which heat Passes from the heat refrigerent Vapour to the Condensing Medium.

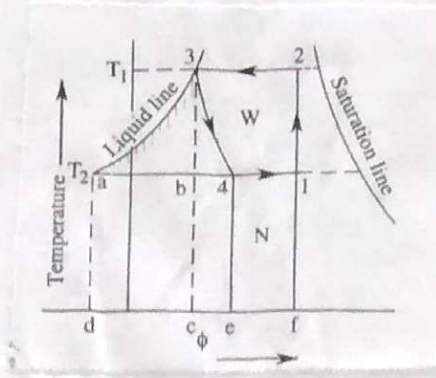
### Expansion Valve:

Its function is to meter the proper amount of refrigerant to the evaporator and to reduce the Pressure of liquid entering the evaporator.

### Evaporator:

An evaporator Provides a heat transfer through which heat can Pass from the refrigerated space into the Vapourizing refrigerant.

## Vapour Compression Cycle:



At Point 2 the Vapour which is at low temperature ( $T_2$ ) and low Pressure enters the Compressor's Cylinder and is Compressed adiabatically to 3 when its temperature increases to the temperature  $T_1$ . It is then Condensed in the Condenser (3-4). It then undergoes throttling expansion while Passing through the expansion Valve and its again Reduces to  $T_2$  by the line 4-1.

Dryness fraction represented by  $\frac{b_1}{b_2}$ .

Work done by Compressor =  $W = \text{Area } '2-3-4-b-2'$

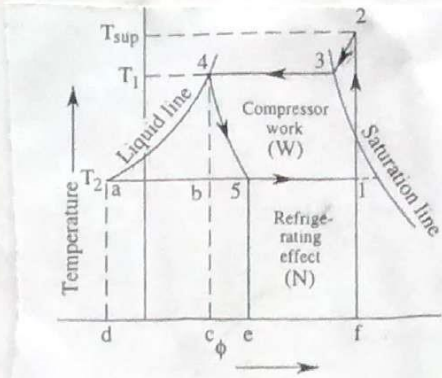
Heat absorbed =  $Q = \text{Area } '2-1-g-j-2'$ .

Cop:  $\frac{\text{Heat extracted (or) Refrigerating effect}}{\text{Workdone}}$ .

$$\begin{aligned} \text{COP} &= \frac{h_2 - h_1}{h_3 - h_2} \\ &= \frac{h_2 - h_4}{h_3 - h_2} \end{aligned}$$

$h_1 = h_4$  since during the throttling expansion 4-1 the total heat content

When super heated:



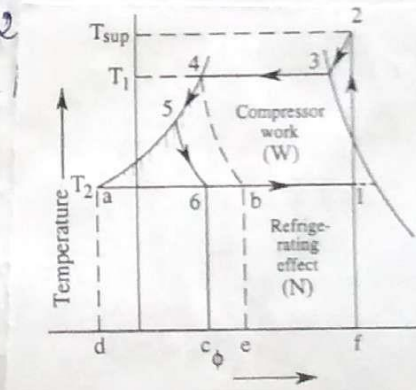
If the Compression of the vapour is continued after it become dry, the vapour will be super heated. The vapour enters the Compressor at '2' and is compressed to '3' where it is super heated to Temperature  $T_{sup}$ . Then it enters the Condenser. Firstly super heated vapour cools to  $T_1$  and Condenses at Const. temperature along the line 3'-4.

$$COP = \frac{\text{heat extracted}}{\text{Work done}}$$

$$\text{Work done} = h_3 - h_2$$

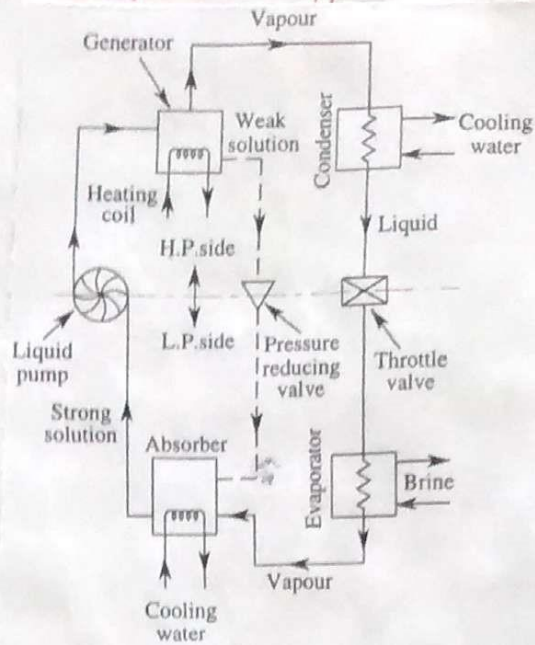
$$\text{Heat extracted} = h_2 - h_1$$

Effect of subcooling:



The Process of cooling the liquid refrigerant below the Condensing temperature for a given Pressure. It increases the COP provided that no further energy has to be spent to obtain the extra Cold Coolant required.

## 54 Vapour Absorption System:



The solubility of **Ammonia (or) lithium bromide (or) water**. Can be used as Refrigerants [only refrigerants differs but not the Working Conditions & Process].

The Ammonia Vapour leaving the evaporator at point 2 is readily absorbed in the low temperature hot solution in the absorber. The process is accompanied by the rejection of heat. The ammonia is pumped to the higher pressure and is heated.

In this work done on Compressor is less than Vapour Compression Cycle.

$$\text{COP} = \frac{\text{Heat extracted from the Evaporator}}{\text{Heat Supplied in the generator} + \text{Work done by the liquid Pump.}}$$



# Prob on Vapour Compression, Superheat & Subcooled

Prob: 5.1

Pg: 813 (Rajput).

Given:

$m = 6 \text{ kg/min}$ ;  $\phi_{\text{relative}} = 50\%$ ;  $x_2 = 0.6$ ;  $p_w = 1.187 \text{ kJ/kg}$

Latent heat of ice =  $335 \text{ kJ/kg}$ .

Soln:

$$h_{f2} = 314 \text{ kJ/kg}; h_{fg2} = 1540 \text{ kJ/kg}.$$

$$h_{f3} = 59.7 \text{ kJ/kg}; h_{fg3} = 138 \text{ kJ/kg}; h_{f4} = 59.7 \text{ kJ/kg}.$$

$$h_2 = h_{f2} + x \cdot h_{fg2}.$$

$$= 314 + 0.6 \times 1540$$

$$h_2 = 1238 \text{ kJ/kg}.$$

$$s_3 = s_2 \text{ (Isentropic)}$$

$$s_{f3} + x_3 \frac{h_{fg3}}{T_3} = s_{f2} + x_2 \frac{h_{fg2}}{T_2}.$$

$$0.2232 + x_3 \times \frac{138}{298} = 0.1251 + 0.6 \times \frac{154}{268}$$

$$= 0.4698.$$

$$x_3 = 0.5325.$$

$$h_3 = h_{f3} + x \cdot h_{fg3}$$

$$= 59.7 + 0.5325 \times 138.$$

$$= 133.2 \text{ kJ/kg}.$$

Also,  $h_1 = h_{f4} = 59.7 \text{ kJ/kg}$ .

$$\text{COP} = \frac{h_2 - h_1}{h_3 - h_2} = \frac{1238 - 59.7}{133.2 - 59.7} = 6.82.$$

Actual Cop =  $\eta_{rel} \times \text{COP}_{\text{theoretical}}$

$$= 0.5 \times 6.82$$

$$= 3.41$$

Heat extracted from 1 kg of water at 20°C for the formation of 1 kg of ice at 0°C.

$$= 1 \times 4.187 \times (20) + 335$$

$$= 418.7 \text{ kJ/kg.}$$

$$\text{COP}_{\text{actual}} = 3.41 = \frac{R_{\text{actual}}}{W}$$

$$= \frac{m_{\text{ice}} \times 418.74}{m(h_3 - h_2)}$$

$$m_{\text{ice}} = \frac{6(133.2 - 123.8) \times 3.41}{418.74}$$

$$= 0.459 \text{ kg/min.}$$

$$= \frac{0.459 \times 60 \times 24}{1000}$$

$$= 0.661 \text{ tonne.}$$

Prob: 5.2.  
Pg: 815. → (R. Put)

Soln:

Given:

5 tonne plant.

(h<sub>1</sub>) Compressor  $h_1 = 183.19 \text{ kJ/kg}$ .

(h<sub>4</sub>) Condenser =  $74.59 \text{ kJ/kg}$ .

h<sub>3</sub> =  $209.41 \text{ kJ/kg}$ .

Soln:

Total refrigeration effect Produced = 5 TR.

=  $5 \times 14,000 = 70,000 \text{ kJ/h}$

i) The refrigerant flow rate  $\dot{m}$ :

$$\begin{aligned} \text{Net refrigerant effect} &= h_2 - h_1 \\ &= 183.19 - 74.59 \\ &= 108.6 \text{ kJ/kg.} \end{aligned}$$

Refrigerant flow rate,

$$\dot{m} = \frac{19.44}{108.6} = 0.179 \text{ kg/s.}$$

ii) The COP:

$$\begin{aligned} \text{COP} &= \frac{h_2 - h_1}{h_3 - h_2} = \frac{183.19 - 74.59}{209.41 - 183.19} \\ &= 4.142. \end{aligned}$$

iii) The Power required to drive the Compressor.

$$\begin{aligned} P &= \dot{m} (h_3 - h_2) \\ &= 0.179 (209.41 - 183.19) \\ &= 4.69 \text{ kW.} \end{aligned}$$

iv) The rate of heat rejection to the Condenser.

$$\begin{aligned} &= \dot{m} (h_3 - h_4) \\ &= 0.179 (209.41 - 74.59) \\ &= 24.13 \text{ kW.} \end{aligned}$$

5.3 Prob:

Pg: 823.

Given:

$$h_2 = 615 \text{ kJ/kg.}$$

$$h_3 = 664 \text{ kJ/kg.}$$

$$h_4 = h_1 = 446 \text{ kJ/kg.}$$

$$v_2 = 0.14 \text{ m}^3/\text{kg.}$$

Soln:

i) Refrigerating effect Per kg.

$$= h_2 - h_1 = 615 - 446 = 169 \text{ kJ/kg.}$$

ii) Mass of refrigerant to be Circulated Per min,

$$m = \frac{20 \times 14000}{169 \times 60} = 27.6 \text{ kg/min.}$$

iii) Theoretical Piston displacement,

$$= \text{specific Volume at suction} \times \text{Mass of refrigerant used/min}$$

$$= 0.14 \times 27.6 = 3.864 \text{ m}^3/\text{min.}$$

iv) Theoretical Power:

$$m \times (h_3 - h_2) = \frac{27.6}{60} (664 - 615)$$

$$= 22.54 \text{ kJ/s.}$$

$$v). \text{ Cop} = \frac{h_2 - h_1}{h_3 - h_2} = \frac{615 - 446}{664 - 615} = 3.45.$$

vii) heat removed through the Condenser.

$$= m(h_3 - h_4)$$

$$= 27.6(664 - 446)$$

$$= 6016.8 \text{ kJ/min,}$$

## 5.5 Air Conditioning:

It is the simultaneous control of temperature, humidity, motion and purity of atmosphere in confined space.

Components:

- Fans
- Filters
- ducts
- Heating Chamber (or) Cooling unit.

### operation:

The Fan forces air into duct work which is connected to the opening in the room.

The duct work directs the air to the room.

Air is cleaned through the filters. it is either heated (or) cooled depends upon the condition in room. If cool air is required, the air is passed over the surface of a cooling coil.

finally the air flows back to the fan and the cycle is completed.

Types & Working:

Central System:

In this system the equipments such as fans, coil are assembled in the field. A central system serves different rooms, requires individual control of each room. The condensed air is carried to various rooms through ducts and return back to the control plants through return duct.

oned System:

In Zoned Systems. the building is divided into Zones such that as nearly possible conditions may be expected. Variation in requirements of this kind are the most common case with which air-conditioning has to deal. The return air from the room passes through grills into the corridor which acts as the returning air collecting duct. The cooling (or) heating booster coils could be served from circulating water mains.

### unitary System:

x They are assembled and fitted near to the zone. unitary is preferred for 15 tonnes capacity (or above  $2000\text{ m}^3/\text{min}$ )  
Components are Attic; Remote units; self contained units;  
Room air conditioners; unit air coolers.

## 5.6 Cooling Load Calculation:

The Cooling load is influenced by:

1. Location of the place geographically i.e. the latitude, elevation above mean sea level and the normal
2. Orientation, whether it is north (or) South (or) East (or) West facing.
3. The building construction features, regarding walls, window etc.
4. The load to the system contributed by the number of people, appliances, lightning etc.

The heat gain is divided into

- i) Sensible heat
- ii) Latent heat.

### Sensible heat gain:

It is the direct addition of heat in a given space. It may be due to conduction through walls, convection & radiation.

### Latent heat gain:

It is due to the addition of moisture content in the space. If the humidity ratio is to be maintained (change of phase).



## Room Sensible Heat factor:

Sensible heat factor is the ratio of sensible to total heat. The total heat is made up of the sensible heat and latent heat.

The room sensible heat factor is the ratio of room sensible to room total heat. The supply air must be able to remove both the room sensible heat & room latent heat.

$$\text{Room Sensible heat factor} = \frac{RSH}{RTH} = \frac{RSH}{RSH + RLH}$$

$$\text{RSHF} = \frac{\text{Room Sensible heat}}{\text{Room Total heat}}$$
$$\text{RSHF} = \frac{\text{Room Sensible Heat}}{\text{Room Sensible heat} + \text{Room latent Heat.}}$$

## Grand Sensible Heat factor:

It is defined as the ratio of total sensible heat to the grand total heat load.

$$\text{GSHF} = \frac{TSH}{GTH} = \frac{TSH}{GSH + GLH}$$

$$= \frac{\text{Total Sensible Heat}}{\text{Total sensible Heat} + \text{Total latent heat.}}$$

## Effective Sensible Heat

It is the ratio of effective room sensible heat to the sum of effective room sensible heat and latent heat.

$$ESHF = \frac{ERSH}{ERSH + ERLH} = \frac{ERSH}{ERTH}$$

$$= \frac{RSH + BFX(OSH)}{[RSH + (BFX(OSH)) + RLH(BFX(OLH))]}$$

OSH  $\rightarrow$  outside sensible heat

OLH  $\rightarrow$  outside latent heat

Prob: 5.7

Pg: 8.52

(Ramoorthy).

Given:

Outdoor air

30° DB and 75% RH

No of people 50

Air/Person/min = 0.4 m<sup>3</sup>.

Room Air

20° DBT and 60% RH

Process:

Sensible Cooling.

Dehumidification

Heating.

T<sub>c</sub> = 25° C.

Soln:

(i) Estimate mass of air / s.

$$\text{Volume of air} = \frac{4 \times 50}{60} = 0.33 \text{ m}^3/\text{s}$$

$$\text{(ii) Cooling Coil Capacity} = \text{Mass of air} \times \text{Drop in enthalpy.}$$

$$= 0.3766 (81.5 - 34) \text{ kJ/s.}$$

$$= 17.88 \text{ kJ/s.}$$

$$= 1073 \text{ kJ/m.}$$

$$= \frac{1073}{211} \text{ Tons of Ref} = 5.09.$$

5.09 Tonnes of Refrigeration.

$$\text{(iii) Capacity of heating coil} = m C_p (T_R - T_{dp}).$$

$$= 0.3766 \times 1.005 [20 - 12]$$

$$= 3.03 \text{ kW.}$$

$$\text{(iv) Water removed / Hr} = (W_1 - W_2) \times 0.3766 \times 3600$$

$$= (20 - 8.75) \times 0.3766 \times \frac{3600}{1000}$$

$$= 15.25 \text{ kg/Hr.}$$

Ans:

$$\text{Cooling Coil Capacity} = 4.23 \text{ Tons of Ref.}$$

$$\text{Heating Coil " } = 3.03 \text{ kW.}$$

$$\text{Water removal/hr} = 15.25 \text{ kg/hr.}$$

Ans