

ALTERNATOR

(1)

Working Principle

→ Electro magnetic induction.

When ~~the~~ flux linking a conductor changes, an emf is induced in the conductor.

→ Same as DC generator

Armature - rotate

Field - Stationary

* But in Alternator

Armature - Stationary

Field - rotating

→ The direction of induced emf can be found by Fleming's Right Hand rule

* Why Armature coil is stationary & field is rotating?

- (i) The ϕ can be directly taken from armature without brush-contact.
- (ii) Easy to insulate ^{for} high voltage upto 30 kV or more.
- (iii) The field winding has low voltage DC supply which can easily be insulated.
- (iv) The armature can easily be cooled by proper ventilation.

① Armature (Stator)

① Frame

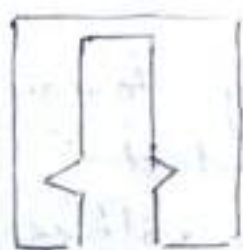
→ Not for ^{carrying} magnetic flux but to hold the armature stamping & winding in position.

→ Ventilation is maintained with the help of hole cast in the frame.

② Stator Core

→ Supported by stator frame & is build made up of laminations of magnetic iron/steel alloy.

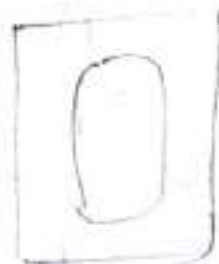
→ To avoid eddy current loss & heating.



Wide Open



Semi closed

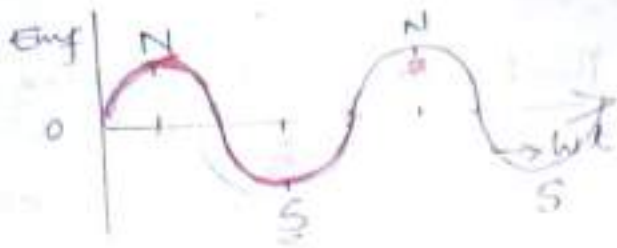


Closed

→ easy to winding
→ But due to air gap flux distribute any generated has ripples.

→ Hard to put coil in it
→ don't distribute stator gap flux
→ any ~~is~~ no harmonics

I * Speed & frequency



One cycle of emf generated on a coil when one pole pair passes over the coil.

$P \rightarrow$ no. of poles in field -

$N \rightarrow$ Speed of rotor (rpm)

$f \rightarrow$ frequency of generated emf

frequency of generated emf in one revolution = $\frac{P}{2}$

frequency of emf per minutes = $\frac{PN}{2}$

frequency of emf = $\frac{PN}{2 \times 60}$

$\frac{1 \text{ min}}{60} \rightarrow \text{sec}$

$$f = \frac{PN}{120}$$

* Synchronous Speed

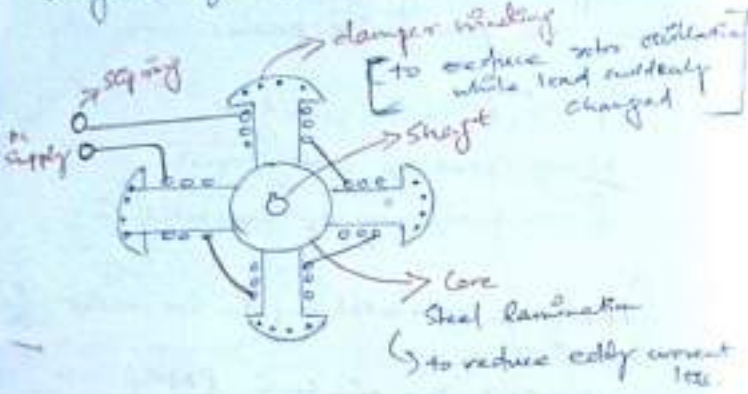
$$N_s = \frac{120f}{P}$$

To have 50Hz frequency.

<u>P</u>	<u>2</u>	<u>4</u>	<u>6</u>	<u>10</u>
<u>N_s</u>	<u>3000</u>	<u>1500</u>	<u>750</u>	<u>600</u>

① Salient Pole

Salient \rightarrow Protuding / Projecting
The pole is projected out from the surface of rotor core.

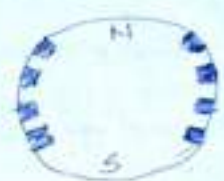


\rightarrow The air gap is not uniform.
Poles are such designed; that the flux distribution is \sim sinusoidal as a result; generated emf is sinusoidal.



- \rightarrow ① Due to windage loss; it operated slowly
- ② Large nos of poles poles on the rotor
 - ③ Large diameter & short axial length
 - ④ Hydel power plant.

Non-Salient Pole



\rightarrow 2/3rd of rotor periphery slots are cut at regular interval.
 \rightarrow Unslotted portion form pole faces

- \rightarrow High grade Ni-Chrome-Mo Steel.
- \rightarrow less centrifugal force.
- \rightarrow high speed of operation.
- \rightarrow less windage loss - less noisy because of uniform air gap.

Driven by
 \rightarrow Steam or Gas turbine
 \rightarrow turbo-alternator.

* Excitation System for Alternator

- Small M/C \rightarrow Pilot excitor (dc generator or permanent magnet)
- Medium M/C \rightarrow AC excitor (or AC gen) - if it is AC it is rectified by applied thyristor slip ring brushes
- Large M/C \rightarrow Slip ring need to avoided
High speed sliding contact
 \rightarrow Brushless DC excitation

* EMF eqn of an alternator $E = \frac{d\phi}{dt}$ (Faraday's Law)

$E_{av}/\text{conductor} = \frac{\phi_{cut \text{ per rev}} (Wb) \times \text{slits}}{\text{time taken for one rev}} (Sec)$

$E_{av}/\text{conductor} = \frac{P\phi \frac{r\omega}{60}}{60/N}$
 $\phi \rightarrow$ flux per pole
 $P \rightarrow$ no. of poles
 $N \rightarrow$ rev. per min
 $f \rightarrow$ Hz

But; $f = \frac{N}{120}$
 $\rightarrow 2f = \frac{N}{60}$
 (replace)

$E_{av}/\text{conductor} = 2f \phi$

$E_{av}/\text{phase} = 2f \phi Z_p$
 $Z_p \rightarrow$ conductors per phase

$E_{av}/\text{phase} = 4f \phi T_p$
 $T_p \rightarrow$ Turns of coil/phase
 $(Z_p = 2T_p)$

form factor = $\frac{E_{rms}}{E_{avg}} = 1.11$ (for sine wave)
 $\Rightarrow E_{rms} = 1.11 \cdot E_{avg}$

$E_{rms}/\text{phase} = 1.11 \times 4f \phi T_p$

$E_{rms}/\text{phase} = 4.44 f \phi T_p$

- $\phi \rightarrow$ flux per pole (Wb)
- $f \rightarrow$ frequency
- $T_p \rightarrow$ Turns of coil per phase

Eqn \rightarrow Variable frequency drive Eq. 114

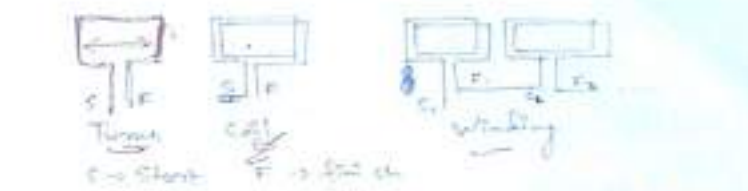
* Armature Winding

The winding above voltage is induced.

Turn - consist of two conductors

coil - several turns in series

Winding - several coil in series



$\phi_{pole} = \frac{P}{2} \phi_{magnet}$
 $\phi_{pole} \rightarrow$ electrical degree
 $\phi_{magnet} \rightarrow$ mechanical degree
 1.8 x no. of poles

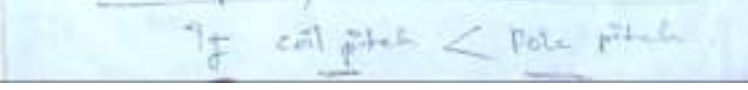
Pole pitch ($\Rightarrow 60-120^\circ$)
 Angular distance bet. two adjacent poles



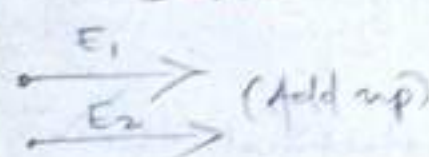
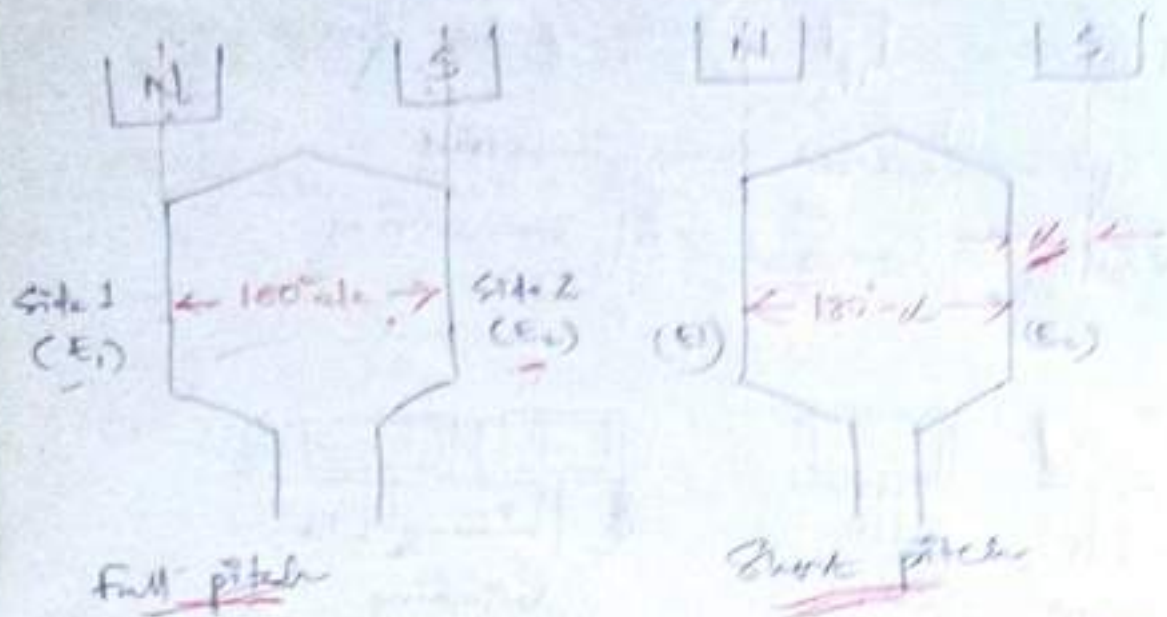
Coil pitch
 The distance bet. the two side of coil is coil-pitch

Full pitch
 Pole pitch = Coil pitch

Short-pitch / Fractional-pitch coil
 $\frac{2}{3}$ coil pitch < Pole pitch



- Pitch factor k_p (also known as span factor) (k_p)



$$E_c = E_1 + E_2 = 2E$$

(Arithmetic Sum)



$$E_c = E_1 + E_2 = 2E \cos(d/2)$$

(Phasor Sum)

$$k_p = \frac{\text{Voltage generated in short pitch}}{\text{Voltage in full pitch}}$$

$$k_p = \cos(d/2)$$

- Saving conductor as winding ends are short
 - Harmonics are eliminated from the generated emf; waveform is improved.
- Advantages of Distributed winding

- 1) Reduce Harmonics in generated emf; improved waveform.
- 2) Diminishes armature reaction.
- 3) Even distribution of conductors helps for better cooling.
- 4) Stator core is fully utilized, as conductors are evenly distributed over the armature periphery.

• Distribution factor / Breadth factor (K_d)

Concentrated winding:

The sides of coil of given phase are concentrated in a single slot under a pole.
 \rightarrow Ind voltage induced were in phase with each other

$$E_c = T * E \rightarrow \text{induced emf per turn} \\ \downarrow \\ \text{No. of turns}$$

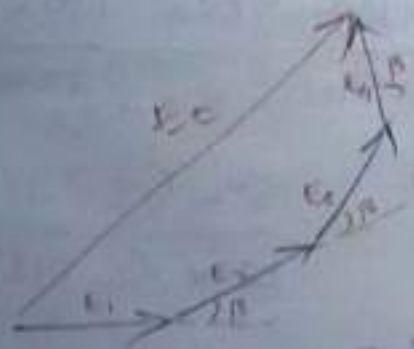


But; Coils are not concentrated in single slot but distributed in number of slots under — form — POLE GROUP.
 \rightarrow Voltage induced is not in phase but differ by an angle " β " (Angle between slots).

$$M = \frac{\text{Slot}}{\text{Pole} \times \text{Phase}} \quad (\text{Slots per pole per phase})$$

$\beta =$ angle — slight both adjacent slots.
 (electrical degree)

$$\beta = \frac{180^\circ}{\text{slot/pole}} = \frac{180^\circ * \text{pole}}{\text{Slots}}$$



$$K_d = \frac{\text{Phasor sum of } E_c}{\text{Arithmetic sum of } e_c} = \frac{\sin(m\beta/2)}{m \sin(\beta/2)}$$

\rightarrow distributed voltage
 Concentrated voltage

Actual voltage Generated

$$E_1 = 4.44 \phi_{\text{pole}} f T_{\text{phase}} K_c K_d$$

$$K_w = K_c K_d$$

↳ "winding factor"

$$E_L = \sqrt{3} E_p \quad (\text{Y-connection})$$

↳ line ↳ phase

Q. A 3 ϕ , 50Hz, 8 pole Δ Alt (Y-connection) with 120 slots & 8 conductors/slots
 $\phi = 0.05$ Wb sinusoidally distributed

Determine Phase A line voltage.

Ans \Rightarrow Assuming full pitch ; $\alpha = 0^\circ$
 $K_c = \cos \alpha = 1$

$m =$ Slots per pole per phase

$$\Rightarrow m = \frac{120}{8 \times 3} = 5$$

$$\beta = \frac{\text{Slots} \times 180^\circ \times \text{pole}}{\text{Slots} \times 2} = \frac{120 \times 8 \times 180^\circ}{2 \times 120} = 12^\circ$$

$$K_d = \frac{\sin(m\beta/2)}{m \sin(\beta/2)} = \frac{\sin(30^\circ)}{5 \times \sin(12^\circ)} = 0.95$$

$$E_1 = 4.44 \phi_{\text{pole}} f T_{\text{phase}} \cdot K_d \cdot K_c = 1699 \text{ V}$$

$E_L = \sqrt{3} E_p = 2992.5 \text{ V}$

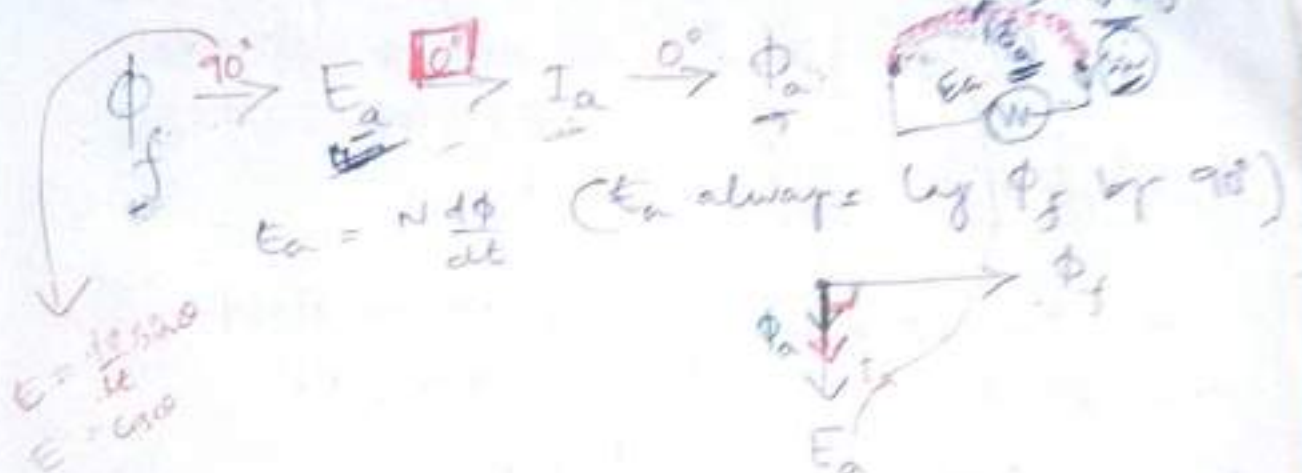
$$T_{\text{phase}} = \frac{48 \times 120}{2 \times 3} = 160$$

* Armature Reaction

The effect of armature flux on the rotor field flux is called AR.

AR effect changes with load type.

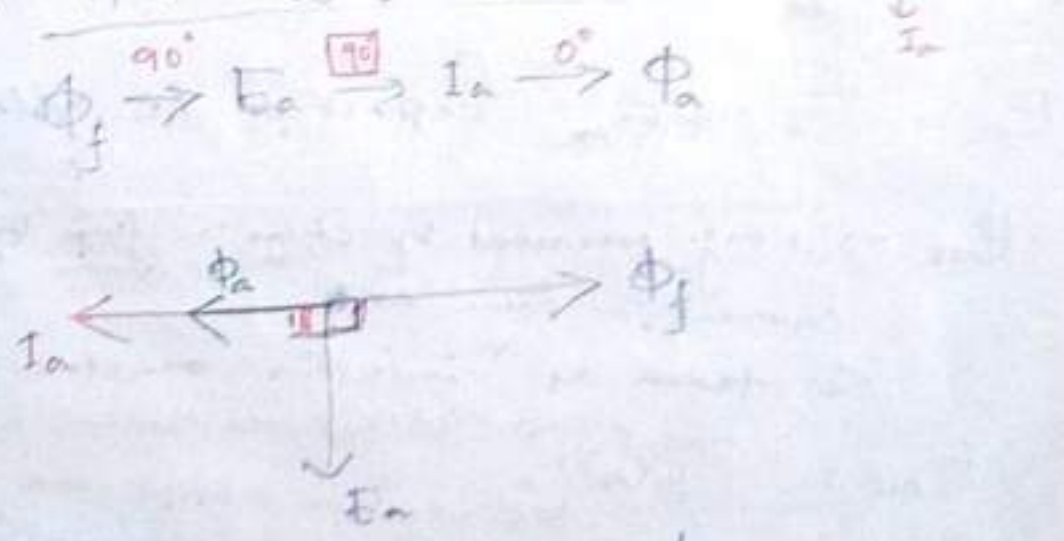
(I) AR: unity Pf $\rightarrow I_a \rightarrow E_a$



→ Cross-magnetizing effect.

- ϕ_a lags Φ_f by 90° w.r.t Φ_f
- Distort the main field flux.

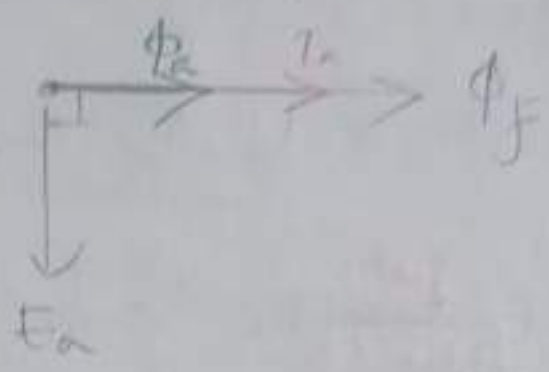
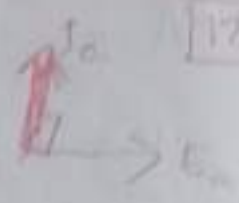
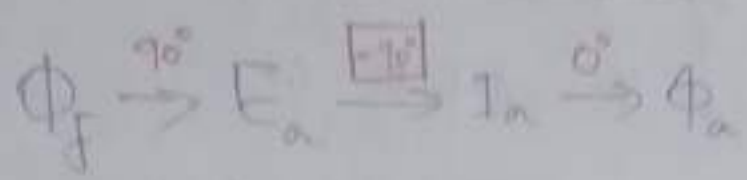
(II) AR: lagging Pf ZERO



→ Demagnetizing effect.

- Opposes & weakens the main field flux.
- Emf generated will be decreased ($E \propto \Phi$)

III AR's unity leading PF.



→ Magnetizing effect.

→ It strengthens the main field flux
 → Emf generated will increase ($E \propto \Phi$)

* Synchronous Impedance

Mag flux → Emf generated

$\Phi_f \rightarrow E_{ex}$

$\Phi_{AR} \rightarrow E_{AR}$

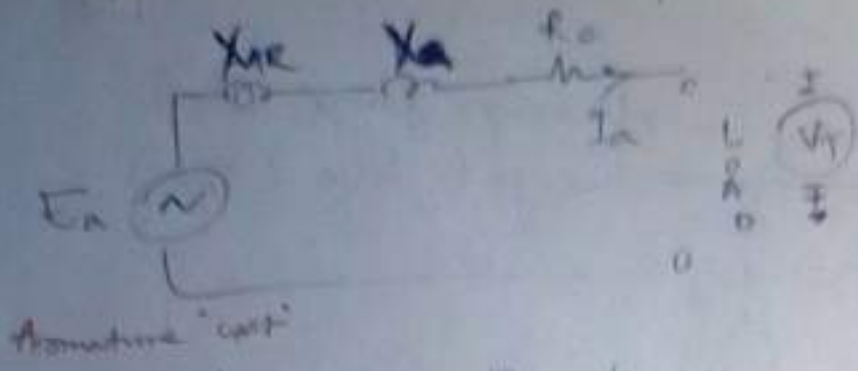
$E_a = E_{ex} + E_{AR}$ (effect of AR added)

E_{AR} → emf generated by change in flux by a current in same coil.

So, taken as "inductive reactance".

$E_{AR} = -j(X_{AR})I_a$
Fieldless reactance
→ negative current cause AR

Auto $\frac{E_a}{I_a} = V_t = (E_a - I_a R_a) \sin \delta + j(X_d I_a - R_a I_a)$



Leakage Reactance

The flux set up by I_a which does not contribute to the useful flux of the m/c is Leakage flux.

This leakage flux induces a self-induced emf in armature windings.

- ① Slot leakage
- ② Tooth head leakage
- ③ Call-end leakage

Now;

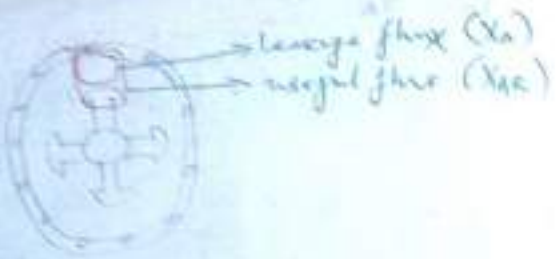
$$V_t = E_a - j(X_{AR} + X_a)I_a - I_a R_a$$

$$= E_a - Z_s I_a$$

$Z_s = R_a + jX_s$
 ↳ Synchronous Impedance

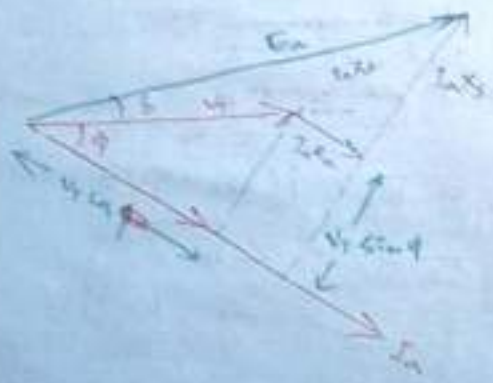
$X_s \rightarrow X_a + X_{AR}$ ↳ Armature Reaction
 ↳ leakage reactance

$Z_s \rightarrow jX_s + R_a$, Armature resistance
 ↳ field reactance



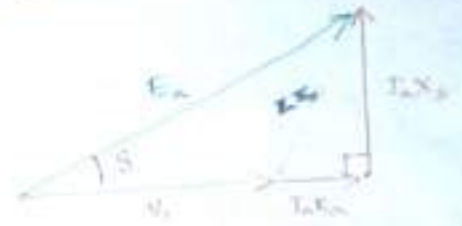
* Equivalent phasor diagram

(I) Lagging PF load.



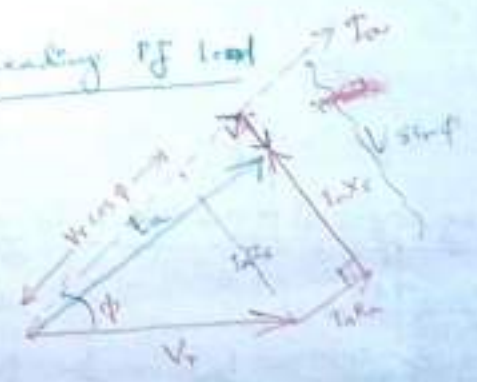
$$E_a = \sqrt{(V_t \cos \phi + I_a X_s)^2 + (V_t \sin \phi + I_a X_s)^2}$$

(II) Unity PF load



$$E_a = \sqrt{(V_t + I_a X_s)^2 + (I_a X_s)^2}$$

(III) Leading PF load



$$E_a = \sqrt{(V_t \cos \phi + I_a X_s)^2 + (V_t \sin \phi - I_a X_s)^2}$$

$\delta \rightarrow$ power angle ($E_a - V_t$)
 Torque angle
 It varies with the load.

$$\vec{E}_a = \vec{V}_t + j I_a X_s \angle \phi$$

* Voltage Regulation (meas after DC test) | 16

The rise/change in voltage at terminal when load is reduced from full load to no-load, keeping field current & speed constant.

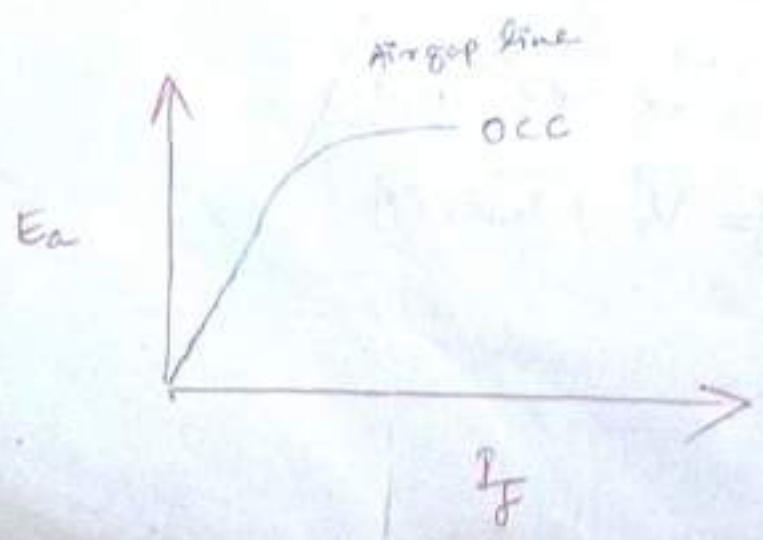
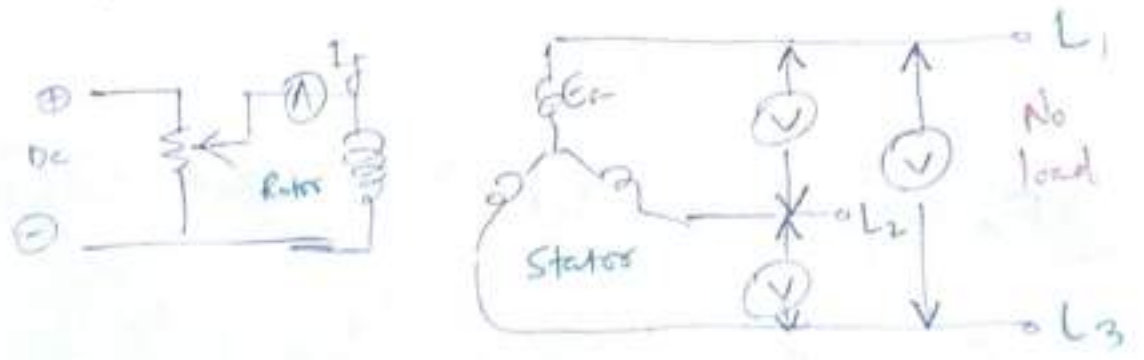
$$VR = \frac{E_a - V_r}{V_r}$$

V_r → rated full load voltage
 E_a → no load voltage (generated voltage).

⇒ VR depends upon the "load".

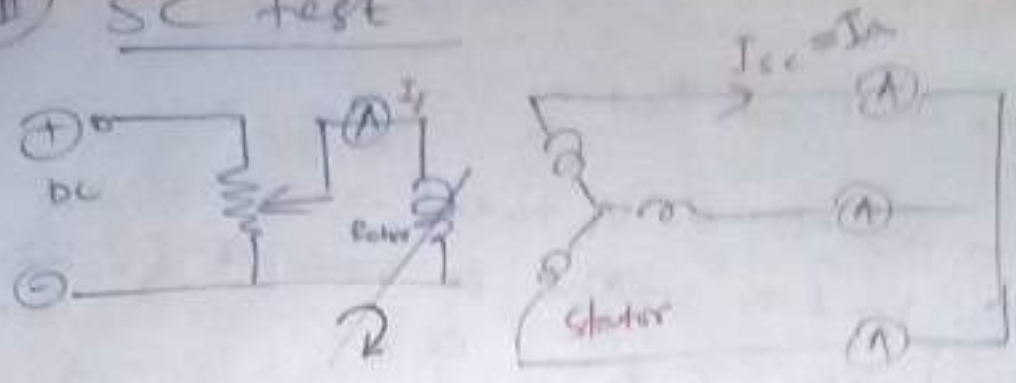
* Testing of Alternator (To measure Z_s)

(I) OC test



field current (I_f) is increased from 0 to 125% gradually

II SC test



Motor I_c run at N_s

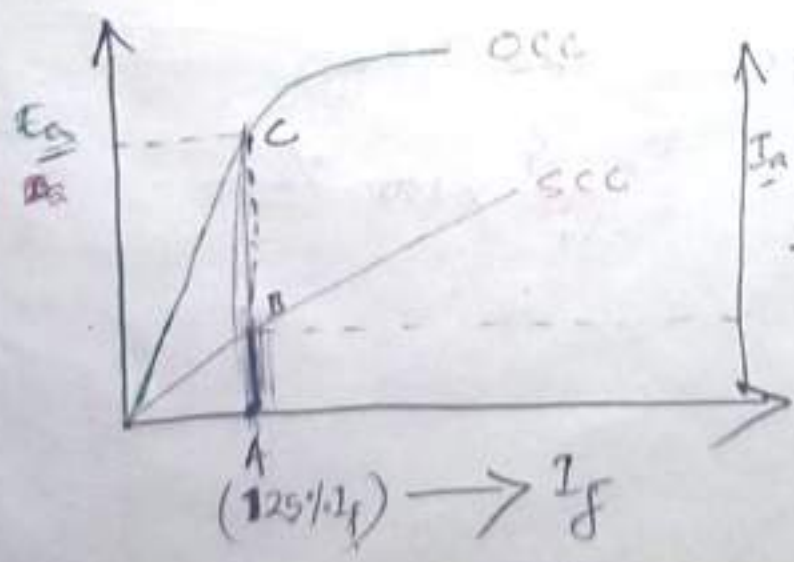
I_f is gradually increased from 0 to 125%



$$Z_s = \frac{\text{OC voltage } (E_a)}{\text{SC Current } (I_a)}$$

$I_f = \text{constant Same } (125\%)$

$$X_s = \sqrt{Z_s^2 - R_a^2}$$



$$Z_s = \frac{AC}{AB}$$

* Voltage Regulation

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(A) Direct Load Test

(i) Run @ N_s & V_T rated

(ii) The load is varied ~~to~~ until I_a is at rated value @ given f .

(iii) Then load is removed & N_c, I_f are same. We measure E_a .

$$(iv) \quad VR = \frac{E_a - V_T}{V_T} \times 100 \%$$

(v) This method is applicable for small power rating alternator (5 KVA)

(B) Synchronous Impedance method (EMF method)

(i) replacing $A.R.$ ^{armature reactance} by fictitious reactance

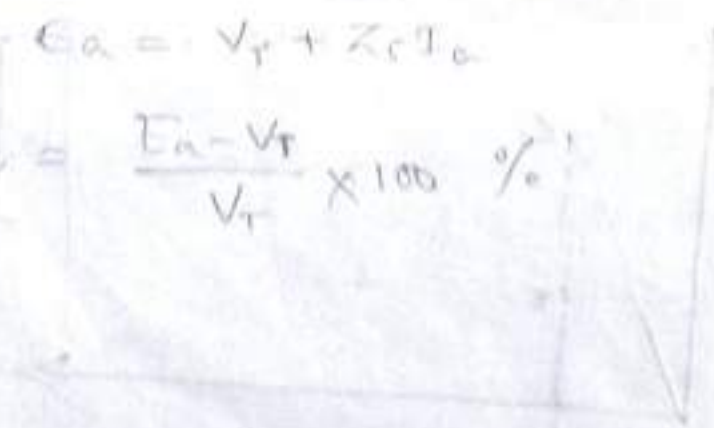
$$V = E_a - Z_s I_a$$

(ii) Z_s is measured from O.C. & S.C. test

(iii) Then E_a is calculated

$$E_a = V_T + Z_s I_a$$

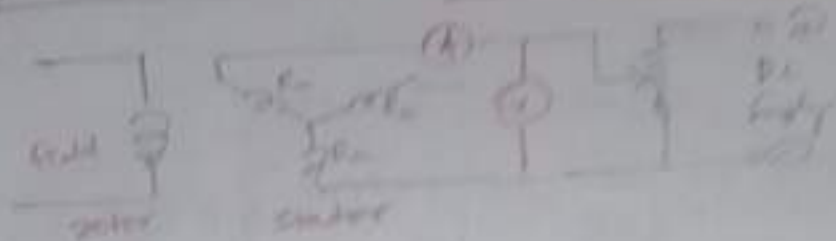
$$(iv) \quad VR = \frac{E_a - V_T}{V_T} \times 100 \%$$



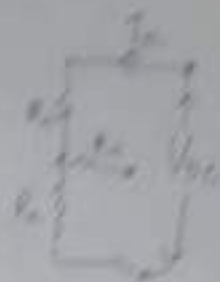
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DC test (BA EM AC SSC Test of Alternator)

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$$\frac{V}{I} = 2R_a \Rightarrow R_a = \frac{V}{2I}$$



Then;

$$X_s = \sqrt{Z_s^2 - R_a^2}$$

$$(Z_s = R_a + jX_s)$$

- Q) A 550V, 55kVA, 1 ϕ Alternator has its resistance $(R_a) = 0.2 \Omega$. $I_f = 10A$ produces $E_a = 200V$ on SC test & $E_a = 450V$ on OC test. Calculate X_s & Voltage regulation @ full load $\cos \phi = 0.8$ lagging.

$$X_s = \sqrt{Z_s^2 - R_a^2}$$

$$Z_s = \frac{E_a}{I_a} = \frac{450}{200} = 2.25 \Omega$$

$$X_s = \sqrt{2.25^2 - 0.2^2} \approx 2.24 \Omega$$

$$X_s = \sqrt{2.25^2 - 0.2^2} = 2.24 \Omega$$

$$VR = \frac{E_a - V}{V} \times 100$$

$$V = 550V$$

$$E_a = V + I_a Z_s$$

1205

* 11th operation of alternator (After 10th number) 21

- (i) Multiple alternator can supply a bigger load than a single alternator.
- (ii) During light load; one or more alternator may be shut down.
- (iii) Suitable for ~~or~~ scheduled maintenance; while other m/c maintain continuity of supply.
- (iv) If there is breakdown of a generator; there is no interruption of power supply.
- (v) In order to meet ^{inc} future demand of load; more m/c can be added without disturbing the original set up.
- (vi) The cost of generation is reduced when a ~~new~~ ^{new} ~~unit~~ ^{unit} is in 11th.

* Condition for 11th operation

Loaded m/c → running m/c

newly connected m/c → incoming m/c

- (i) The phase sequence of the busbar voltage & i/c m/c must be same.
- (ii) The voltage must be same.
- (iii) No phase difference both busbar & i/c m/c voltage.
- (iv) frequency of generated voltage must be same.

* Synchronization

The process of one machine in sync with other machine / infinite busbar is known as synchronization.

✓ The process of matching the ^{phase} & frequency of a generator to an infinite bus / synchronous motor. _{V_T must be same phase angle.}

* Infinite Bus



A system of constant voltage and constant frequency.

Connect to the generator.

has no effect on the busbar voltage.

(1) V_T is constant & bus V_c etc's

(2) δ remains constant; bus rotated

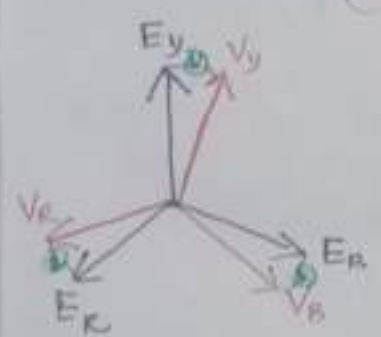
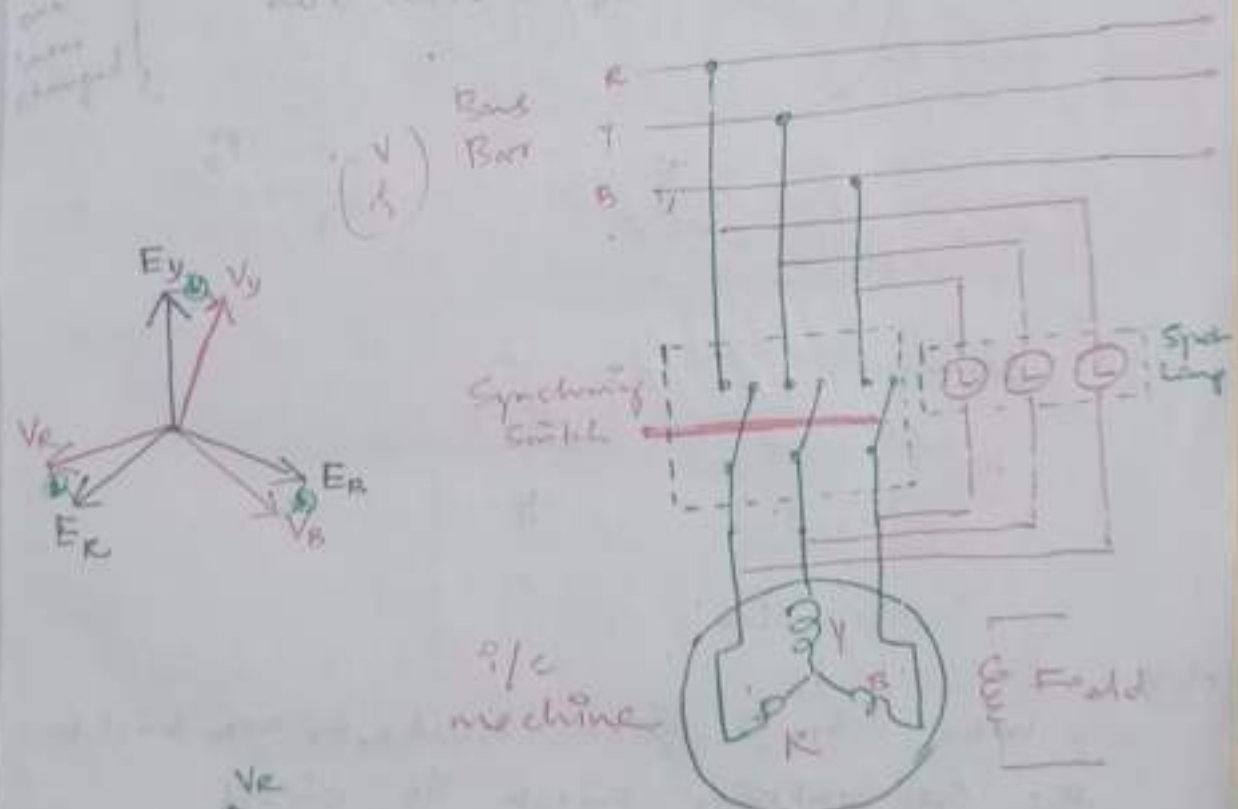
(3) X_c is very small ≈ 0 or ∞



Q1) Synchronizing Lamp (3 dark lamp method) 23

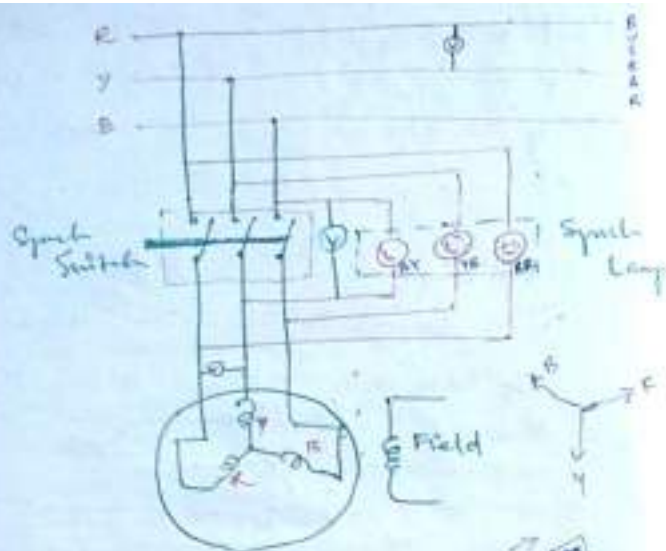
- (i) Lamp never to started if $V_L \neq V_R$ lamp
- up when voltage equal
- (ii) If it adjusted such that $V_L = V_R$ equal
- to bus bar voltage.

if $V_L \neq V_R$ or phase sequence are wrong
 (iii) 3 lamps if phase sequence are equal & $V_L = V_R$
 if $V_L \neq V_R$ we to different then bus bar
 If all lamp will not bright & dark
 the lamp type phase sequence are
 not correct.



- Disadvantage
- Sync switch will be closed only when the lamp is dark.
 - ∴ A large inductance around lamp will
 - Lamp should not be used

If two phases are interchanged



Adv → When L_1 is dark & L_2, L_3 are bright the synchronizing switch is closed. No circulating current flow.

Dis → f of 1/c % is still not known.

→ The posⁿ of pointer indicates that the ϕ "phase diff" betⁿ Busbar & incoming alternator.

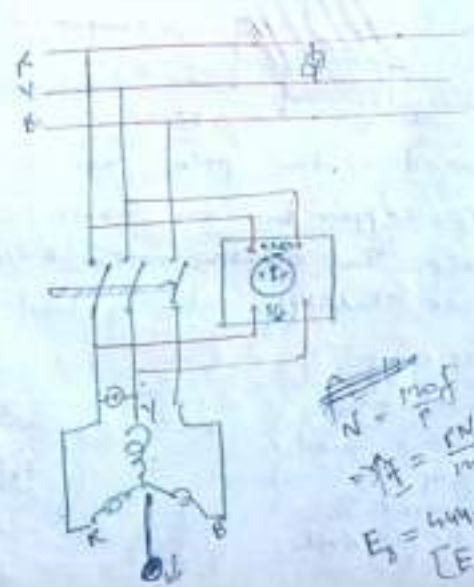
→ $f \rightarrow$ Same \rightarrow Pointer const^t

$f \rightarrow$ low \rightarrow pointer rotate in one direction

$f \rightarrow$ fast \rightarrow rotate in other direction

Speed of rotation \propto (Phase diff betⁿ Bus & 1/c %)

→ It gives no info about phase sequence to change f → Speed of prime mover is adjusted $N \propto \left[\frac{E_b}{f} \right]$



$$N = \frac{120f}{P}$$

$$\Rightarrow f = \frac{PN}{120}$$

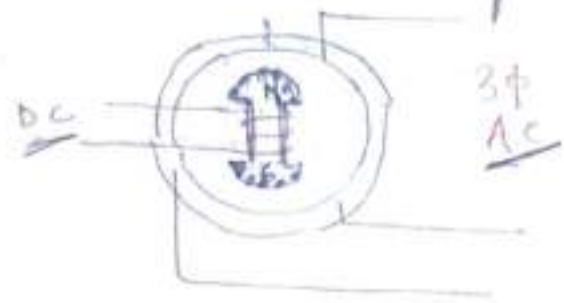
$$E_b = 4.44 f \phi_m K_w T_n$$

$$[E_b \propto f]$$

THREE PHASE SYNCHRONOUS MOTORS



It is a M/C that convert AC electric power to Mech power at a constant speed called Synchronous motor.

It is "doubly excited machine".

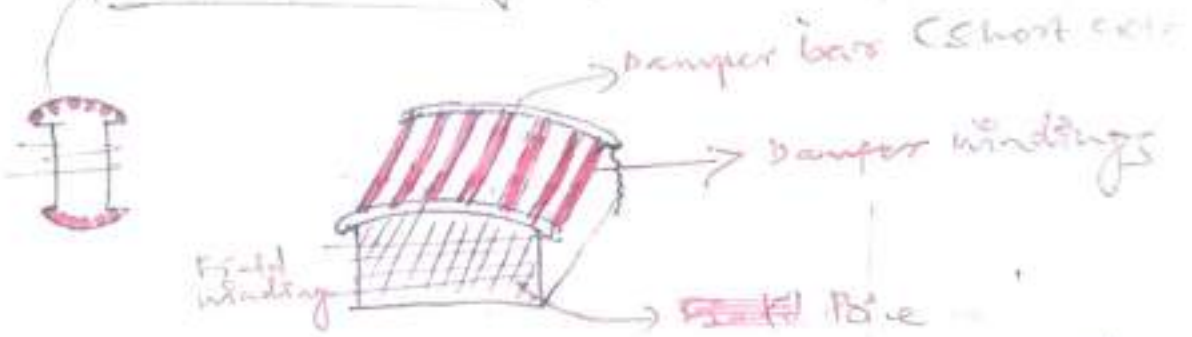


* Construction

Stator - Same as generator

rotor - salient pole 
 - cylindrical pole 

Damper Winding -



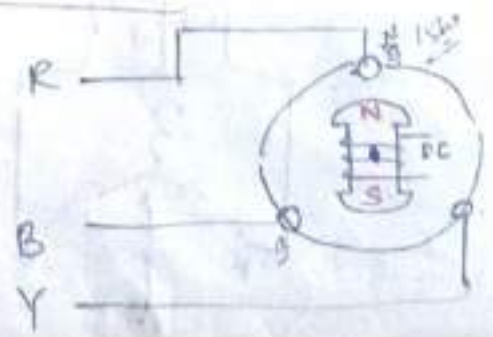
Placed on the pole face & || to stator. End of copper bars are short circuited.

It helps in starting the S/M.

Increase stability during load transient

* Principle of Operation

→ stator field rotate @ synchronous speed. in air gap -
 → Field / flux is steady (DC) / constant



- The two ϕ magnetic field in machine.
- Rotor will try to align with the stator field.

→ Stator rotating magnetic field tends to "drag" the rotor along; as if north pole on the stator "loves" with a south pole of the rotor.

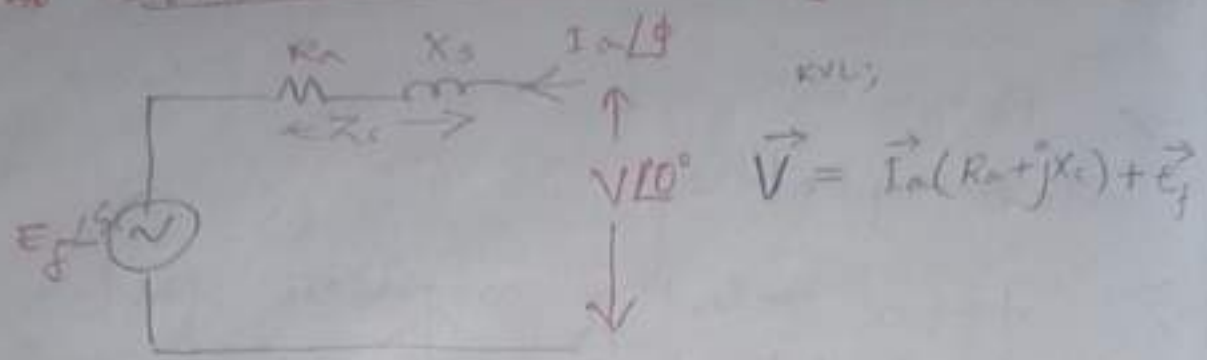
Q) Why synchronous motor is not self starting?

- At starting rotor is stationary.
- When a pair of poles rotating stator poles sweep across the stationary rotor pole @ NS, the stator pole tends to rotate in one direction & then in other direction.
- However, bez of rotor inertia, the stator field slides by so fast that rotor can't follow it.
- Hence, rotor ~~could~~ does not move & starting torque is ZERO.

* Features of SM/c

- ① While running it maintain constant speed.
- ② Not inherently self starting: to be brought into synchronism by other means.
- ③ Can be operated under wide range of PF.
- ④ It stops when load torque is more than T_{max} .

* Equivalent Phasor diagram

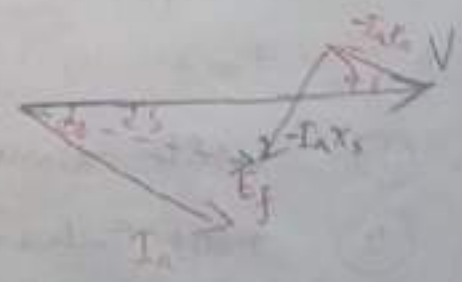
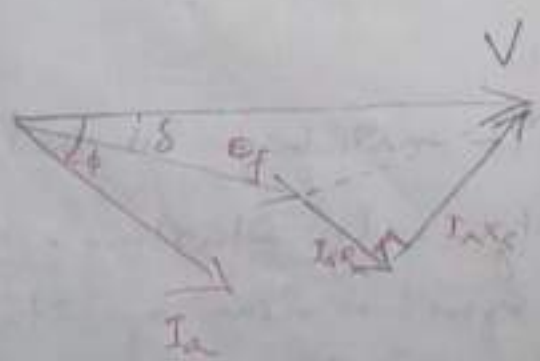


- $E_f \rightarrow$ excitation voltage.
- $V \rightarrow$ Terminal Voltage supplied.
- $I_a \rightarrow$ Armature current drawn by m/c per phase from the supply.
- R_a
- $X_s \rightarrow$ Synchronous reactance per phase.
- $Z_s \rightarrow$ Impedance per phase.
- $\phi \rightarrow$ PF angle
- $\delta \rightarrow$ Torque / Load angle
Phase diff betn V & E_f

KVL:

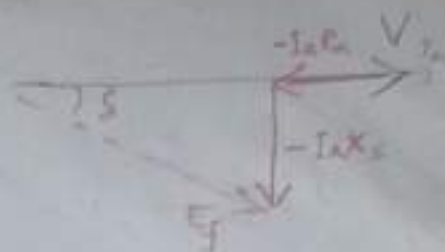
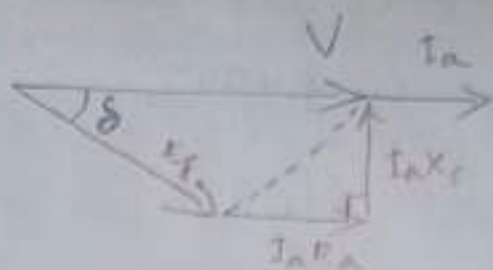
$$\vec{V} = \vec{E}_f + \vec{I}_a(R_a + jX_s)$$

$$\Rightarrow \vec{E}_f = \vec{V} - \vec{I}_a R_a - j\vec{I}_a X_s$$

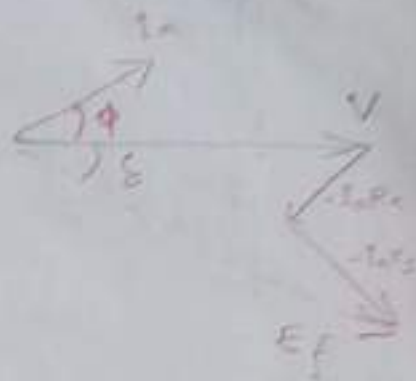
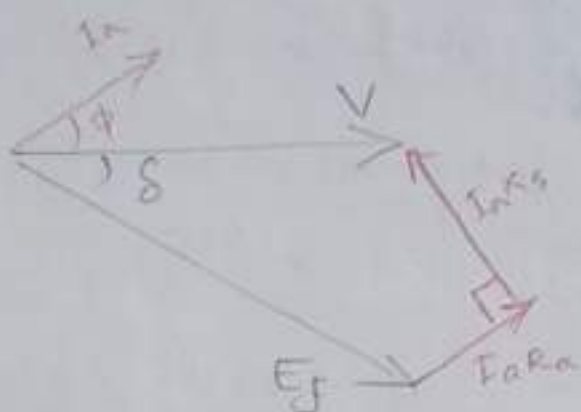


(Lagging PF)

$$E_f = \sqrt{(V \cos \phi - I_a R_a)^2 + (V \sin \phi - I_a X_s)^2}$$

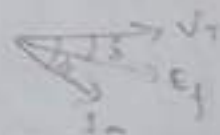
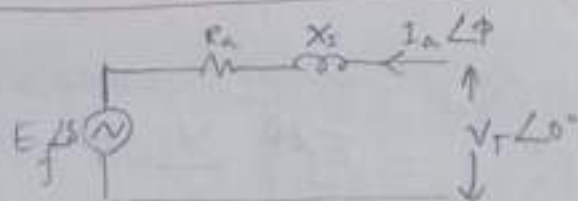


(Unity PF)
$$E_f = \sqrt{(V - I_a R_a)^2 + (I_a X_s)^2}$$



(Leading PF)
$$E_f = \sqrt{(V \cos \phi - I_a R_a)^2 + (V \sin \phi + I_a X_s)^2}$$

* Power developed in motor (put $\theta = \phi$)



$$E_f = V - I_a Z_s$$

$$\Rightarrow I_a = \frac{V \angle 0^\circ - E_f \angle \delta}{Z_s \angle \phi}$$

$$I_a = \frac{V \angle -\phi - E_f \angle -(\phi + \delta)}{Z_s}$$

$$I_a = \frac{V \angle \phi - E_f \angle \phi + \delta}{Z_s}$$

* P_{in}

$$S_{in} = P_{in} + Q_{in}$$

$$\Rightarrow S_{in} = \vec{V} \cdot \vec{I}_a^* = V \left[\frac{V \angle +\phi - E_f \angle (\phi + \delta)}{Z_s} \right]^*$$

$$\Rightarrow S_{in} = \frac{V^2 \angle \phi}{Z_s} - \frac{E_f V \angle (\phi + \delta)}{Z_s}$$

To match convention
[Reactive power
& Active power]
Polarity

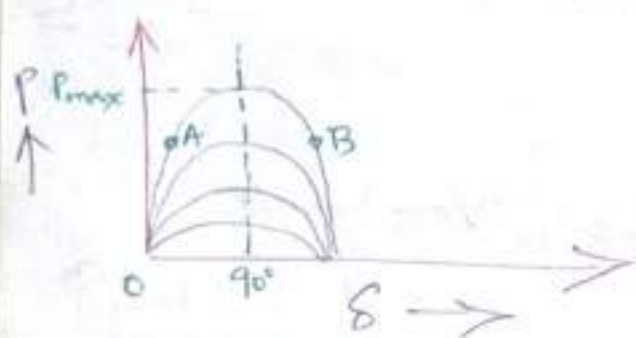
But $R_a \ll X_s \ll X_c$
 $Z_c \approx X_s$; $\phi = 90^\circ$

$$S_{in} = P_{in} + Q_{in}$$

$$P_{in} = \frac{V^2}{X_s} \cos(\phi) - \frac{E_f V}{Z_s} \cos(\phi + \delta)$$

$$P_{in} = \frac{E_f V}{X_s} \sin(\delta)$$

$$P_{max} = \frac{E_f V}{X_s} \quad @ \delta = 90^\circ$$



A → stable region
 B → unstable region
 (will make rotor out of synchronism)

* P_{out} (P_{mech})

$$S_o = P_o + Q_o$$

$$\Rightarrow S_o = E_f I_a^* = E_f \left[\frac{V}{Z_c} \angle \phi - \frac{E_f}{Z_s} \angle (\phi + \delta) \right]$$

$$\Rightarrow S_o = \frac{V E_f}{Z_s} \angle (\phi - \delta) - \frac{E_f^2}{Z_s} \angle (\phi + \delta - \delta)$$

$$\Rightarrow S_o = \frac{V E_f}{Z_s} \angle (\phi - \delta) - \frac{E_f^2}{Z_s} \angle \phi$$

$$P_{out} = \frac{V E_f}{Z_s} \cos(\phi - \delta) - \frac{E_f^2}{Z_s} \cos(\phi)$$

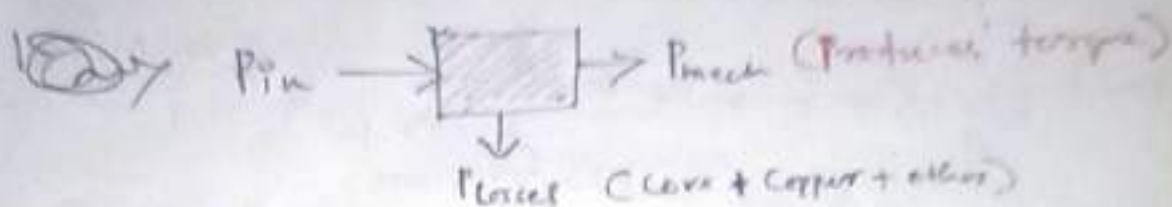
$P_{o/max} = \frac{V E_f}{Z_s} @ \phi = \delta = 90^\circ$

* Torque

$$P_o = \tau W$$

$$\Rightarrow \tau = P_o / W$$

$$\Rightarrow \tau = \frac{V E_f \cos(\phi - \delta)}{W Z_s} - \frac{E_f^2}{Z_s W} \cos(\phi)$$



* Q_{in} (X)

$$\textcircled{3} Q_{in} = \frac{V}{X_s} (V - E_f \cos \delta)$$

$$\textcircled{1} Q_{in} = \frac{V}{X_s} (V \angle \phi - E_f \angle (\phi + \delta))$$

$$\textcircled{2} Q_{in} = \frac{V^2}{Z_s} \sin \phi - \frac{E_f V}{Z_s} \sin(\phi + \delta)$$

I. (X)

if $V - E_f \cos \delta = 0$

$\Rightarrow V = E_f \cos \delta$ (unity PF)

Normally excited generator

II. if $V > E_f \cos \delta$

$Q_{in} = +ve$

underexcited motor

Absorb lagging VAR (lagging PF)

III. if $V < E_f \cos \delta$

$Q_{in} = -ve$

Absorbing leading VAR = output @ lead PF.

* Effect of varying I_f (excitation) and load constant

$$P_o = \frac{E_f V}{X_s} \sin \delta = V I_a \cos \phi$$

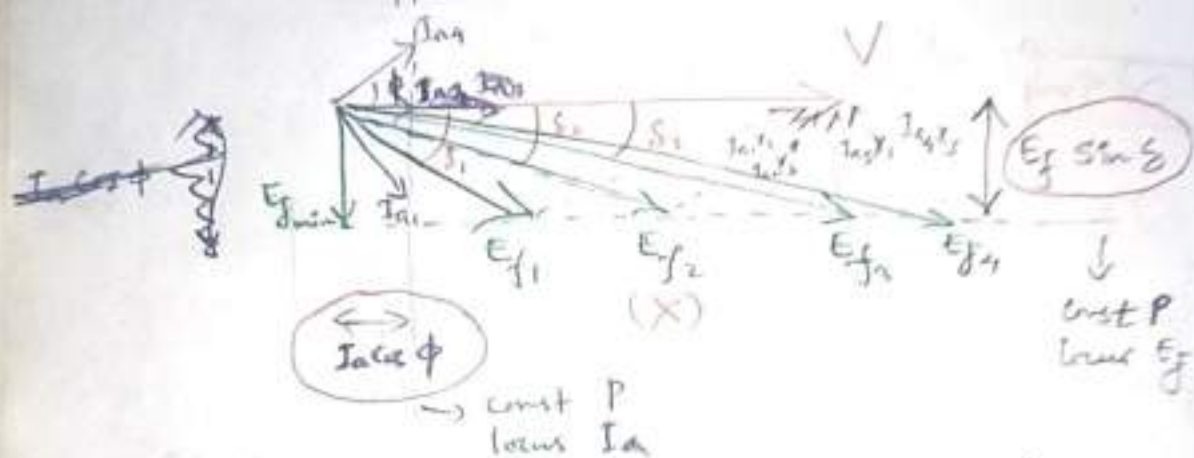
$V, X_s \rightarrow$ constant

$P_o \rightarrow$ constant (\because load is constant)

$$E_f \sin \delta = \text{constant}$$

$$I_a \cos \phi = \text{constant}$$

$$\vec{V} = \vec{E} - \vec{I} X_s$$



$$\uparrow E_f \propto I_f \uparrow \quad (\because \uparrow E_f \propto \omega \uparrow)$$

but $E_f \sin \delta$ is constant

$\rightarrow I_a X_s$ varies $\rightarrow I_a$ varies but $I \cos \phi$ is constant

Since; $I_a (jX_s) = V - E_f$

$$\Rightarrow I_a = \frac{V - E_f}{jX_s}$$

' I_a ' must remain \perp^{to} to drop " $-I_a X_s$ "

$$\left\{ \begin{array}{l} E_f \sin \delta = \text{const} \\ I_a \cos \phi = \text{const} \\ I_a \perp^{\text{to}} \text{ to } jX_s I_a \end{array} \right\} \text{constraints.}$$

$$E_{g1} \sin \delta_1 = E_{g2} \sin \delta_2 = E_{g3} \sin \delta_3$$

$$I_{a1} \cos \phi_1 = I_{a2} \cos \phi_2 = I_{a3} \cos \phi_3$$

Conclusion

(i) $A_f \uparrow I_f \rightarrow \uparrow E_f \rightarrow$

\downarrow First I_a decreases & then increases again

(ii) For Small E_f ;

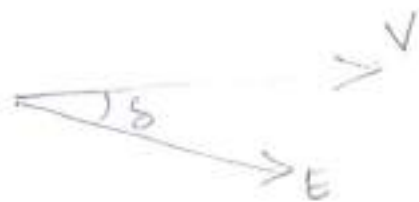
I_a is lagging and the motor is an "lt" load.
Consume \mathcal{Q} power.

(iii) $A_f \uparrow E_f \uparrow$

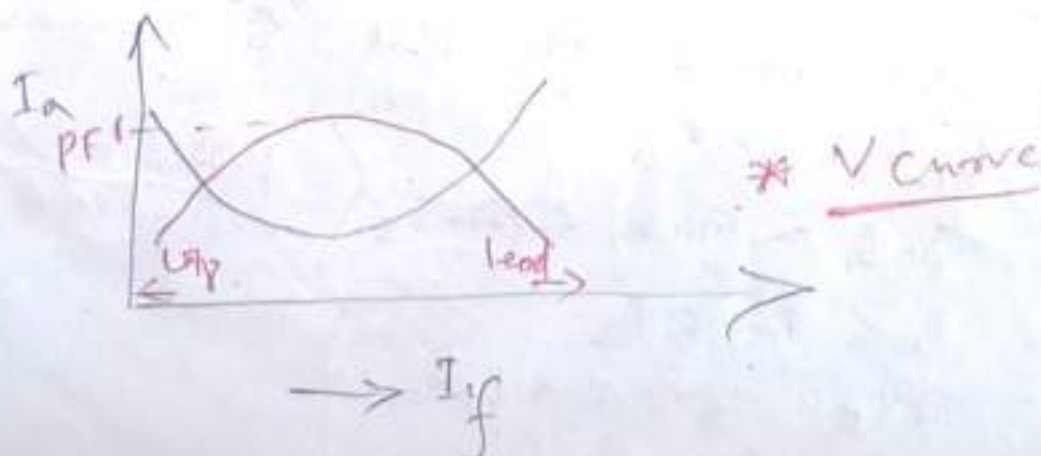
I_a comes in phase with V . } Normal Excitation
Motor becomes purely "R" load.

(iv) $A_f \uparrow E_f \uparrow$ further

I_a becomes leading.
Motor becomes Capacitive load.
Consume $-\mathcal{Q}$
Supply \mathcal{Q} power to the system.



i_f $E \cos \delta < V$; \rightarrow lagging PF
 i_f $E \cos \delta > V$; \rightarrow leading PF



* Effect of varying load $I_f = \text{constant}$

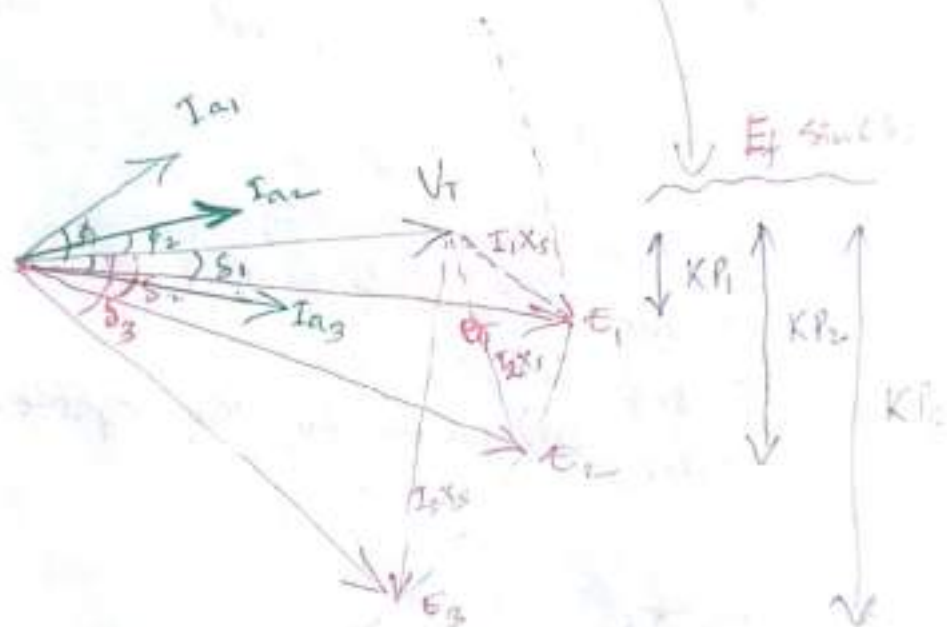
$N_s, I_f, E_f, X_s, V_t \rightarrow \text{constant}$
 $\rightarrow [K \phi \omega] \text{ constant}$

We have,

$$P = \frac{V_t E_f}{X_s} \sin \delta = V_t I_a \cos \phi$$

$$\uparrow \frac{P(X_s)}{V_t} = \frac{E_f \sin \delta}{\text{const}} \uparrow$$

$$\Rightarrow PK = E_f \sin \delta$$



Start with leading load.

\rightarrow load is increased.

rotor momentarily slow down

$$\uparrow \tau_{ind} = \frac{V E_f}{X_s} \sin \delta \uparrow$$

\rightarrow rotor run @ N_s but " δ " increases.

- $E_1 = E_2 = E_3$
- $\sin \delta_1 < \sin \delta_2 < \sin \delta_3$
- $P_1 < P_2 < P_3$
- $I_1 X_s < I_2 X_s < I_3 X_s$
- $I_1 < I_2 < I_3$

With increase in load

Conclusion (When load is increased)

- (i) Motor run @ N_s (\rightarrow ~~E_g~~ \rightarrow const)
- (ii) Torque/Load angle δ \uparrow
- (iii) E_g remain constant
- (iv) I_a drawn from supply increases
- (v) " ϕ " phase angle increases in lagging direction. Load ~~is~~ can be increased till motor reach pull out torque.

Torque

I Break Pull-in torque

A SM is started as IM till it runs @ 95-98% of N_s . Then DC excitation is given to the rotor & it pulls into synchronism with the stator rotating magnetic field.

It is the maximum ~~or~~ constant torque @ V_{rated} & f_{rated} : under which a motor will pull a connected load into synchronism ~~with~~ when DC motor excitation is applied.

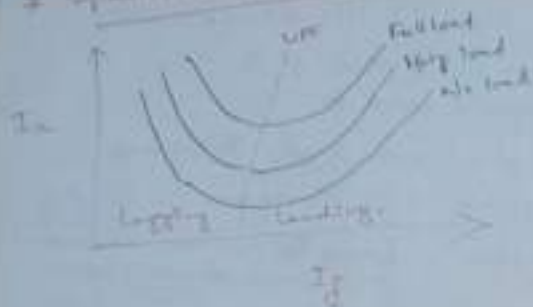
II Running Torque

It is the torque developed by the motor @ running condⁿ. $(\propto \text{Power rating})$
 $\propto W$

III Pull-out torque

It is the maximum torque that motor can develop @ V_{rated} & f_{rated} without losing synchronism.
 $\propto W$
 \rightarrow $(\propto W)$

Synchronous motor V-curves



$\uparrow \text{load} \rightarrow \uparrow I_a \rightarrow \uparrow \cos \phi \rightarrow \uparrow \phi \rightarrow \uparrow E_b$
($\uparrow I_a$)

Causes/Effects of Hunting

- ① Loss of synchronism
- ② Same day cause V_f variation: pointing undesirable lamp flicker
- ③ Large mechanical stress on rotor
- ④ Temperature of machine rises, machine loss increases

Hunting / Phase swinging

$$\uparrow T_e = \frac{9VE_b \sin \delta}{\omega_s}$$

When there is change in load (\uparrow)

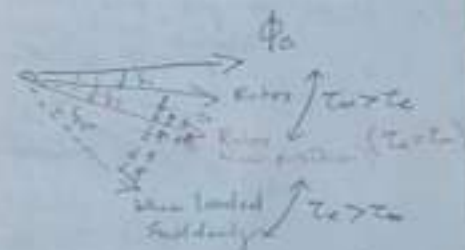
$$\uparrow T_{load}$$

$$T_e - T_{load} = \int \frac{d\omega}{dt}$$

angular velocity of rotor
constant

The motor slows down a bit & δ is increased to restore the torque equilibrium \rightarrow $\uparrow N_s$

$\rightarrow \uparrow \delta \rightarrow \uparrow T_e \rightarrow \uparrow N$ till it reaches N_s



\rightarrow The phenomenon of oscillation of the rotor about its final equilibrium position after load changing load is called Hunting

Causes of Hunting

- (i) Sudden change of load
- (ii) Fault in system
- (iii) Sudden change in I_f
- (iv) Cycle variation of load torque

* Reduction of ~~Loss~~ Hunting

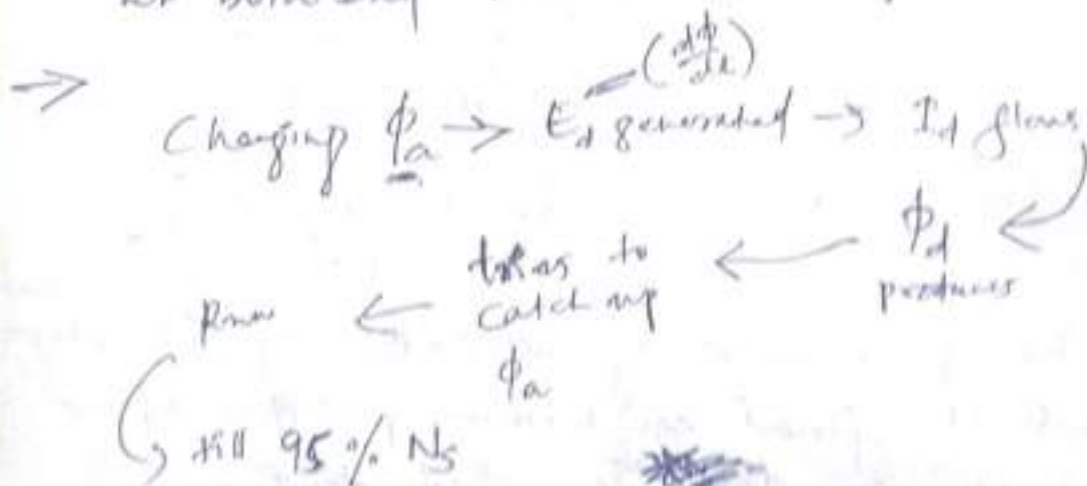
- ① Use damper winding.
- ② Use of flywheel.

Can prime mover mounted with heavy flywheel. Increase J of motor & help in maintaining the motor speed.

* Damper Winding/Bar



→ Copper bar on pole faces are short circuited at both end ^{placed} || to the shaft.



Used

- ① Starting of SM (Self Starting)
- ② ~~SM~~ Reduces hunting phenomenon. oscillation in.

* Starting of SM (After Dumper winding)

① With the help of Dumper winding

② With external prime motor

- external motor drives the SM & brings it to synchronism. (IM with 2% slip less than SM)
- SM is synchronised as a generator with the busbar as a synchronous generator.
- Then prime mover is disconnected.
- Now m/c run as SM & load can be connected to it.

$$\Rightarrow T_{HL} < T_{FL}$$

* Application of SM

→ Constant Speed application.

- ① High P; High N's compressor
② Blower.

③ ~~Variable~~ variable main line traction.

④ Variable inductor/capacitor, in power transmission line to regulate voltage.

⑤ Synchronous condenser to provide VAR (Re) in industries.

⑥ Explain it

$$Q_{in} = \frac{V}{X_s} (V - E_f \cos \delta)$$

⊕ leading (over excited)
⊖ lagging (under excited)
(Supply VAR)

THREE-PHASE II

→ For large power transfer
 → step up & step down voltage in various stages
 of power system etc.

3-Phase Group

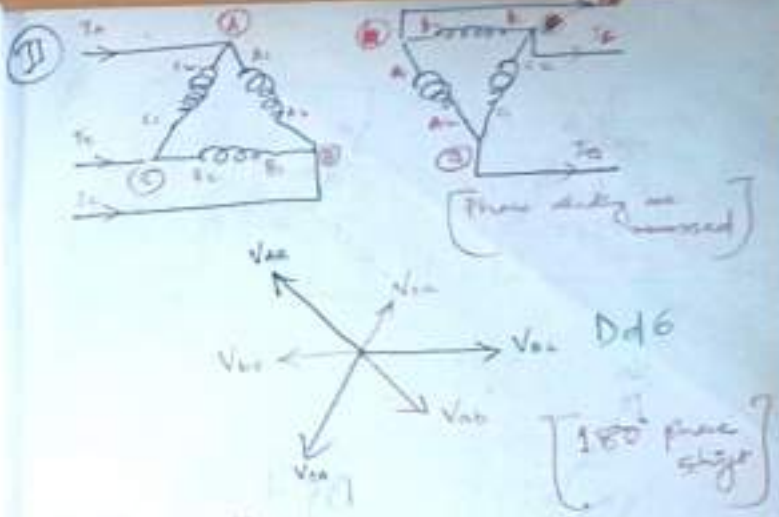
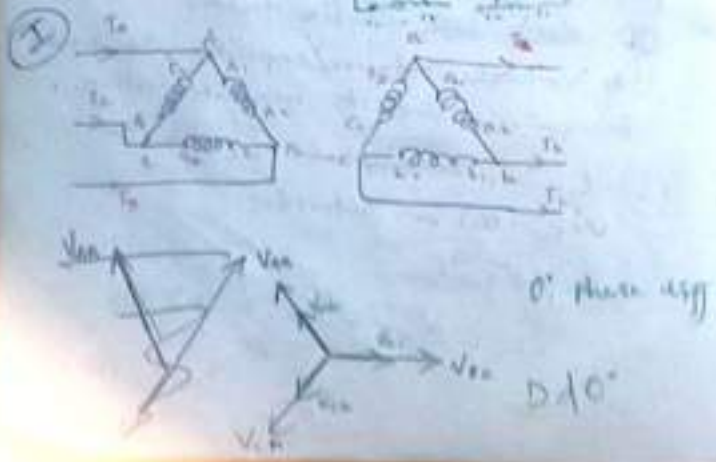
Y → star
 Δ → delta

- ① Grp-I : No phase displacement $Yy0, Dd0$
- ② Grp-II : 180° — Δy — $Yy6, Dd6$
- ③ Grp-III : $(\pm 30^\circ)$ — Δy — $Yd1, Dy1$
- ④ Grp-IV : $(\pm 30^\circ)$ — Δy — $Yd11, Dy11$

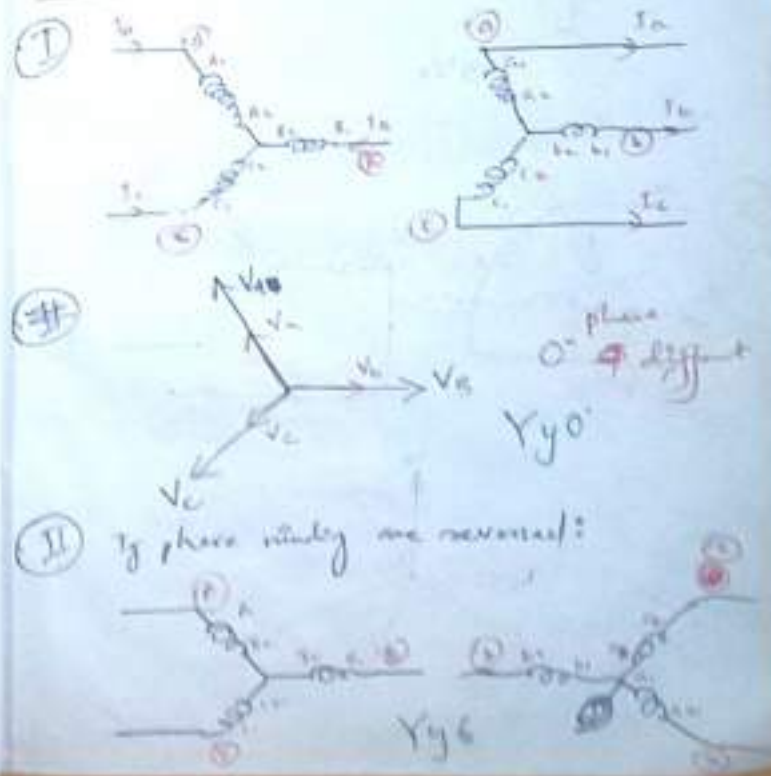


$Yd11$ — Δy — $Yy0$ — Δy — $Yy0$
 (clockwise)

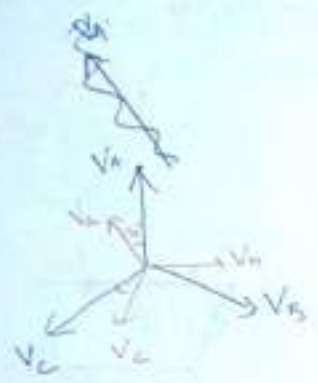
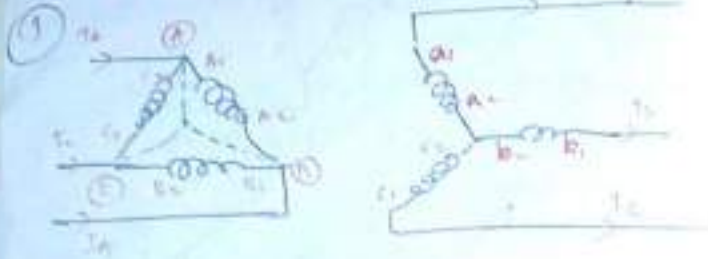
Δ-Δ Connection



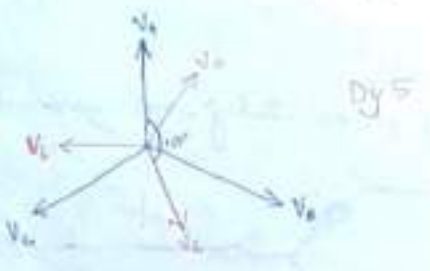
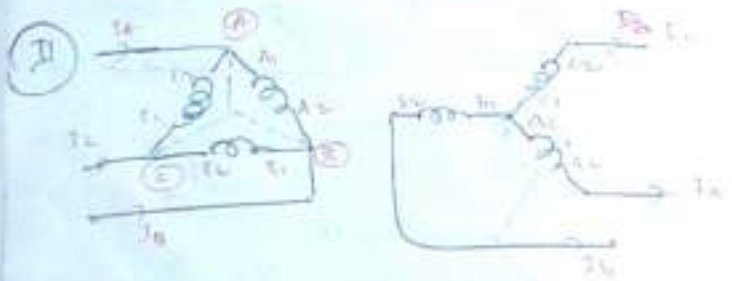
Y-Y connection



3 Δ -Y connection

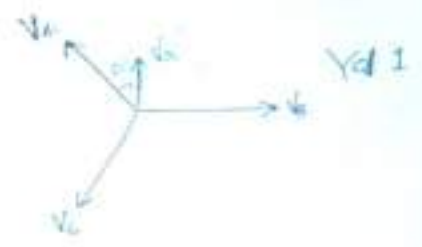
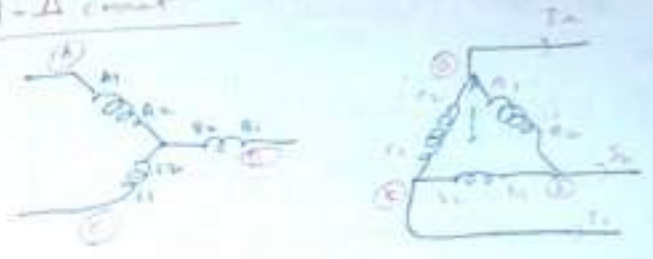


Δ Y II



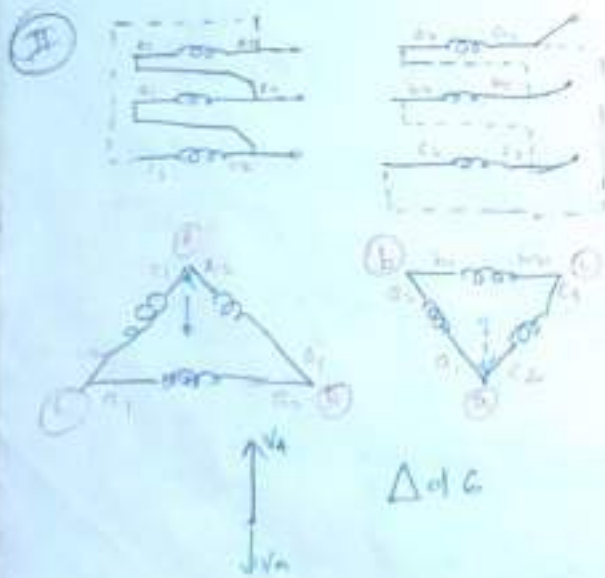
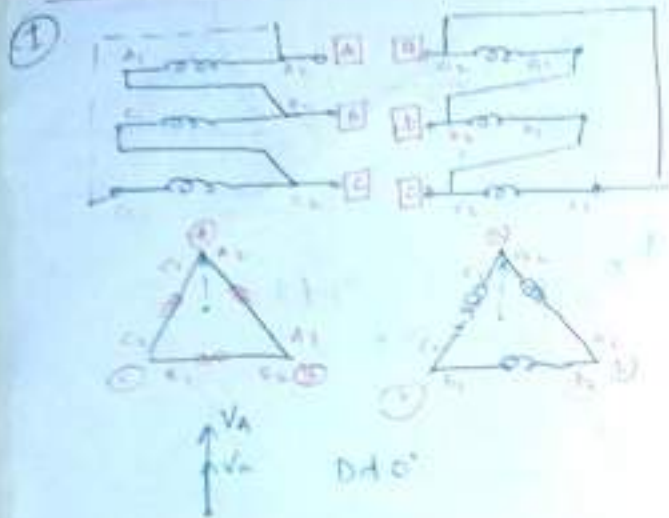
Δ Y V

4 Y - Δ connection

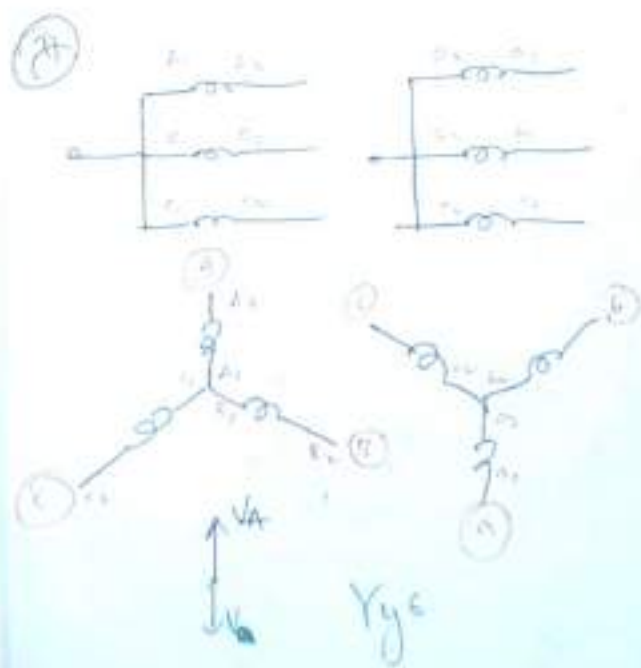
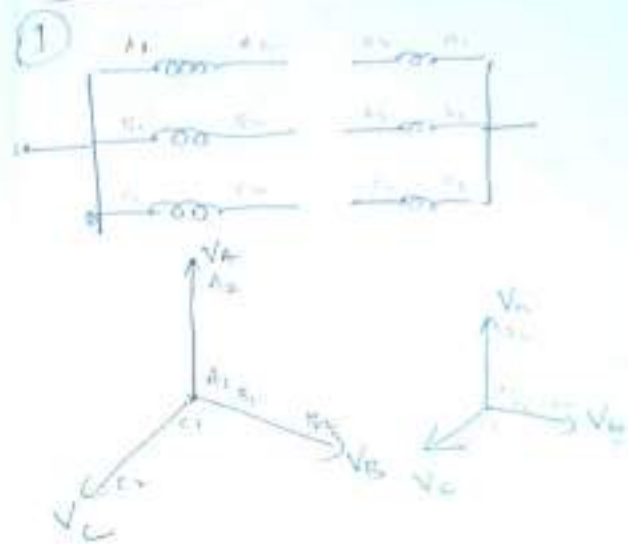


Y Δ I

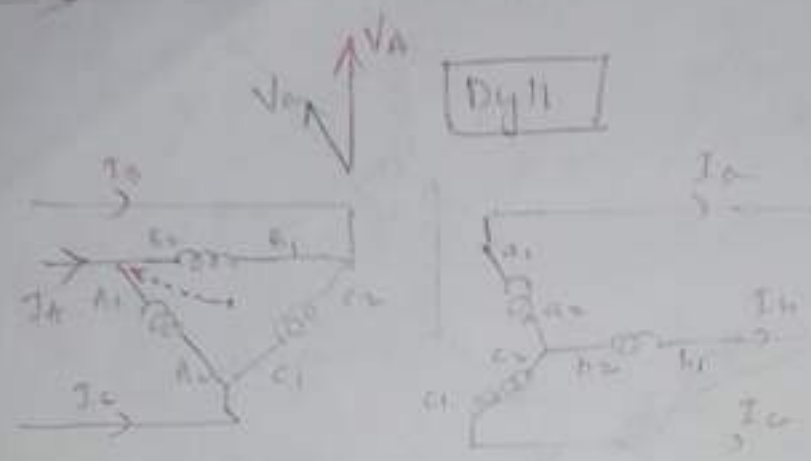
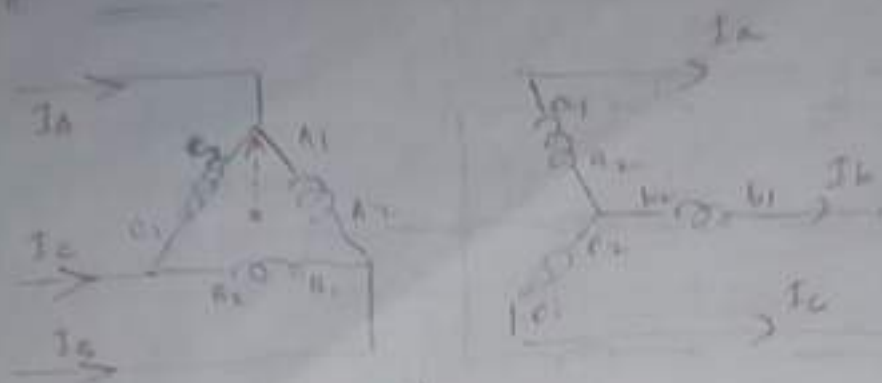
~~Star~~ Δ - Δ connect



Y-Y connect (Teacher Hand)



* $\Delta-\Delta$

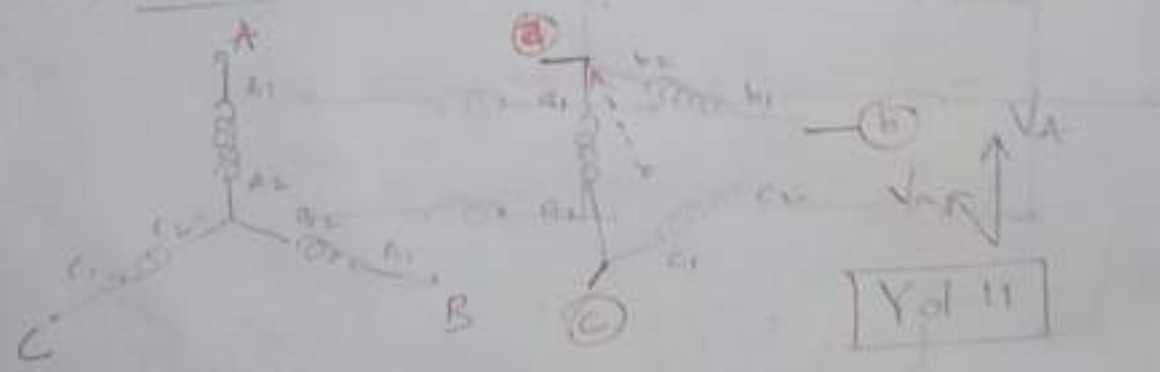


$Dy11$

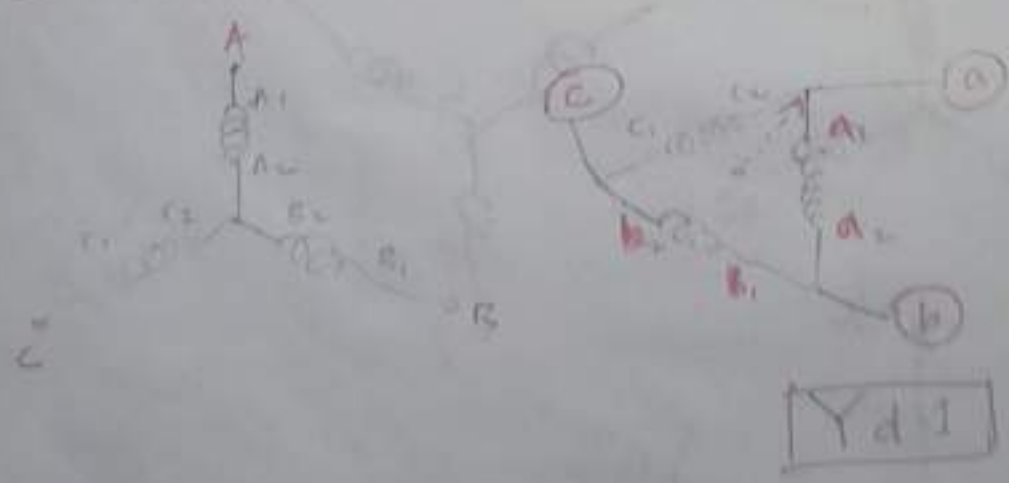


$Dy1$

* $Y-\Delta$



$Yd11$



$Yd1$

$0^\circ \rightarrow Yy0, Dd0$

$180^\circ \rightarrow Yy6, Dd6$

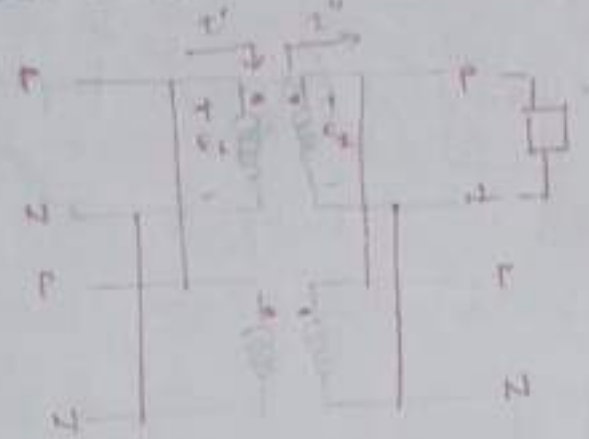
$-90^\circ \text{ (lag)} \rightarrow Yd1, \Delta y1$

$30^\circ \text{ (lead)} \rightarrow Yd11, \Delta y11$

* Parallel operation of 3 ϕ TF

1/1 Polarities of TF must be same

(Dot convention) \rightarrow (same polarity) if entire dot in



{ primary & secondary dot in 2 $^\circ$.
(ϕ^1 opp to ϕ^2)
[I_1^1 entire dot,
 I_2^1 entire dot.
 ϕ^1 & ϕ^2 are additive

2 Identical 1 $^\circ$ & 2 $^\circ$ voltage ratings



\rightarrow load sharing Acc to their ratings
(Same PF operation)

4 Identical $\frac{X}{R}$ ratios in the TF impedance.

3 ϕ /5 Same pu impedance for load sharing (desirable)
(Zpu)

A Phase sequence must be the same. (0-1-2)

B The phase shift both 1 $^\circ$ & 2 $^\circ$ voltage must be same for all TF which are connected in 1 $^\circ$.

(Phase group)

$\Delta\Delta$	ΔY	
YY	$\Delta\Delta$	
$Dd0^\circ$	ΔY	
$Yy0^\circ$	ΔY	
	ΔY	$Yd11$
	ΔY	$Yd11$
	ΔY	$Dy1$
	ΔY	$Dy1$
	ΔY	$Yd1$

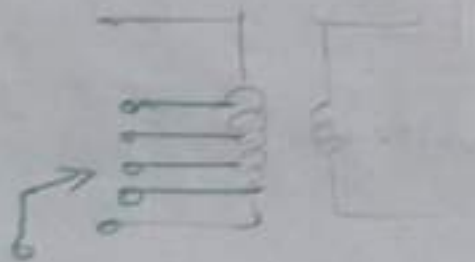
* Reason for 11kV operation

- ① Uneconomical to have a long line
- ② Capacity of Spare to reduce
- ③ Scope for future expansion
- ④ Reliability to provide supply during fault

Spark the lines with a fault

I Off load Tap changer (After Tap changer)

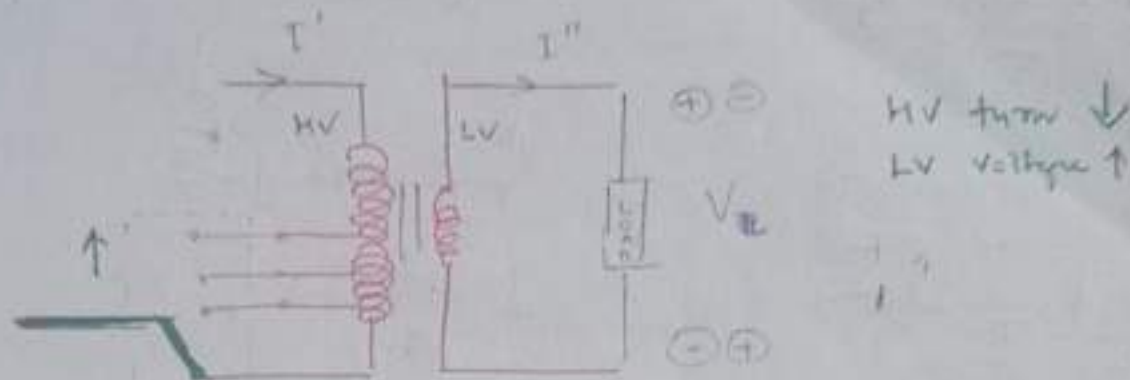
It regulates the output voltage through changes of Tap in the transformer.



→ The TR is disconnected from the supply when tap changing is required.

* Tap changer (First)

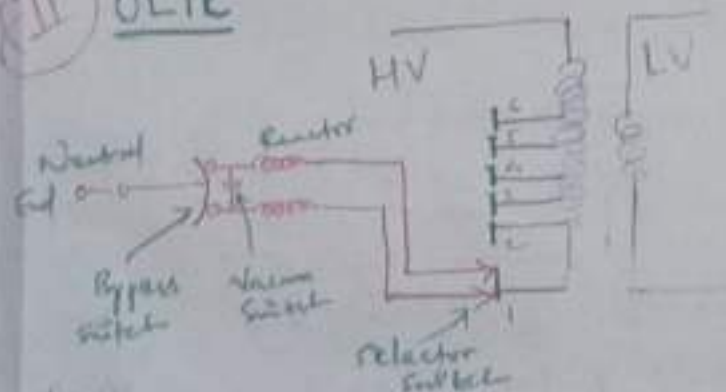
- Due to change in load; V_L varies.
 \uparrow load $\rightarrow \downarrow V_L$ (drop)
- To keep the V_L constant & tapping from HV winding as to receive



\rightarrow Why on HV winding?

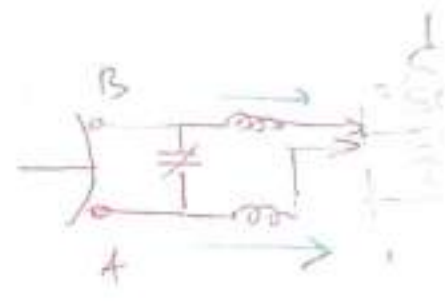
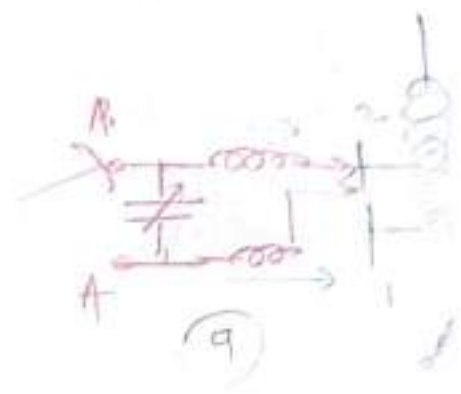
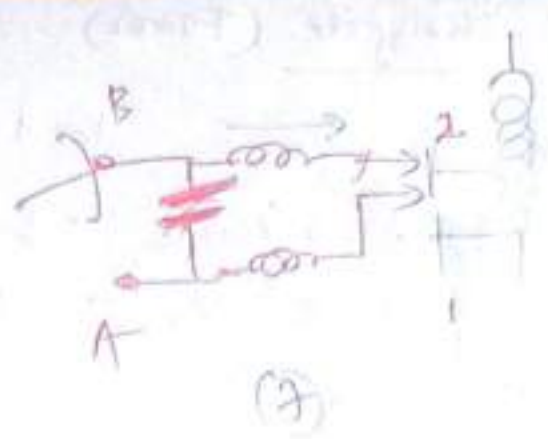
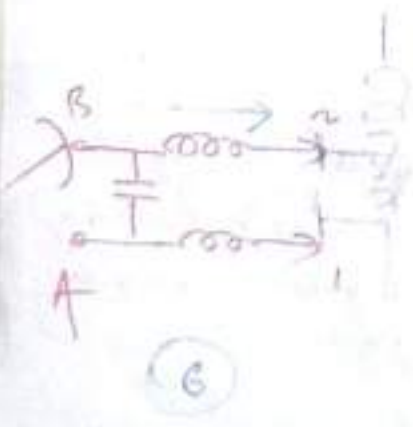
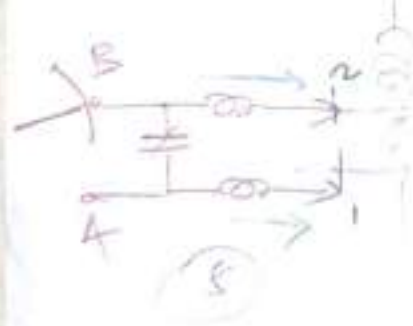
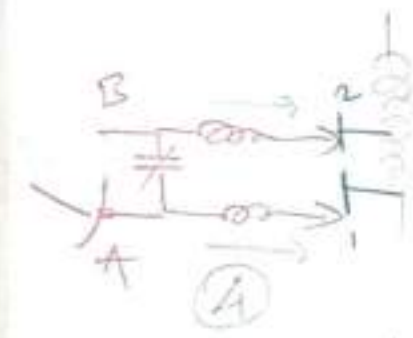
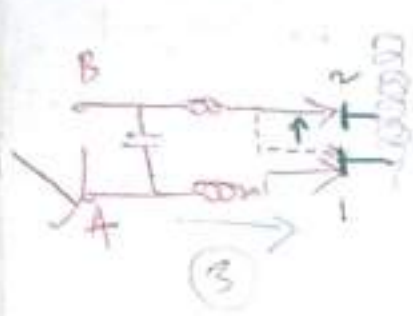
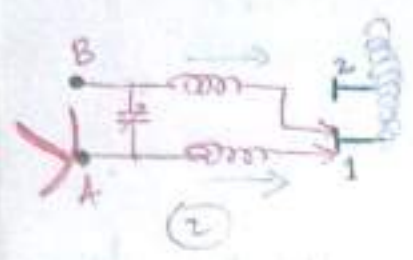
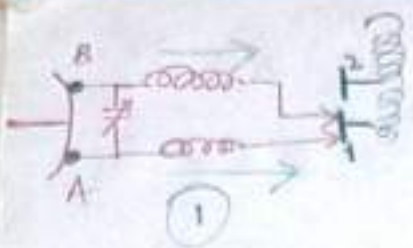
- ① HV winding are on & outside the LV, so easier to get tapping connection.
- ② Current is low on HV side, tap changing lead can be smaller size. (Less sparking).

II OLTC



\rightarrow Load cut should not be broken to avoid arcing which may damage insulation.

- ① Selector switch (Select taps from HV winding)
- ② Reactor (during tap change, circulating current is limited by it)
- ③ Vacuum contact (Duty of this device is to break & make current during tap changing operation)
- ④ Bypass switch



* Maintenance of 3 ϕ TF

I Daily

(1) Ambient Temperature

(2) Winding Temperature if oil temp

If above normal level then; shutdown TF.

(3) Load & Voltage

Check against rated figure.

II Weekly

(1) Oil level

if low then & check than the minimum level then check out for leakages.

(ii) Oil level in bushing

if low then; stop the oil & examine

for leakage.

III Monthly

(i) Relief diaphragm

Replace if crack or broken.

→ Mechanical pressure relief valve.

→ Gas pressure will lift the diaphragm & gas escape quickly.

(ii) Dehydration breather

Check for the color of silica gel.

If pink then change with new &

dehydrate the pink silica gel to get back to normal color.

(III) Quarterly

(I) Brushing

Examine for cracks & dirt.
Pulley; clean or replace.

(IV) Half yearly

(1) Oil

Check for dielectric strength &
water content in it.

(2) Carbons, bearings & control mechanism

Lubricate bearing, check gears,
examine contacts, control.
Replace burnt or worn contact pair.

(III) Oil pressure

Test for pressure.
Examine if any leakage.

(V) Yearly

(I)

Oil the arrangements / Oil filled bushes

Check for sludge.
Filter or replace.

(II)

Cable box

Examine the connection of cranks.

3 ϕ INDUCTION MOTOR

* Advantages

- ① Cheap
- ② Robust
- ③ Efficient
- ④ Reliable
- ⑤ Overload Capacity
- ⑥ Good Speed regulation
- ⑦ High $T_{starting}$.
- ⑧ Little maintenance

* Construction

① STATOR

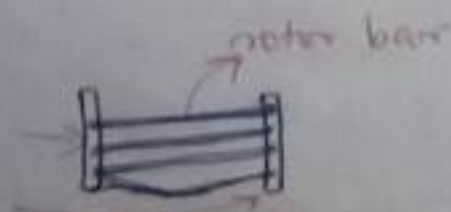
- High grade alloy steel lamination.
- Lamination are supported on stator frame of cast iron.
- Stator insulated conductor are placed on the slots present in inner periphery of the stator frame.
- Stator conductor are connected to form 3 ϕ winding.

② Rotor

- Laminated alloy of steel.
- Mounted on the shaft
- Lamination are slotted on the outer periphery to receive rotor conductor.

① Cage rotor

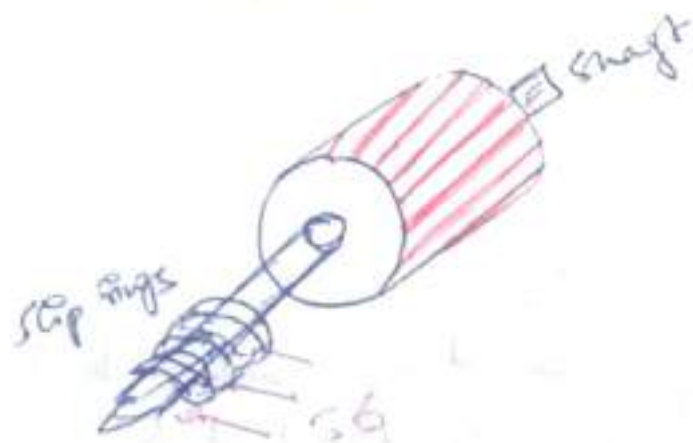
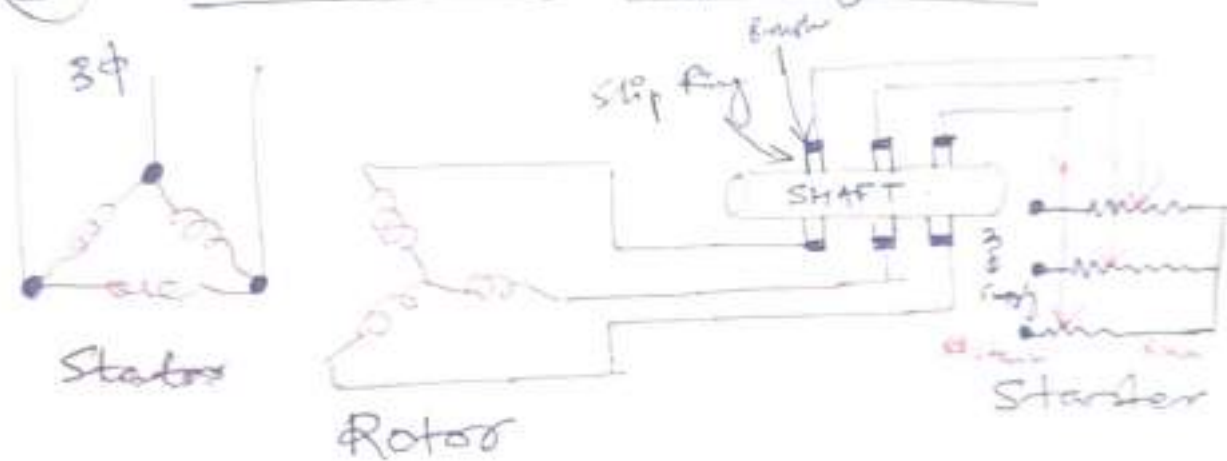
- Copper/Al
- Screwed slots/bars



* Skewed because

- (i) More uniform torque & less noise during operation
- (ii) Locking tendency of rotor is reduced;
Locking
rotor & stator teeth attract each other due to magnetic action

ⓑ Wound rotor / slip ring rotor



- Insulated conductors are put in slots of rotor to form 3 ϕ distributed winding
- Slip rings are mounted on the shaft & brushes resting on them.
- This set up provide connection to external resistance.

Why Rotor connected

- (I) To increase T_{st} & I_{st} decrease.
- (II) To control speed of motor.

* Working Principles III

According to Faraday's law of EMF, EMF is induced in rotor bar due to change in magnetic flux (3 ϕ rotating magnetic field) linkage through it.

As rotor bars are short circuited, current flows through the rotor bars.

As per Lenz's law, the rotor will rotate ~~to~~ to reduce the relative speed ~~rate~~ between magnetic flux & stator rotor conductor.

(To reduce its cause).

If rotor speed up to N_s ; then there shall be no relative speed.

~~It~~ It results in no flux change ~~to~~ experienced by rotor bars.

Hence no emf is induced & no current flows in rotor conductor.

Therefore, rotor ~~decelerates~~ ^{would} decelerate no ~~any~~ torque will be generated.

\therefore Rotor decelerate & can't run at N_s .

It always run \odot ~~at~~ below N_s

As, the motor operation depends upon the induced voltage in rotor conductors, it is called induction motor.

SLIP

between
The difference in speed the N_s & rotor speed is called "slip speed".

$$\% S = \frac{N_s - N_r}{N_s} \times 100 \quad \left| \begin{array}{l} \text{Percent} \\ \text{slip} \end{array} \right.$$

$$\text{Speed Slip} = N_s - N_r$$

It is around 5% at full load
2% at large motor.

* Frequency of Rotor voltage & current

$$\text{At stator: } f = \frac{PN_s}{120}$$

$$\text{At rotor: } f_r = \frac{P(N_s - N_r)}{120}$$

$$\frac{f_r}{f} = \frac{N_s - N_r}{N_s} = S$$

$$\Rightarrow \boxed{f_r = S f}$$

(A) Standstill, $N_r = 0$; $S = 1$; $f_r = f$

(B) $N_r = N_s$; $S = 0$; $f_r = 0$

② Frequency of e.m.f. in ^{stator or} 4 pole IM is 50 Hz, and that in rotor is 1.5 Hz. What is the slip, and speed of motor.

$$f_r = s f$$

$$f = 50 \text{ Hz};$$

$$f_r = 1.5 \text{ Hz};$$

$$s = \frac{1.5}{50} = \underline{\underline{3\%}}$$

$$N_s = \frac{120 f}{p} = \frac{120 \times 50}{4} = \underline{1500 \text{ rpm}}$$

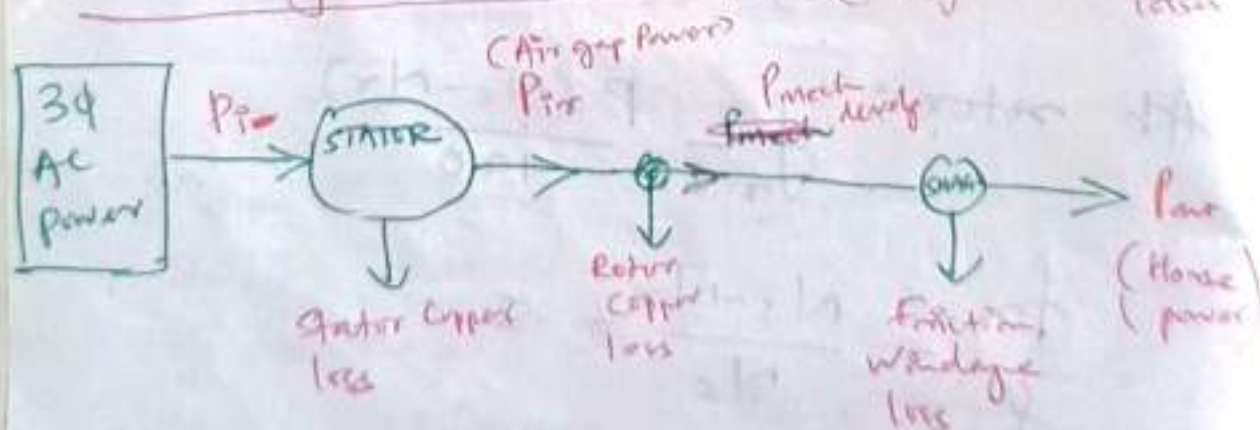
$$s = \frac{N_s - N_r}{N_s} \times 100 = 3$$

$$\Rightarrow \frac{1500 - N_r}{1500} = \frac{3 \times 1500}{100}$$

$$\Rightarrow N_r = 1500 - 45$$

$$N_r = \underline{1455 \text{ rpm}}$$

Power flow in IM (Before Rotor losses)



gato = starting method of IM

* ROTOR CURRENT

⊕ At standstill

{ 0 → standstill } subscript
 { s → rotor }

Let; E_{r0} = emf induced/phase of rotor @ standstill
 R_r = Resistance per phase -
 X_{r0} = reactance/phase
 Z_{r0} = Impedance/phase

Then
$$I_{r0} = \frac{E_{r0}}{Z_{r0}}$$

$$\cos \phi_{r0} = \frac{R_r}{Z_{r0}} = \frac{R_r}{\sqrt{R_r^2 + X_{r0}^2}}$$

Ⓛ At Running

{ s → slip } subscript

$E_{rs} = s E_{r0}$ induced emf/phase at slip 's'

$R_r \rightarrow$ constant
 $X_{rs} = 2\pi (sf_0) L = s \cdot X_{r0}$

$$Z_{rs} = s R_r + j X_{rs} = R_r + j s \cdot X_{r0}$$

$$I_{rs} = \frac{E_{rs}}{Z_{rs}}$$

$$\cos \phi_{rs} = \frac{R_r}{\sqrt{R_r^2 + (s X_{r0})^2}} \quad \text{[NOT REQUIRED]}$$

Power generated at rotor $\rightarrow I^2 R$ copper loss

$$P_{rs} = 3 E_{rs} I_{rs} \cos \phi_{rs} = 3 E_{rs} \frac{E_{rs}}{Z_{rs}} \frac{R_r}{Z_{rs}}$$

$$\Rightarrow P_{rs} = 3 \frac{E_{rs}^2 R_r}{(Z_{rs})^2} = 3 \frac{s^2 E_{r0}^2 R_r}{R_r^2 + (s X_{r0})^2}$$

$\frac{P_{rs}}{s} [s \cdot 2\pi n \tau d] = P_{rs}$ (All power will be $I^2 R$ loss)
 rotor input \rightarrow GOTO TORQUE

Example 4.4 (Page 319) "Asfag Hassan"

3 ϕ , 50Hz, 4-pole IM	$R_2 = 1\Omega$
Slip = 4%	$X_{20} = 4\Omega$
Calculate (a) Speed of motor	ϕ_{20} (a) start of
(b) frequency of rotor emf	(b) 1400 rpm

Ans (i)

$$(a) N_s = \frac{120f}{p} = 1500 \text{ rpm}$$

$$s = \frac{N_s - N_r}{N_s} \times 100 \quad N_r = (1-s)N_s$$

$$\Rightarrow \frac{4 \times 1500}{100} = 1500 - N_r$$

$$\Rightarrow \boxed{N_r = 1440 \text{ rpm}}$$

$$(b) f_r = sf = \frac{(4)(50)}{100}$$

$$\Rightarrow \boxed{f_r = 2 \text{ Hz}}$$

$$(ii) (a) \phi_{20} = \frac{R_2}{\sqrt{R_2^2 + X_{20}^2}} = \frac{1}{\sqrt{1+16}} = 0.24$$

$$\cos \phi_{20} = \cos(75^\circ) = \underline{\underline{0.24 \text{ (lag)}}}$$

$$(b) (a) 1400 \text{ rpm}$$

$$s = \frac{1500 - 1400}{1500} \times 100 = \frac{100}{15} \% = 6.67\%$$

$$Z_{2s} = R_2 + j s X_{20} = 1 + j \frac{1}{15} (4)$$

$$\Rightarrow Z_{2s} = 1.034 \angle 14.93^\circ$$

$$\cos \phi_{2s} = \underline{\underline{0.9662 \text{ (lag)}}}$$

* Relationship between rotor Copper

Loss of rotor input (After Power flow in IM)

T_d = developed torque on the rotor.

n_s = synchronous speed (rpm) = $\frac{N_s}{60}$

n_r = rotor speed (rpm) = $(1-s)n_s$

P_{ir} = Power input to rotor from stator.

$$P_{ir} = \omega_s T_d = 2\pi n_s T_d$$

P_m = Mechanical power developed by rotor.

$$P_m = \omega_r T_d = 2\pi n_r T_d$$

" $I^2 R$ " loss in rotor = $P_{ir} - P_m$

$$\Rightarrow P_{rc} = 2\pi (\omega_s - \omega_r) T_d$$

$$\frac{P_{rc}}{P_{ir}} = \frac{2\pi (n_s - n_r) T_d}{2\pi n_s T_d} = \frac{n_s - n_r}{n_s}$$

$$\Rightarrow \boxed{P_{rc} = s \cdot P_{ir}} \leftarrow \text{Slip power (loss)}$$

$$P_{ir} = P_m + P_{rc}$$

$$P_{rc} = s (P_m + P_{rc})$$

$$\Rightarrow \boxed{P_{rc} = \left(\frac{s}{1-s}\right) P_m}$$

$$P_{ir} = P_m + s P_{ir}$$

$$\Rightarrow P_{ir} (1-s) = P_m$$

$$P_{ir} : P_{rc} : P_m = 1 : s : (1-s)$$

$$n_s : n_{\text{eng. gen.}} : n_r = 1 : s : (1-s)$$

$$P_{rc} = s \cdot P_{ir}$$

$$P_m = (1-s) \cdot P_{ir}$$

$$\tau_d = \frac{P_{ir}}{\omega_c}$$

(a) Ex 4.6 (322)

$$P_{is} = 60 \text{ kW}$$

$$s = 0.03 = \frac{3}{100}$$

$$P_{\text{loss-stator}} = 1 \text{ kW}$$

$$P_{ir} = 60 - 1 = 59 \text{ kW}$$

$$P_{rc} = s P_{ir} = \frac{3}{100} \times 59 = 1.77 \text{ kW}$$

$$P_m = P_{ir} - P_{rc}$$

$$\Rightarrow P_m = 59 - 1.77 = 57.23 \text{ kW}$$

(a) 4.8 (323)

440V, 50Hz, 6 pole, 3- ϕ , $P_{is} = 80$

rotor. emf $\rightarrow 100$ alternations/min $= \frac{100}{60} \text{ Hz}$

$$f_r = \frac{100}{60} \text{ Hz}$$

(a)

Slip

$$f_r = s \cdot f_o$$

$$\Rightarrow s = \frac{50}{100} \times 60 =$$

$$\Rightarrow s = \frac{100}{60 \times 50} = \frac{1}{30}$$

(b)

Rotor Speed

$$N_s = \frac{120(50)}{6} = 1000$$

$$N_r = (1-s) N_s = \left(1 - \frac{1}{30}\right) (1000)$$

$$\Rightarrow N_r = 966.7 \text{ rpm}$$

$$(c) P_{\text{mech-develop}} = P_{\text{ir}} - P_{\text{rc}} = (1-s)P_{\text{ir}}$$

$$P_{\text{rc}} = \left(\frac{1}{30}\right)(80) * 10000 \text{ W} (s \cdot P_{\text{ir}})$$

$\leftarrow 2667 \text{ W}$

$$P_{\text{m}} = (1-s)P_{\text{ir}}$$
$$= 77333 \text{ W}$$

(d) Rotor copper loss / phase

$$P_{\text{rc}} = (s)P_{\text{ir}}$$

$$\Rightarrow P_{\text{rc}} = \left(\frac{1}{30}\right)(80000)$$

$$\Rightarrow P_{\text{rc}} = 2667 \text{ W}$$

$$P_{\text{rc/phase}} = \frac{2667}{3} = 889 \text{ W}$$

(e) $R_{\text{r}} ; I_{\text{r}} = 65$

$$P_{\text{rc}} = I_{\text{r}}^2 R_{\text{r}}$$

$$\Rightarrow \frac{889}{65^2} = R_{\text{r}} \Rightarrow R_{\text{r}} = \underline{0.21 \Omega}$$

Torque in an IM

Power given in motor:

$$\begin{aligned}
 &= 3 E_{as} I_{sc} \cos \phi_c = 3 E_{as} \frac{V_{in} - I_{sc} R_r}{Z_{sc}} \\
 &= 3 \frac{E_{as}^2}{R_r^2 + (sX_m)^2} R_r \\
 &= 3 \left(\frac{s E_{as}^2}{R_r^2 + (sX_m)^2} \right) R_r
 \end{aligned}$$

$P_{me} = 3 I_{sc}^2 R_r$ (rotor copper loss)

$\Rightarrow P_{me} = 3 \left(\frac{s E_{as}^2}{R_r^2 + (sX_m)^2} \right) R_r$

$\Rightarrow P_{me} = 3 \left(\frac{s E_{as}^2}{R_r^2 + (sX_m)^2} \right) R_r = \frac{3}{2\pi n_s} P_{in}$

$\Rightarrow \frac{3 s E_{as}^2 R_r}{R_r^2 + (sX_m)^2} = T_d \cdot 2\pi n_s$

$\Rightarrow T_d = \frac{3 s}{2\pi n_s} \left[\frac{E_{as}^2 \cdot R_r \cdot s}{R_r^2 + (sX_m)^2} \right]$

$\Rightarrow T_d = K \cdot \left[\frac{s E_{as}^2 \cdot R_r}{R_r^2 + (sX_m)^2} \right]$ (Torque developed)

Starting torque

$s=1$
 $T_{st} = K \left[\frac{E_{as}^2 \cdot R_r}{R_r^2 + (X_m)^2} \right]$

$K = \left(\frac{3}{2\pi n_s} \right)$

$T_{st} \propto E_{as}^2$ (i.e. E_{in}^2)

Starting torque is proportional to the square of input voltage to stator.

Developed Torque (T_d)

$T_d = \frac{P_{me}}{\omega_{sc}}$ (mechanical power developed / mechanical angular velocity of rotor)

But: $P_m = (1-s) P_{in}$
 $\omega_{sc} = (1-s) \omega_s$

So: $T_d = \frac{P_{in}}{\omega_s} \rightarrow$ constant $\Rightarrow \left[\frac{P_{in}}{\omega_s} \right]$

$\Rightarrow T_{dmax} = \frac{P_{in}}{\omega_s} = \frac{P_{in} - \text{rotor copper loss}}{\omega_s}$

Maximum Torque

$\frac{d[T_d]}{ds} = 0 \Rightarrow T_d = \frac{K E_{as}^2 R_r}{R_r^2 + (sX_m)^2}$

$\frac{dT_d}{ds} = 0 \Rightarrow \left[\frac{R_r (R_r^2 + (sX_m)^2) - 2s^2 X_m^2 R_r}{R_r^2 + (sX_m)^2} \right] = 0$

$\Rightarrow 0 = R_r^2 + s^2 R_r X_m^2 - 2s^2 R_r X_m^2$

$\Rightarrow s^2 R_r X_m^2 = \frac{R_r^2}{R_r}$

$\Rightarrow R_r = s X_m$

$R_r = X_m$ ✓

$T_{dmax} = \frac{K'}{2 X_m}$

Torque @ Starting

$R_r = s X_m = X_m$ (i.e. $s=1$)

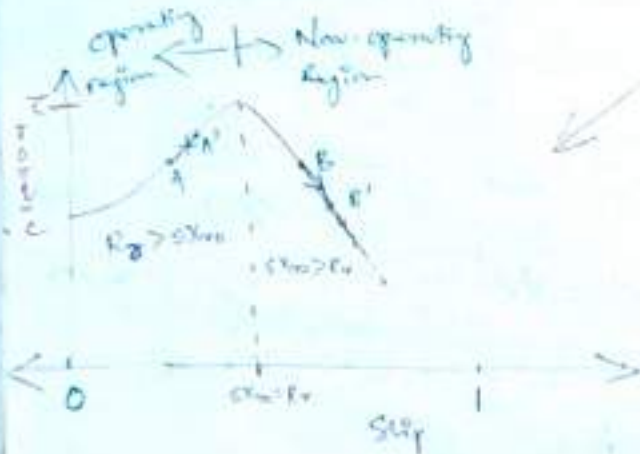
$R_r = X_m$ ✓

So: $T_{dmax} = K' \left[\frac{s \cdot R_r}{2 R_r^2} \right] = \frac{K' \cdot s}{2 s X_m}$

$$T_{max} = \frac{K (E_m)^2}{2 X_m}$$

Conclusion:
 (i) T_{max} is independent of the " R_r "

(ii) $T_{max} \propto \frac{1}{X_m}$



Slip $\uparrow \rightarrow$ Speed $\downarrow \rightarrow$ motor slows down

Ⓐ

If load increases \rightarrow slip increases
 operating point moves to A
 As a result, torque increases

Load $\uparrow \rightarrow$ Slip $\uparrow \rightarrow$ Speed $\downarrow \rightarrow$ Torque \uparrow

applied torque \leftarrow Speed $\uparrow \leftarrow$

Ⓑ

If load $\uparrow \rightarrow$ slip $\uparrow \rightarrow$ motor slows down
 Torque \downarrow
 Breakdown \leftarrow Slip $\uparrow \leftarrow$ Speed \downarrow

* Torque - slip & Torque - Speed

We have;

$$T = \frac{K s R_r E_m^2}{R_r^2 + s^2 X_m^2}$$

If R_r & X_m are constant
 then T varies with s
 $T-s$ curve has three regions

- (i) Low-slip (ii) High-slip
- (iii) Medium-slip

(i) Low-slip ($s \ll 1$) ($R_r \gg s X_m$)

$$T = \frac{K s R_r E_m^2}{R_r^2} = \frac{K' s}{R_r}$$

$$\Rightarrow T \propto s \propto \frac{1}{s} \quad (\because R_r \text{ \& } E_m \text{ are constant})$$

$T \propto s$
 straight line curve (linear operation)

(ii) High-slip ($s \gg 1$) ($R_r \ll s X_m$)

$$T = \frac{K' s R_r}{s^2 X_m} = \frac{K'}{s}$$

$$T \propto \frac{1}{s}$$

inversely proportional

(iii) Medium-slip

The graph shows curve change
 this curve @ $R_r = s X_m \mid T_{max}$
 also called pull-out torque / breakdown torque

Ex-4.13

$R_r = 0.05 \Omega$
 $X_{ro} = 0.2 \Omega$

Find :- 'Rest' for T_{max} stability

DE

T_{max} condition

$R_r = s X_{ro}$

$\Rightarrow 0.05 = \frac{0.2}{s} \quad @ \quad s = 1 + j \quad \& \quad s = 1$

$\Rightarrow R_{est} = 0.2 - 0.05 = 0.15 \Omega$

Full load torque & maximum torque

$T_{FL} = \frac{K_s K_r E_{ro}^2}{R_r^2 + (s X_{ro})^2}$

$T_{max} = \frac{K_r E_{ro}^2}{2 X_{ro}}$

At stability, $s = 1$

$T_{st} = \frac{K_r R_r E_{ro}^2}{R_r^2 + X_{ro}^2}$ (Next page derivation)

$\frac{T_{FL}}{T_{max}} = \frac{2 s s_m}{s^2 + s_m^2}$

$\frac{T_{st}}{T_{max}} = \frac{2 s_m}{1 + s_m^2}$

$\frac{T_{st}}{T_{FL}} = \frac{s^2 + s_m^2}{s(1 + s_m^2)}$

$\frac{T_{FL}}{T_{max}} = \frac{2s(R_r^2 + X_{ro}^2)}{R_r^2 + (sX_{ro})^2} = \frac{2sX_{ro}K_r}{R_r^2 + (sX_{ro})^2}$

But: $R_r = s_m X_{ro}$

$\frac{T_{FL}}{T_{max}} = \frac{2sX_{ro}K_r}{s_m^2 X_{ro}^2 + s^2 X_{ro}^2} = \frac{2s s_m}{s_m^2 + s^2}$

$\frac{T_{FL}}{T_{max}} = \frac{2s s_m}{s_m^2 + s^2}$

$\frac{T_{st}}{T_{max}} = \frac{2s_m}{s_m^2 + 1}$

Ex-4.14 6 pole, 50Hz
 $s_m = 4\% = 0.04$
 $Z_{ro} = (0.01 + j0.05) \Omega$

Find $T_{st} = f(T_{FL})$?

Speed (N_m) = ?

$N_s = \frac{120(50)}{6} = 1000 \text{ rpm}$

$s_m = \frac{N_s - N_m}{N_s} = \frac{1000 - N_m}{1000}$

$\Rightarrow (0.04)(1000) = 1000 - N_m$
 $\Rightarrow N_m = 960 \text{ rpm}$

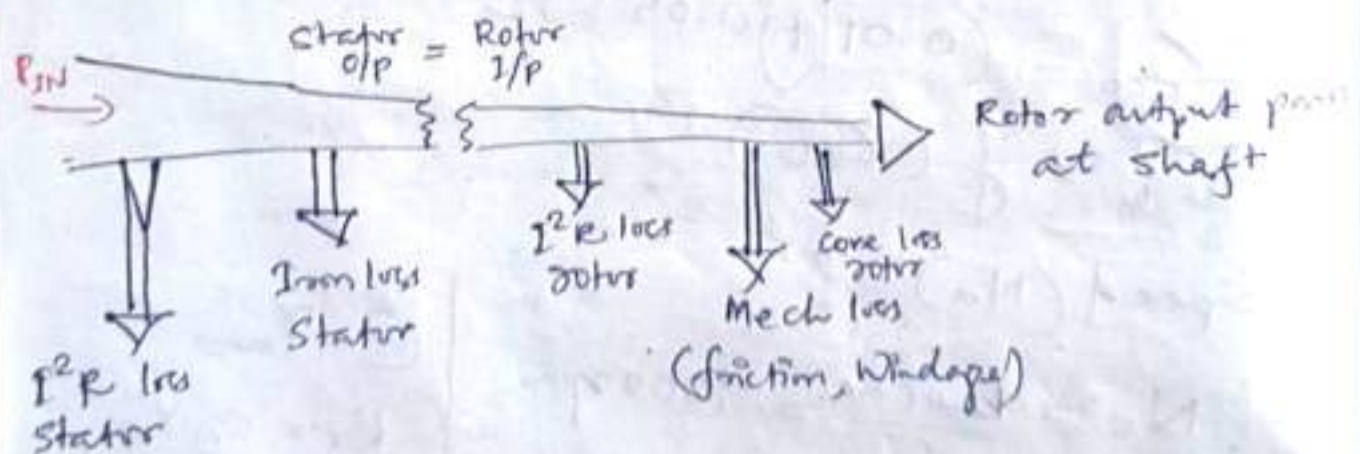
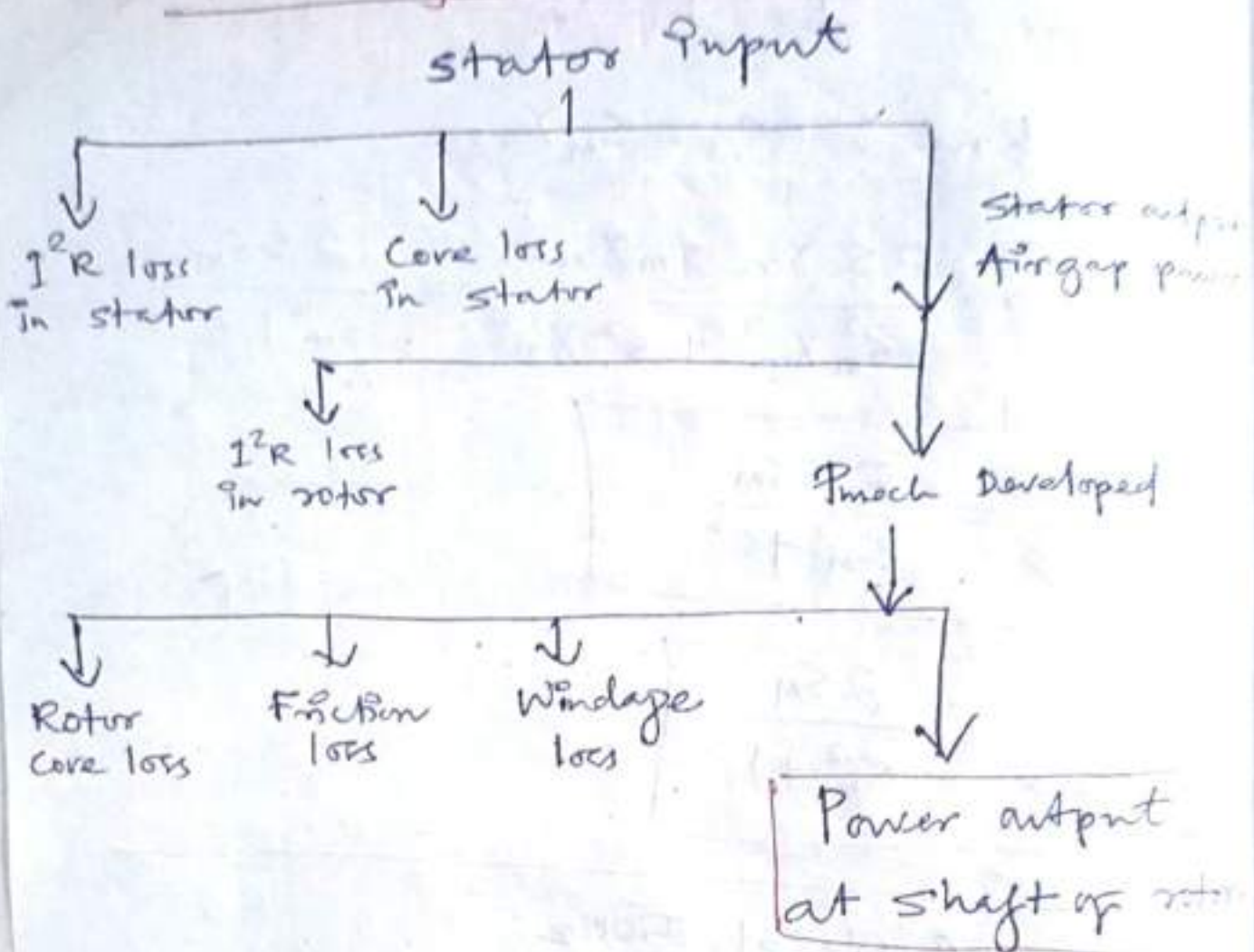
@ T_{max}
 $R_r = s_m X_{ro}$
 $\rightarrow \frac{0.01}{0.04} = s_m$
 $\rightarrow s_m = 0.2$

$\frac{T_{FL}}{T_{max}} = \frac{2s s_m}{s^2 + s_m^2}$

$T_{FL} = \frac{2(0.2)(0.04)}{0.04 + 0.0016} T_{max}$

$\Rightarrow T_{max} = 2.6 T_{FL}$

* Power flow in IM



Starting of IM

(a) $N_s = 0 ; s = 1$

EMF $\uparrow \rightarrow$ rotor current $\uparrow \rightarrow$ stator current \uparrow

Voltage drop in $\pi \leftarrow$ Voltage drop \uparrow
(V \downarrow)

That's why to limit I_{sc} ; different means are adopted ..

(1) DOL starting

\rightarrow Direct on line

\rightarrow For small IM upto 5kW.

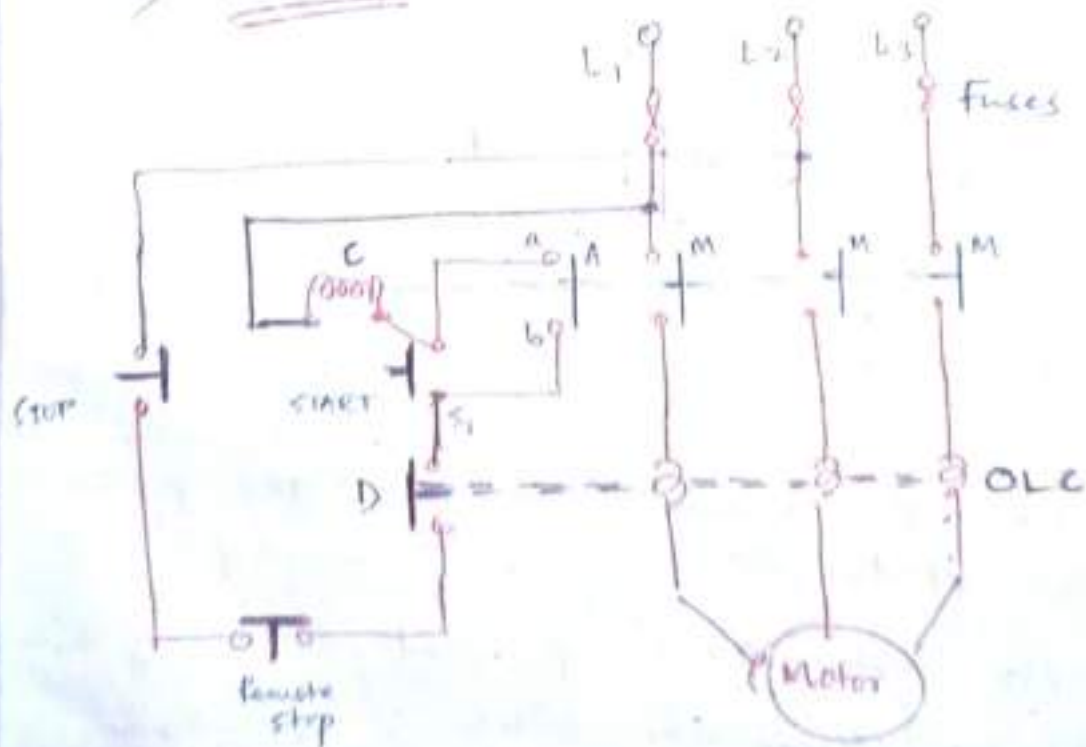
Push ON/OFF

Overload \rightarrow Bimetallic strip (thermal element)

Underload \rightarrow when power is not present

\rightarrow It doesn't require voltage in starting

\rightarrow Large inrush current flows @ starting.

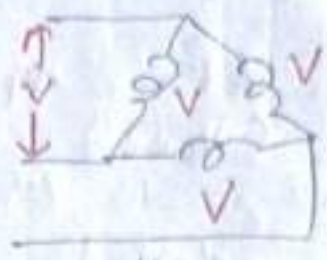
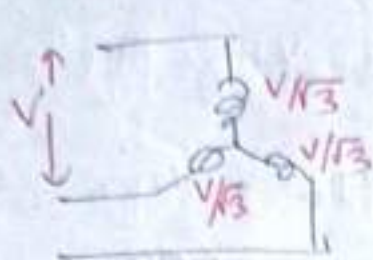


* Undervoltage protection - Below a certain voltage 'C' coil is demagnetized, motor disconnects

* Overload protection - OLC are energized during OL, and NC contact D to open & C de-energized, motor stop

② Y-Δ starter (Reduced voltage)

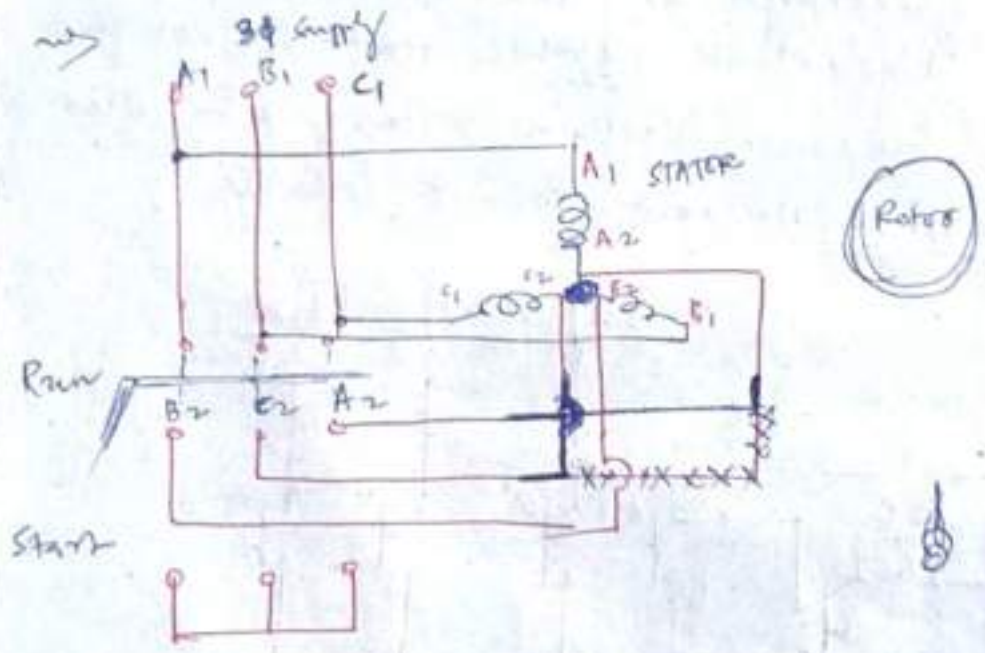
↓ ↓ α V ↓



$I_p = I_L / \sqrt{3}$

$I_p = I_L$

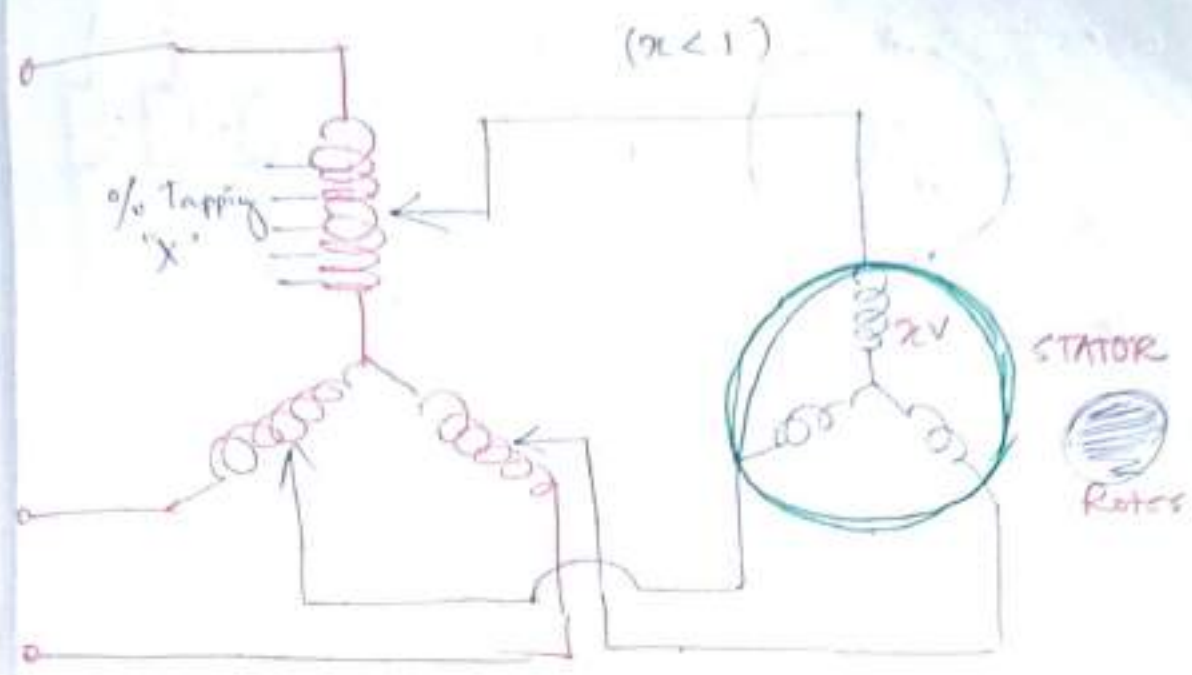
- Start as STAR & run as Δ
- At Y connection; $V \downarrow$ & I are reduced
- 57.7% • ($V_{ph} = V_L / \sqrt{3}$)



- When the switch S is in START position the stator windings are connected in Y
- When motor picks up speed; 80% of speed; change over switch S is thrown quickly to the RUN position; which connects stator winding in Δ.

$$\frac{T_{st}}{T_{FL}} = \left(\frac{1}{3}\right) \left(\frac{100}{100}\right)^2$$

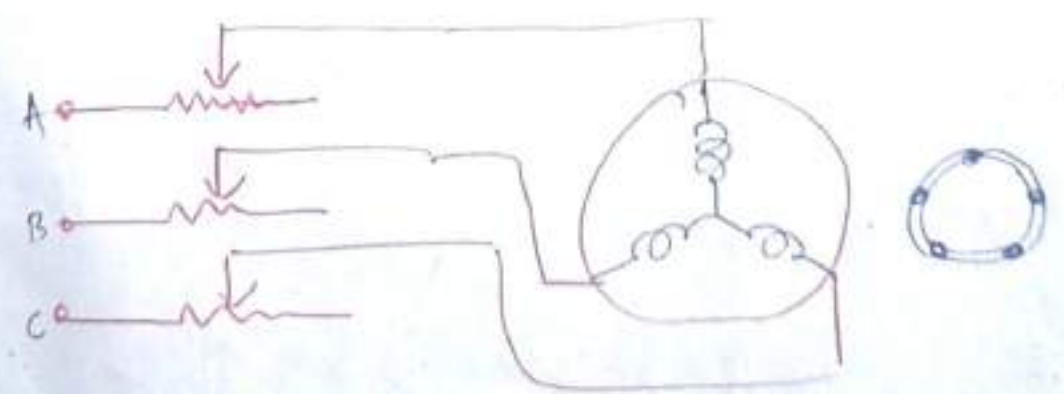
III Auto Transformer



- For large IM,
- It is efficient but expensive.
- It required suitable ϕ Auto Tf.
- The starting current of Torque is dependent on tapping.

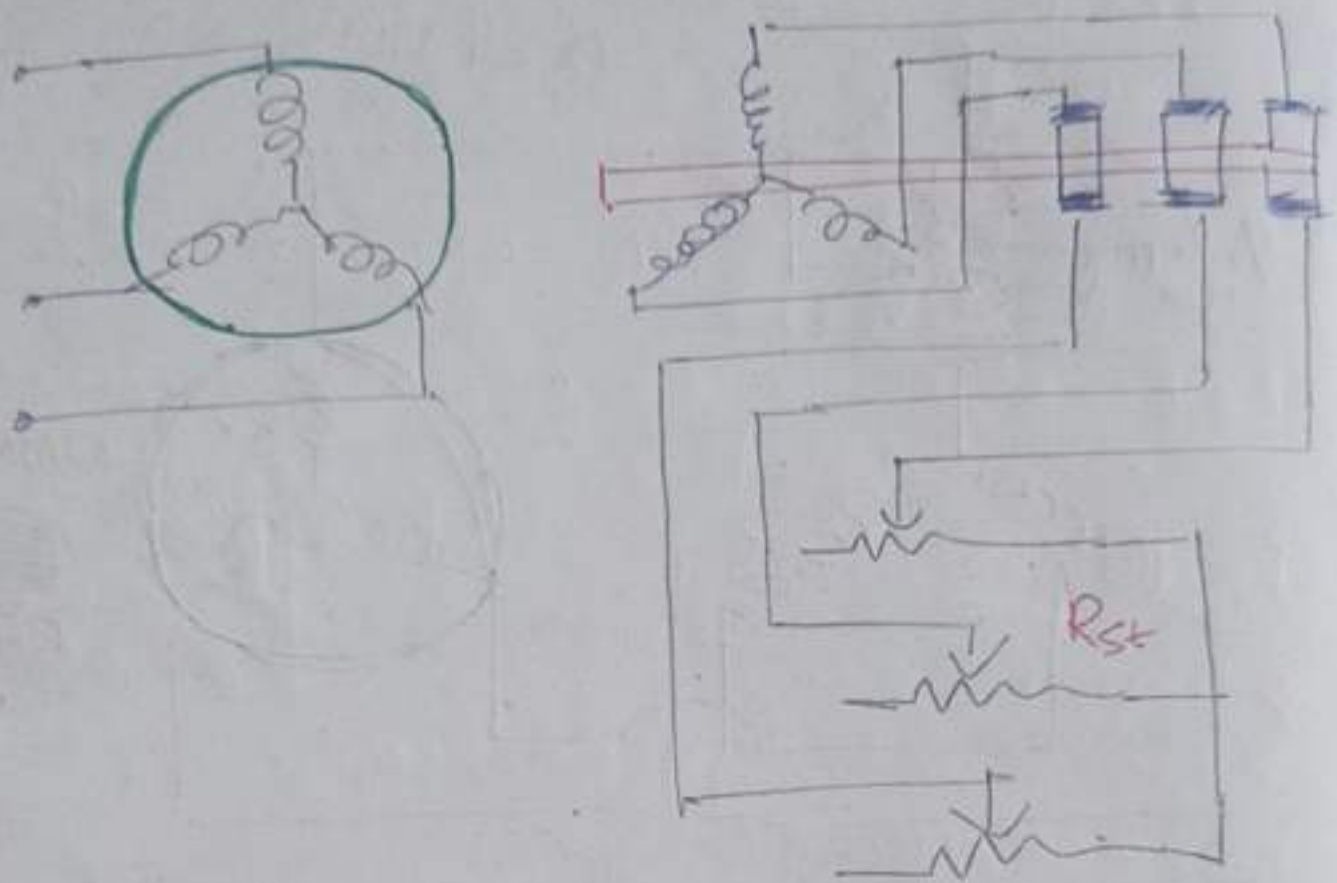
$$\left[\frac{I_{st}}{I_{FL}} = x^2 \left(\frac{I_{st}}{I_{FL}} \right)^2 S_{fl} \right]$$

IV Stator Rotor resistance by Starting



$\uparrow R \rightarrow \downarrow I_{sc} \rightarrow \Phi \downarrow \rightarrow E_{ind} \downarrow \rightarrow IR \uparrow$
 $\left(\frac{I_{sc}}{I_{FL}} \right)^2 S_{fl}$
 low N_s ; voltage drop $\uparrow \uparrow$ $E_{st} \downarrow$

* Rotor resistance starting



- R_{st} limits the I_{rotor} .
- T_{st} is increased ($\because R_{st} + R_r = X_r$)
- High starting torque application like TRACTION.

Speed Control of IM

$$N_s = (1-s) \frac{120f}{P} = f(s, P, f)$$

① Pole changing

Ⓐ Multiple stator winding

Two separate windings are provided on stator for two diff pole numbers.

One winding is energized at a time.

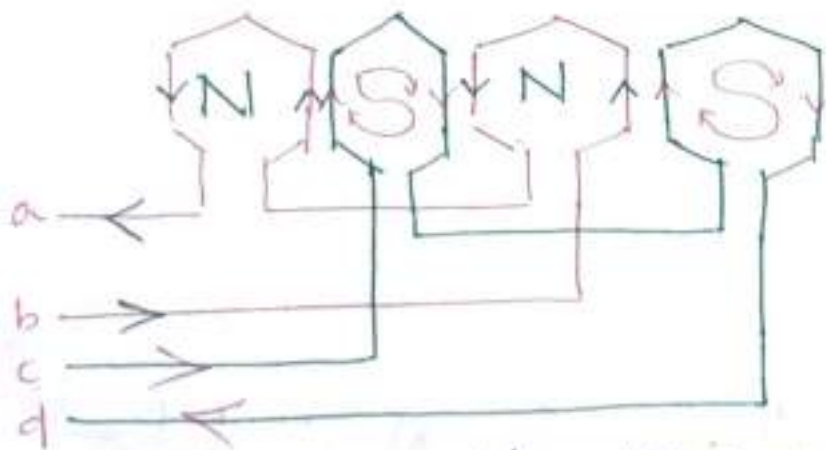
Ex - 6 pole & 4 pole.

@ 5% slip.

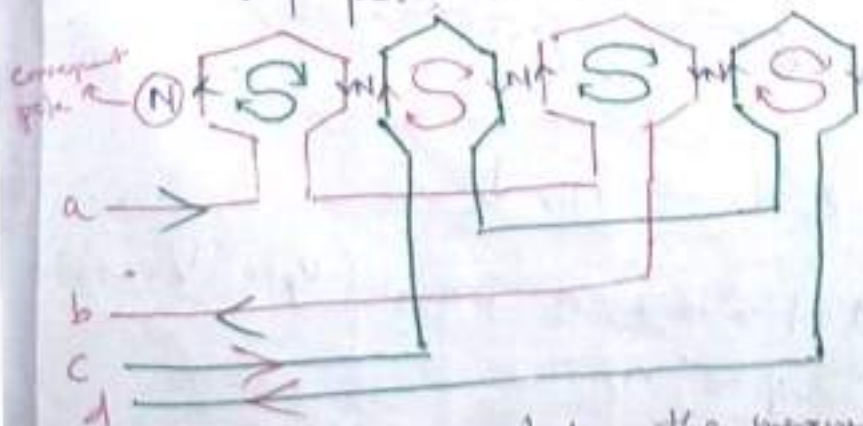
950 rpm, 1425 rpm.

→ This method is less η & costly.

Ⓑ Method of consequent pole -



4 pole $\rightarrow N_s = 1500 \text{ rpm}$



Reversing 'a-b'

In order to complete the magnetic path, the flux of the pole group must pass through the space between the groups, thus inducing magnetic

pole of opposite polarity (i.e. S).
 These induced poles are called consequent
 pole.

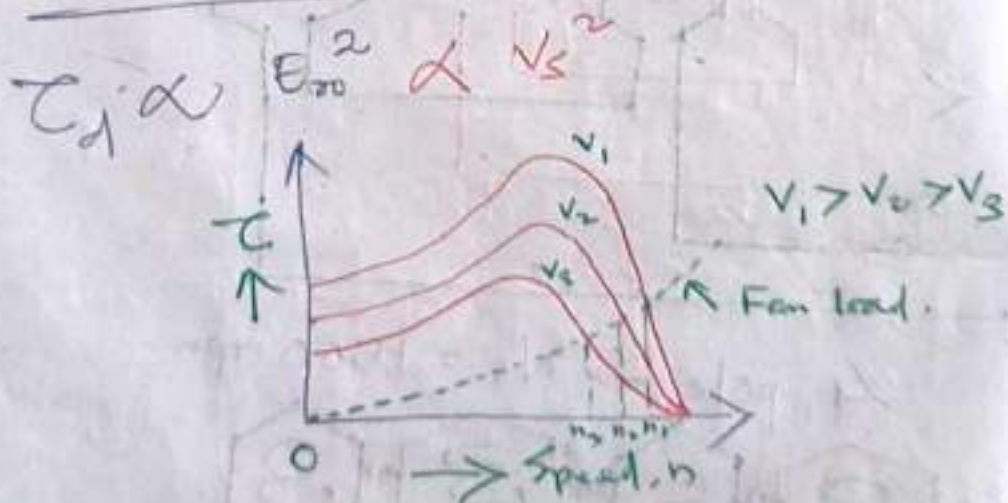
$$N_s' = \frac{120 \times 50}{8} = 750 \text{ rpm (Half speed)}$$

2:1 speed ratio is possible

(c) Pole amplitude modulation -

Speed ratio other than 2:1.

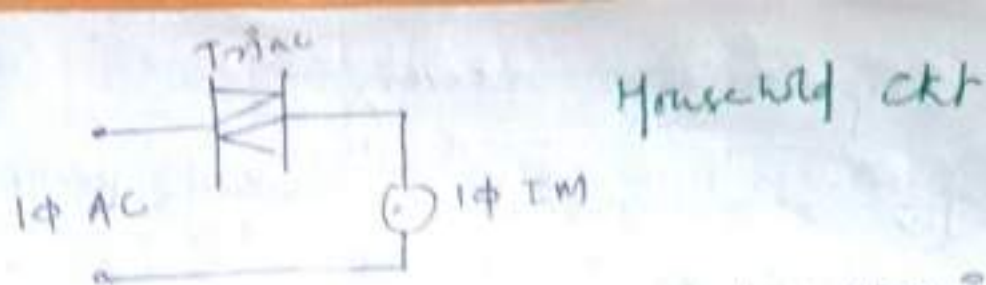
(II) Stator voltage control



$$V \downarrow \rightarrow T \downarrow \rightarrow n_s \downarrow$$

Speed control within a range (upto V_{rated})

" Δn_s upto n_s "



Speed control is obtained by varying firing angle of the triac.

III Variable frequency control

$$N_s = \frac{120f}{P}$$

$\frac{V}{f}$ ratio is maintained constant.

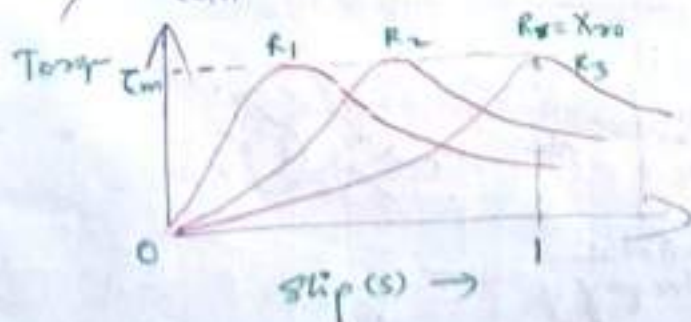
$E = 4.44 \phi f T$ * Variable voltage & variable frequency source is required.

- (A) Voltage Source Inverter } DC to AC (df/dv)
- (B) Inverter } DC to AC (df/dv)
- (C) Cyclo converter } AC to AC (df)

IV Rotor resistance control

→ For only wound IM

→ Rext is connected to rotor high slip ring.



$$R_1 < R_2 < R_3$$

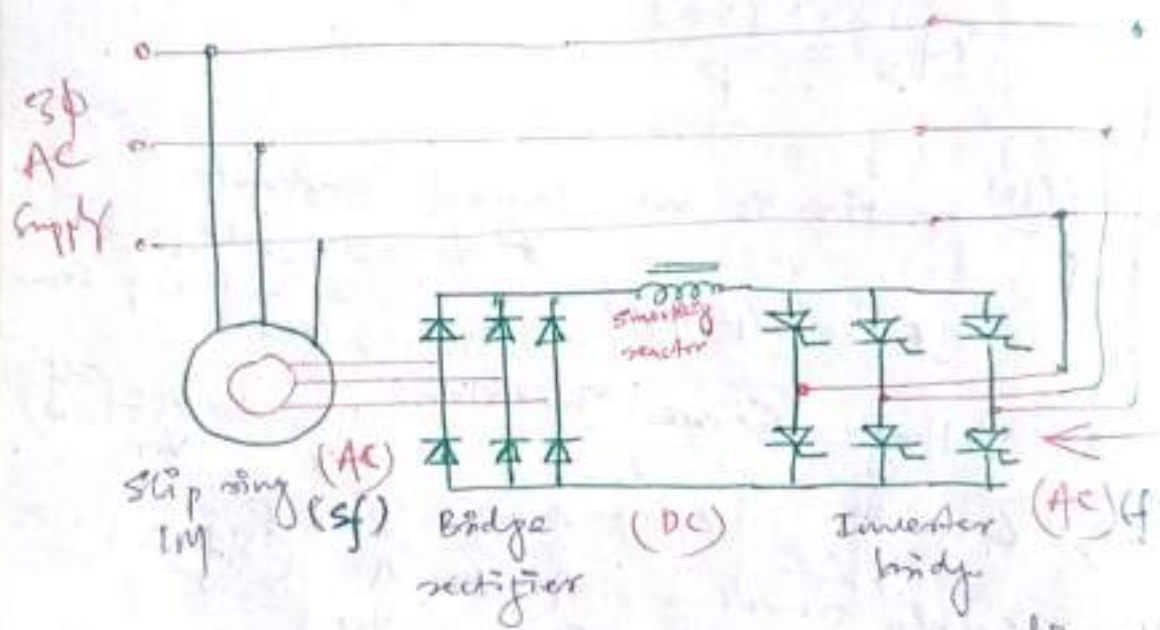
$$\uparrow R_r = \uparrow s X_{ro} \quad | \quad @ \quad T_{max}$$

speed ↑
(Upto No-load)

⑤ Slip - ~~energy~~ ^{power} recovery

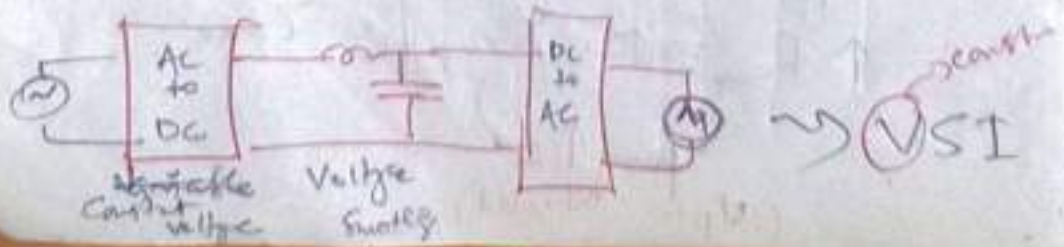
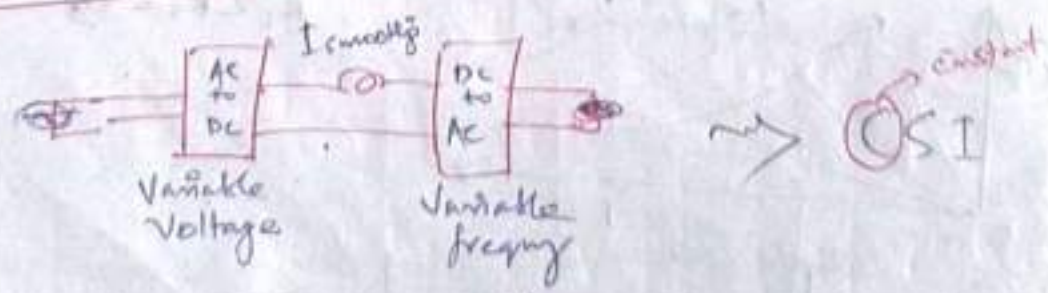
- In rotor resistance method power is wasted as I^2R loss
 - efficiency decreased.
 - If slip power is recovered from rotor ckt; $\eta \uparrow$
- "SCHERBIOR drive";

- (A) Additive (2 π)
- (B) Subtractive (2 π)



- Why not rotor power is directly connected to supply.
- Bcz it has 'sf' frequency

Variable frequency drives



Plugging

- It is a method of braking of IM.
- Reversing the phase sequence of 2 phase terminals across stator in running motor.



- The rotor want to rotate in opposite direction due to which it come near 0 speed where an adequate mechanical braking is applied otherwise there is a possibility that motor rotate in reverse direction.

- Relative Speed = $N_s + N_r$
High induced emf → ↑↑ I_{rotor}
- Temperature rise ↑↑ → need to be withstand by IM.

* Type of motor - Enclosure

① Open drip proof (ODP)

→ Allow air to circulate through motor for cooling.

→ Prevent drop of liquid/dirt falling into motor when 15° angle from vertical.

→ Indoor application
[clean, dry loads]



② Total enclosed, fan cooled (TEFC)

→ Air ventilation is prevented from both inside & outside of frame.

→ A fan is attached to the shaft to pull air over the frame during this operation.

Ex - pump, fan, compressor, industrial drive
(Most versatile)

③ Total enclosed non-ventilated (TENV)

→ No cooling fan is provided.

→ No opening vent; tightly enclosed but not air tight.

Ex - suitable for "dirt & dampness" ^{through motor frame}

④ Total enclosed Air over (TEAO)

→ Direct sight fan & blower duty motor
→ Motor must be mounted above the surface of the fan
→ Air flow over the fan

⑤ Explosion proof enclosure (EXPL)

→ Totally enclosed machine
→ Design to withstand explosion of gas & vapour inside machine, not prevent
Ex - branch containing hazardous gas or dust.

⑥ Hazardous location (HAZ)

Class I: Chemical, Wax, Acetone, Acrylic, Benzene, Ethanol, butane.

Class II: Al, Mg - dust
Carbon, coal - dust
Flour - dust

Induction Generator

Conditions of operation of IG:

- (i) Slip becomes negative
 $\therefore N_r > N_s$
- (ii) Prime mover torque is applied to the electric torque.

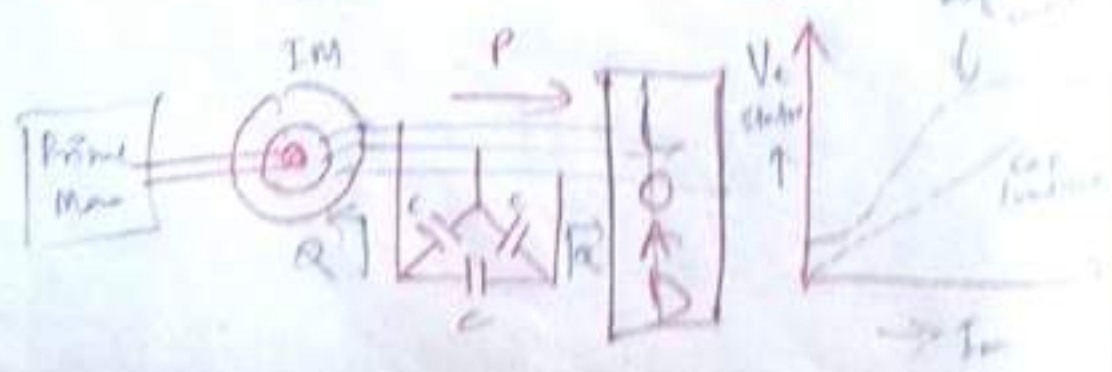
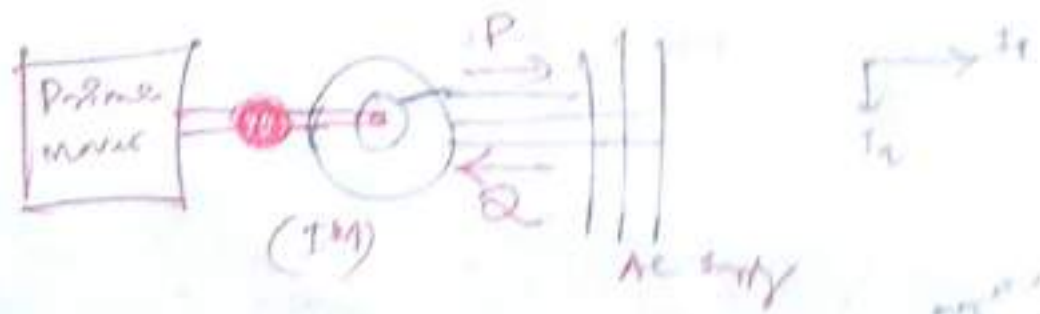
→ With external source; prime mover speed becomes greater than N_s
 $N_s \Rightarrow \frac{s}{(-ve)} = N_r - N_s$

→ It is also called asynchronous generator.

→ It is not self excited machine.

→ It requires (reactive power Q), to magnetize the stator.

→ It continuously requires Q for its so, ~~not~~ to make it self excited capacitor bank is used.



Application

- ① Wind turbine (Variable wind speed)
- ② Hoist

Advantage

- ① No commutator, No brush arrangement
- ② Cheaper, ③ No need for synchronization is

Disadvantage

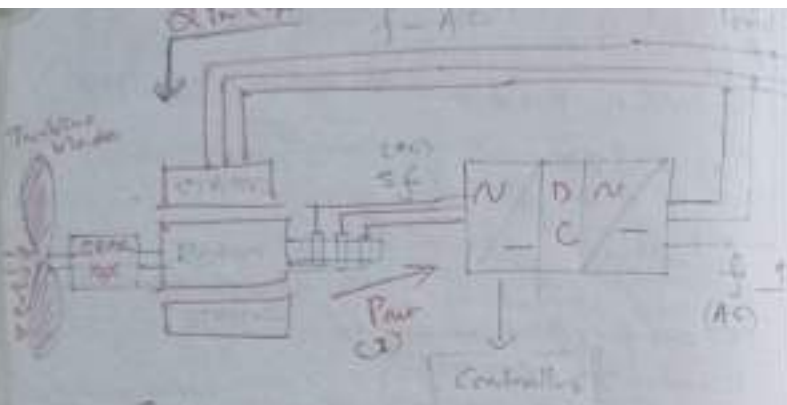
It requires large ϕ from the supply

Why Over excited ~~of~~ Alternator is called Synchronous condenser?

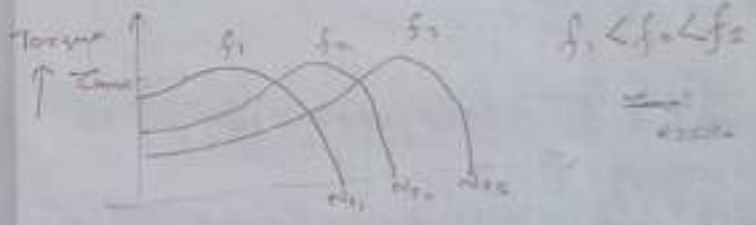
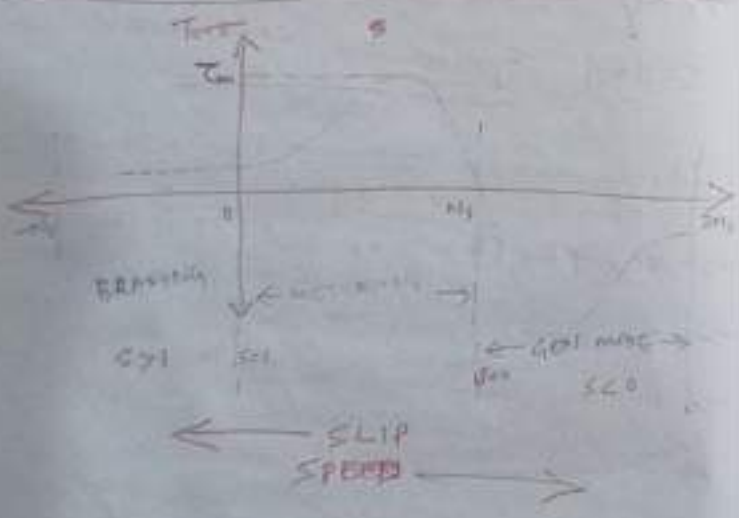
Mech Energy $\xrightarrow{\text{Mag flux}}$ Electrical Energy

- The flux is nothing but reactive power
- It comes from the alternator field.
- If less reactive power excitation is given, the M/c draws reactive power from the system.
- If large excitation is given, the excess reactive power is supplied to system.

$(\phi \propto I_f)$ magnetizing current



(Wind Turbine)



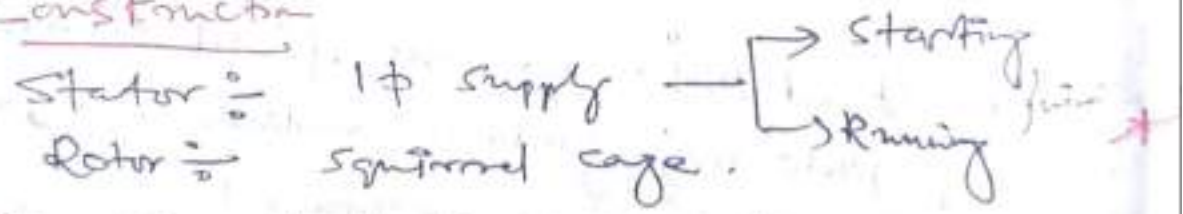
Torque-Speed ω

SINGLE-PHASE IM

① Working principle

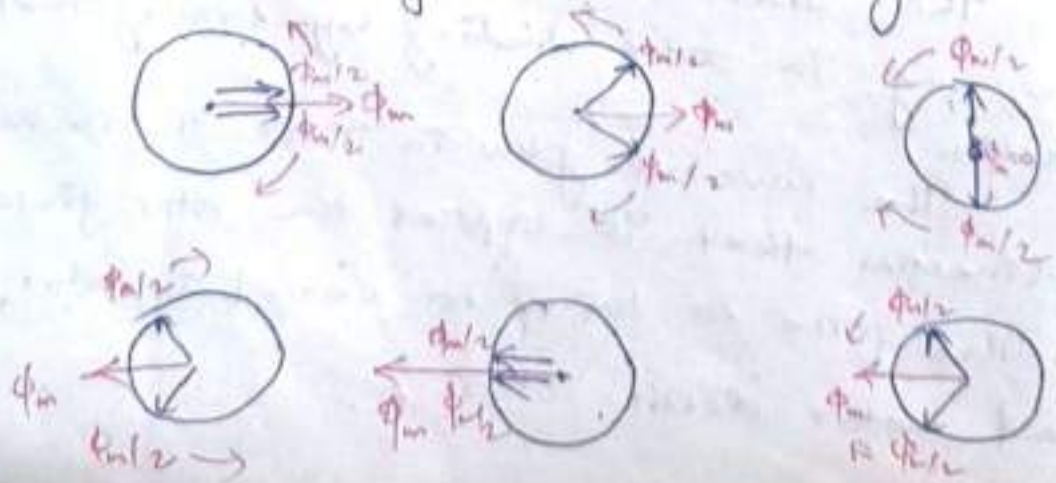
- When the stator of a 1 ϕ IM is fed with 1 ϕ supply it produces alternating flux in the stator winding.
- This changing alternating flux produces an emf in rotor bars according to Faraday's law of EML.
- Alternating flux unable to start motor.
- However, if rotor is given initial start by external force; then the motor accelerates to its rated speed.

④ Construction



② Double field Revolution theory

Any alternating quantity can be resolved into two components having magnitude half of the maximum value of the alternating quantity.

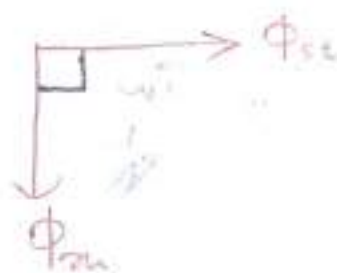
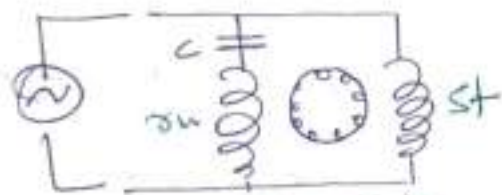


② Why 1 ϕ IM is not self starting?

Alternating flux acting on the S_f rotor can't produce rotation; only rotating flux can.

⑤ * How to make 1 ϕ IM self starting?

→ At starting; it is converted into 2 phase motor; by introducing additional "starting winding".



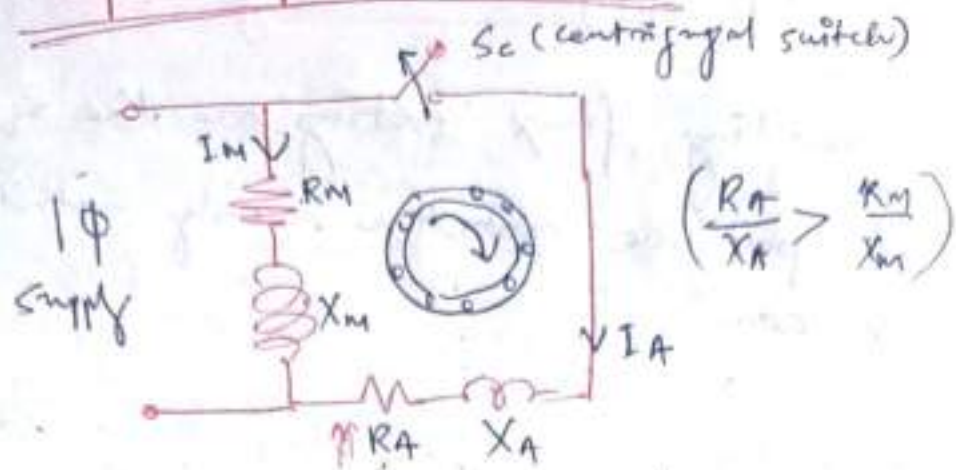
Ferraris's Principle

→ The two windings are connected in parallel across a 1 ϕ supply and are spaced 90° electrical degree apart.

→ Hence motor behaves like a 2 ϕ IM and stator produces revolving rotating magnetic field.

→ Once the motor gathers speed upto 80-90%; the starting winding is disconnected by the means of a centrifugal switch.

① Split-phase IM



→ Resistance start motor

→ Main & Auxiliary winding.

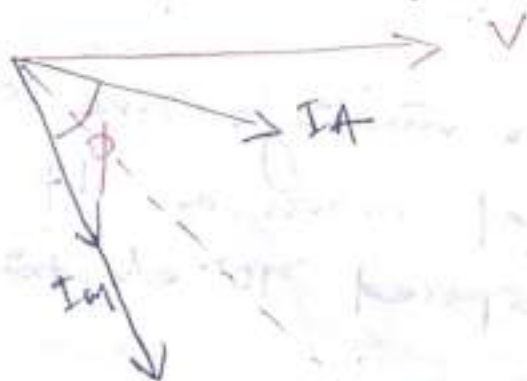
Main $R_M \ll R_A$

Main = Thicker

Auxiliary = Thin

I_A in phase with V_s ($\because R_A \gg X_A$)

→ I_M ~~is~~ ^{lags} phase lag ($\because X_M \gg R_M$)



→ The phase diff b/w two winding is 30° (not 90°)

→ Unequal current → unequal torque

$$\tau_{st} = 1.5 \text{ to } 2 \tau_{FL}$$

→ At 80% speed " S_C " disconnect I_M and motor rotate with main winding.



* Reversal of Direction

→ It can be reversed by reversing the connection of either main or starting winding.

→ the motor must be brought to rest for this purpose.

* Motor CS

$$\tau_{st} = 1.5 \tau_{FL}$$

$$\tau_{max} = 2.5 \tau_{FL} \text{ @ } N_0 = 0.75 N_s$$

$$I_{st} = (7 \text{ to } 8) I_{FL}$$

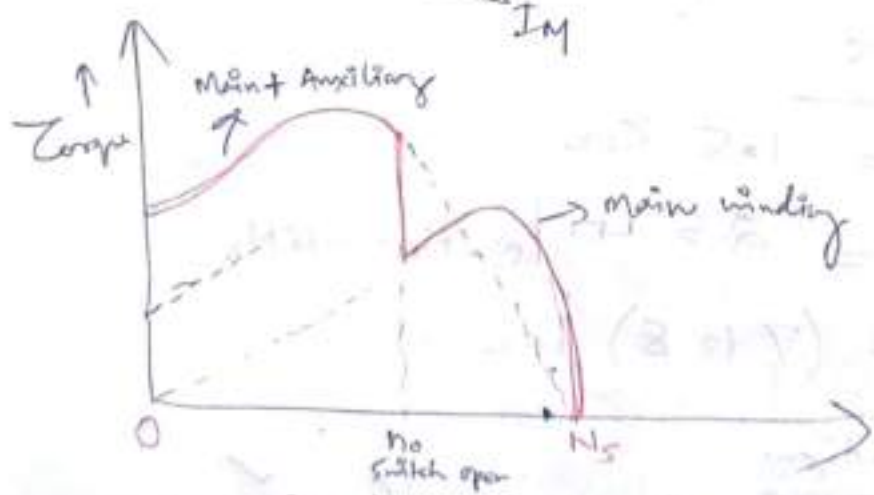
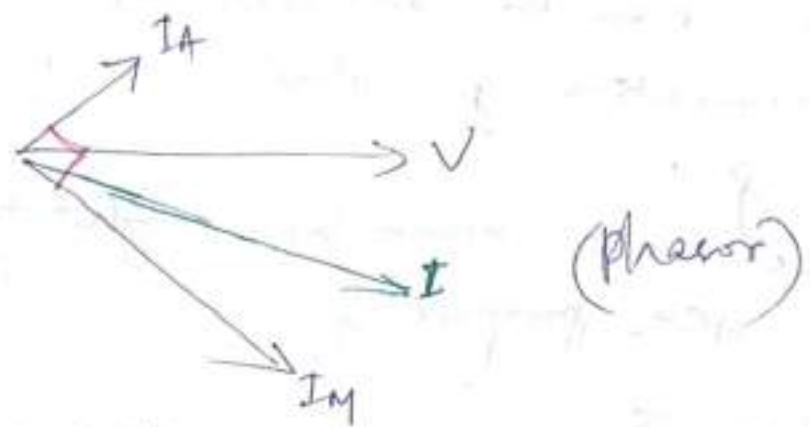
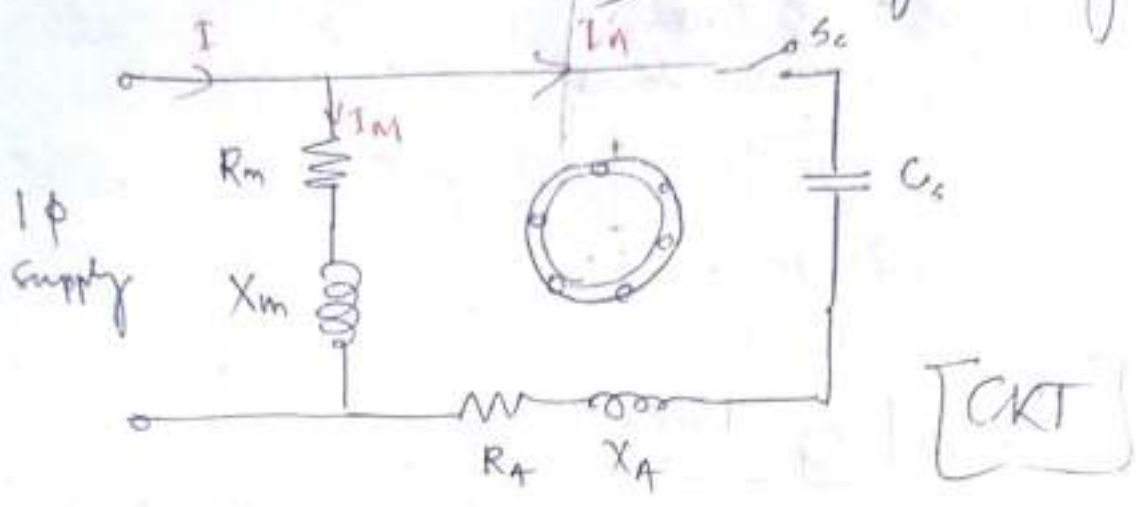
* Application

→ washing m/c, AC fan, food mixture floor polisher, blower, etc.

→ low starting τ_i so used for ^{load} up to 1 kW.

② Capacitor-start motor.

-> To produce greater phase diff between current in main & auxiliary winding.

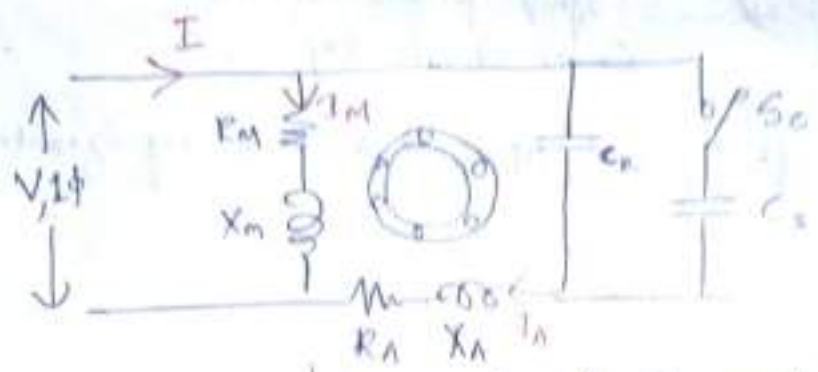


* Reversal of direction

⊙ Either one of the windings connection is reversed to get it done. Before that the motor brought to rest.

* High inertia load where frequent starts are required. Refrigerator, AC-compressor,

③ Capacitor Start - Run IM



→ For $Z_{st} \uparrow \rightarrow I_{sc} \uparrow$ is required.

$$X_c \downarrow = \frac{1}{\omega C_c \uparrow}$$

Start Run capacitor

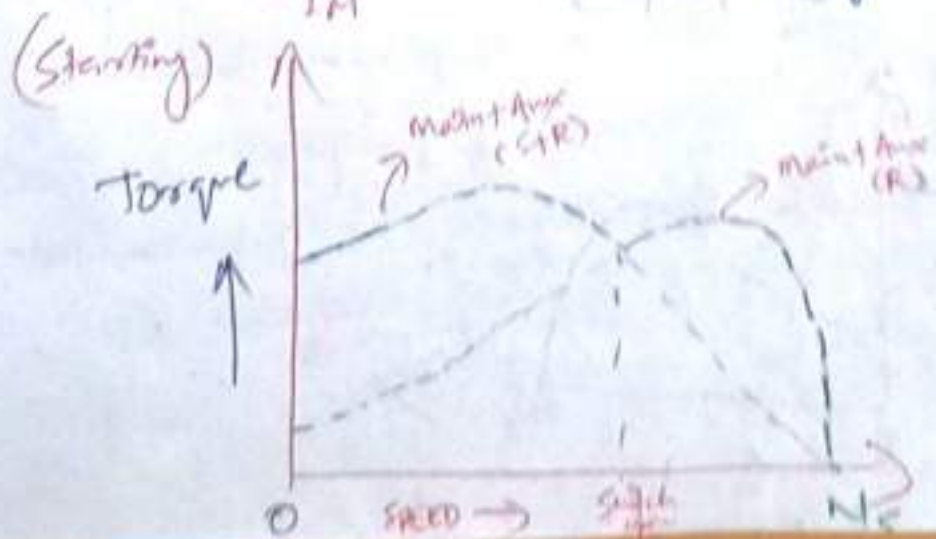
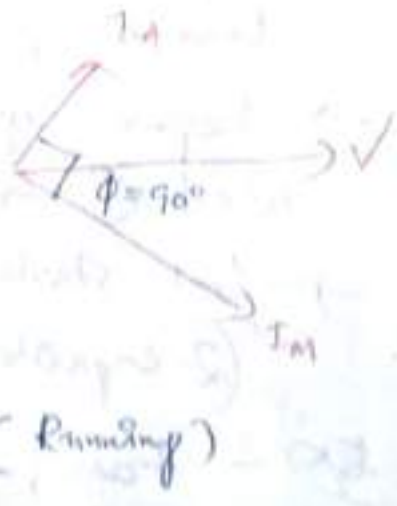
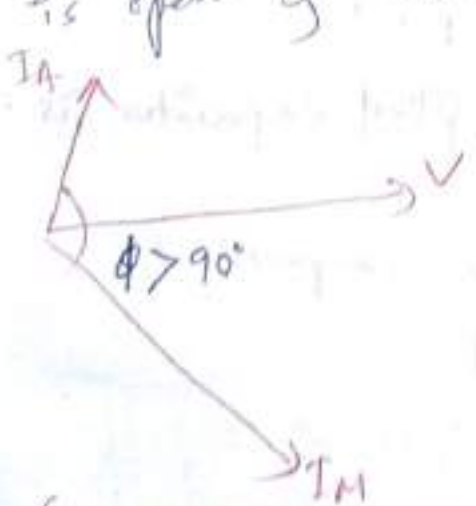
→ ~~Effect~~ During normal operation.

$$I_{rated} < I_{sc}$$

Electrically the cap

→ $\uparrow X_c = \frac{1}{\omega C_c} \downarrow \rightarrow$ long time constant (capacitor) paper S_c

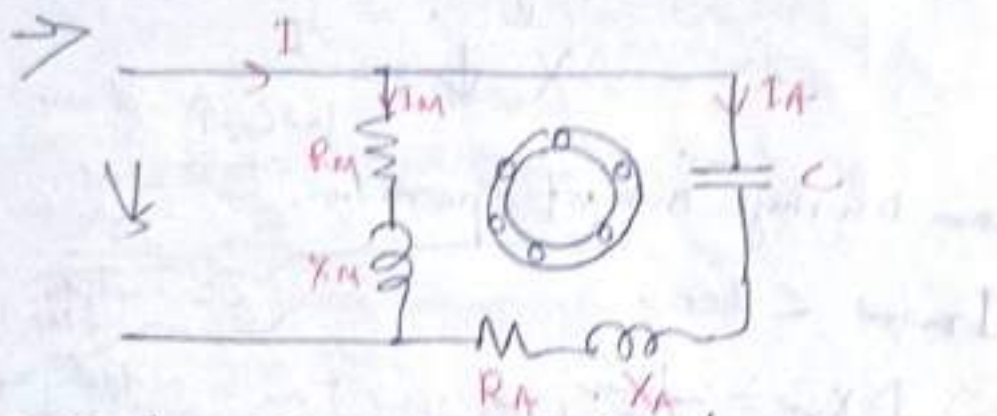
→ As motor approaches 90% Ns, S_c is open & C_c is disconnected.



- Quiet & smooth running.
- $\uparrow \eta$ than split phase or IM.
- Cap-start IM.

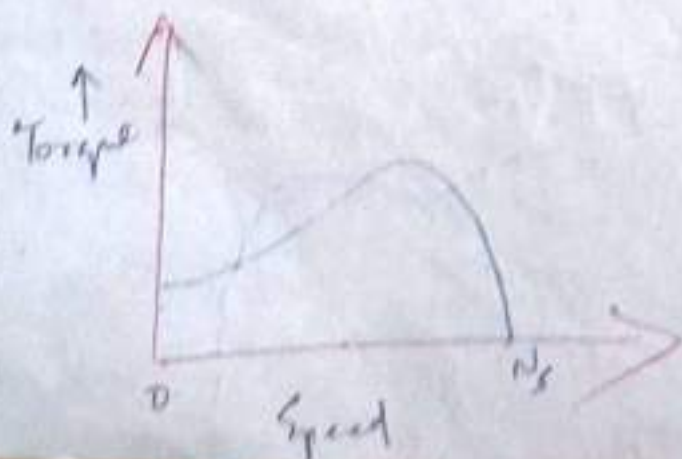
EX:- Pump, Air compressors, refrigerator.

(A) Capacitor-Run IM (Permanent split capacitor)



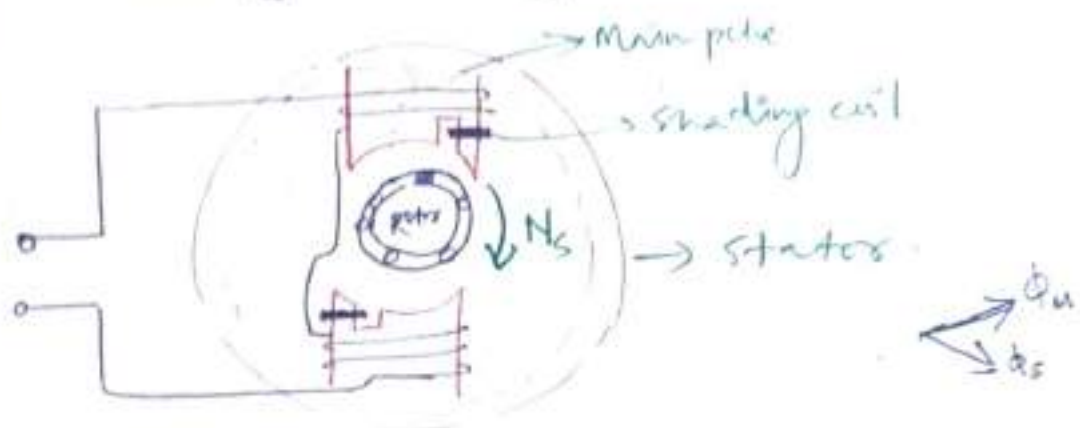
- No switch is required.
- Uniform torque.
- Less noisy during operation.
- Paper-spaced oil filled capacitor is used (Costly)
- Low starting torque compared to (2-capacitor IM)

EX - Fan, AC,

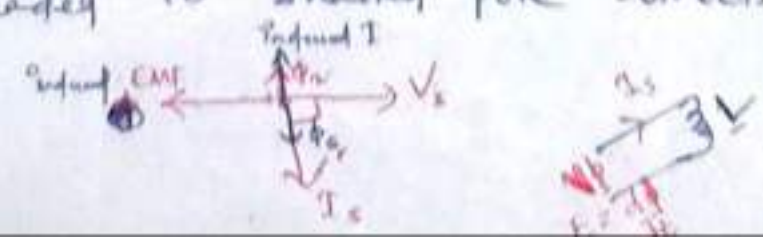


* Shaded pole IM

- Self starting 1 ϕ IM.
- Salient pole stator.
- Copper ring is fitted on the smaller part "a"; called shaded pole.
- Shading coil - single turn coil of copper



- Alternating flux produced in the stator core.
- A portion linked with ~~the~~ shading coil & emf is induced, induced current flows and produces a flux which is opposite to the main field flux.
- There is space & time displacement between the main pole & shading pole results in rotating magnetic field.
- As a result; Starting torque is produced developed on the rotor.
- The direction of rotation is from Non shaded to shaded pole direction.



→ reversal is not possible
shading pole.

Application

- cheap
- Z_{st} is low
- losses are high; $\therefore \eta \downarrow$.
- Small size motor upto "40kW"
- Ex - Relay, Table fan, exhaust fan, hair dryer.



START

- High current for T_{st}
- $$I_C = \frac{S}{V}$$
- (430-510) μF
- Voltage rating
- Larger size
($I_C = \frac{S \cdot 10^3}{V}$)

RUN

- medium current
- $$C = \frac{Q}{V}$$
- $5 \mu F - 45 \mu F$
- ϕ
 $V_{rating} = 1.5 V_{line}$
(peak voltage)
- maintain 90° phase delay.

SPECIAL ELECTRICAL MACHINE

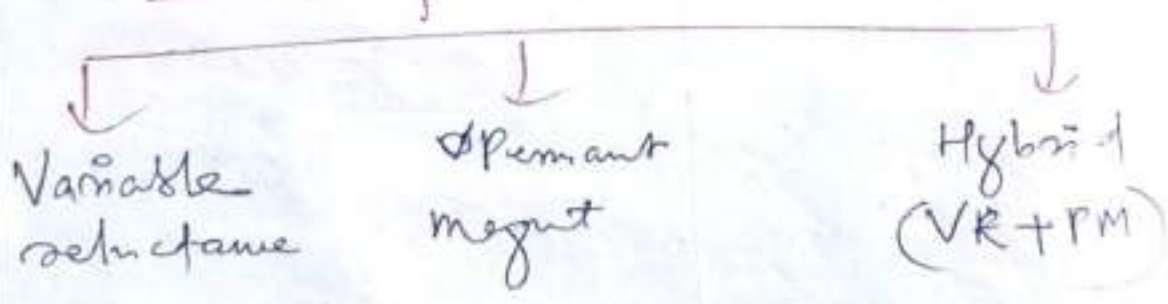
→ For control of speed & precise positioning.
* Principle of stepper motor - → Robotics
→ 2-D printing
→ Printing press

→ It has movement in discrete steps.
→ The angular rotation depends upon the nos of pulses fed into the control circuit.

→ Each input pulse initiate the drive circuit which produces one step of angular movement.

→ Solid state switch (FET, MOSFET, BJT) are used to energised & deenergised appropriate winding in required sequential manner.

* Classification of Stepper motor



* Variable Reluctance motor

It operate on the principle that, flux line occupy low reluctance path.

The stator and rotor get aligned in such a way that, the magnetic reluctance is low.

→ Iron is used for magnetic core of rotor

* Step Angle

The angle by which a stepper motor moves when one pulse is applied to the (input) stator.

$$\text{Resolution} = \frac{\text{Nos of Steps}}{\text{Nos of Revolution of rotor}}$$

Ex

High precision motor

1000 Step per revolution

i.e. - 0.36° step angle

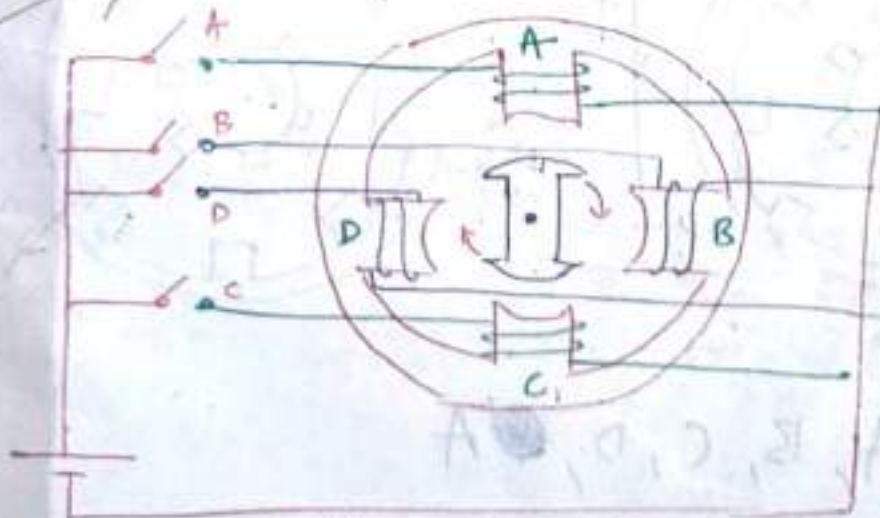
Standard motor

200 step per revolution

i.e. - 1.8° step angle

$$\alpha = \frac{360^\circ}{M_s N_s}$$

\rightarrow Nos of rotor pole
 \rightarrow Nos of stator phase.



[4/2 - pole]

8 Four phase - 2 pole VR Stepper motor

$$\alpha = \frac{360^\circ}{m_s N_r} = \frac{360^\circ}{4 \times 2} = 45^\circ$$

A, B, C, D, A \rightarrow 90° steps
clockwise rotation.

A, A+B, B, B+C, C, C+D, D, D+A, A \rightarrow 45° step

$$\alpha = \frac{N_s - N_r}{N_s N_r} \times 360^\circ \rightarrow 45^\circ$$

clockwise rotation

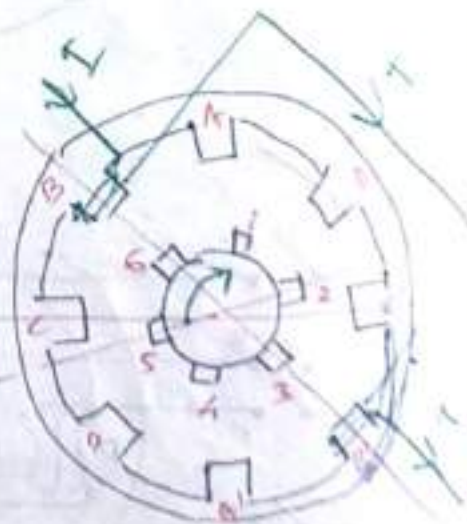
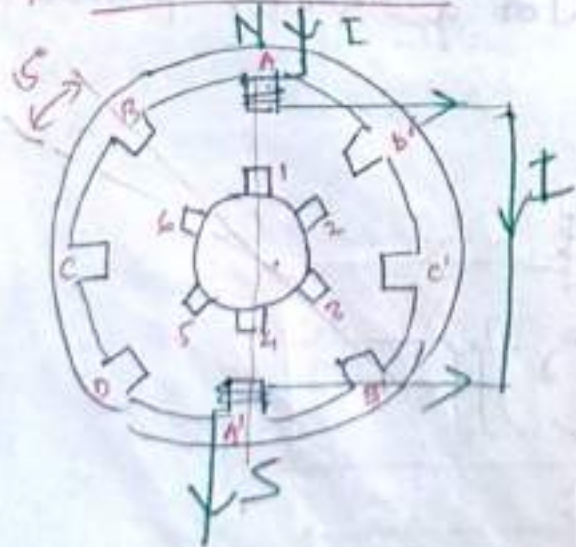
$N_s \rightarrow$ No. of stator pole

$N_r \rightarrow$ No. of rotor pole.

$$\alpha = \frac{360^\circ}{m_s N_r} \rightarrow 90^\circ$$

m_s = no. of stator phases

* 8 phase 6 pole



\rightarrow A, B, C, D, ● A

$$\alpha = \frac{8-6}{8 \times 6} \times 360^\circ = 15^\circ$$

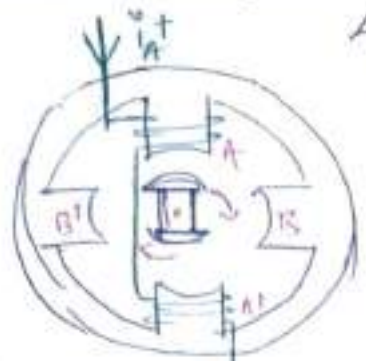
Disadvantage

\rightarrow Motor may drift from final position after supply is cut-off due to inertia.

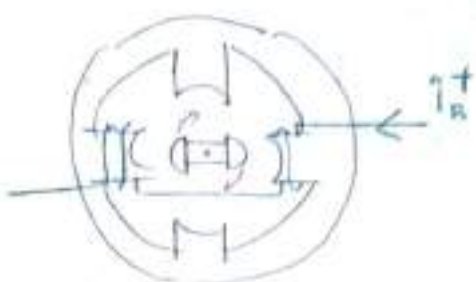
Permanent Magnet / Stepper motor

→ Detent torque (next page)

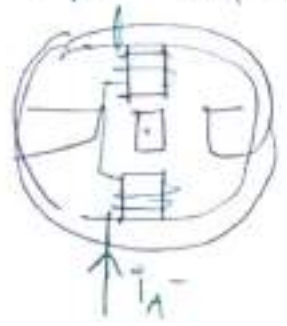
4/2 pole PM stepper motor



(A) $\alpha = 0^\circ$



(B) $\alpha = 90^\circ$



$\alpha = 180^\circ$



$\alpha = 270^\circ$

Phase winding sequence

$i_A^+ \ i_B^+ \ i_A^- \ i_B^+ \ i_A^+$ → Clockwise rotation

$i_A^+ \ i_B^- \ i_A^- \ i_B^+ \ i_A^+$ → Anti-clockwise rotation

Comparison

→ PM has higher inertia & lower acceleration than VR.

→ Pulse rate is 300 pulse/second - PM

1200 pulse/sec - VR.

→ PM produce more torque compared to VR.

Advantage

- ~~Step~~ → Detent torque
- High torque
- Better operation for start, stop & reverse
- More reliable.

Disadvantage

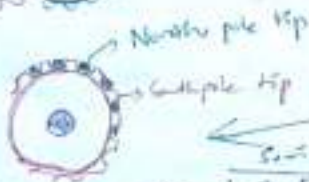
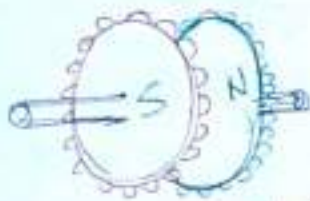
- low acceleration
- Slow work efficiently for step angle $30^\circ - 90^\circ$

Hybrid Stepper motor

* Detent Torque

In permanent magnet type motor, it prevent the rotor from drifting when machine supply is turned off.

→ IM of Hybrid stepper motor produce detent torque.



S_1-S_5
 pole 1, 3, 5, 7 → A phase
 pole 2, 4, 6, 8 → B phase
 A⁺ → 1, 5 → North
 3, 7 → South
 5 align with S-disk

B⁺ → 2, 6 → North
 4, 8 → South
 6 align with S-disk

A⁻ → 3, 7 → North

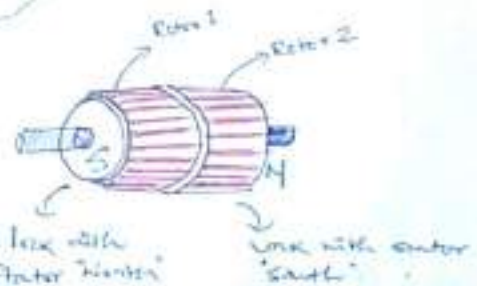
→ Hybrid motor is combination of variable reluctance & permanent type motor.

→ rotor is axially magnetized like permanent magnet stepper motor & stator is electro-magnetically magnetized like variable reluctance stepper motor.

→ Both stator & rotor are multi-toothed.

→ One end is axial as North pole & other end — as South pole.

→ Toothed rotor cup are placed on each end of the magnet, and the cup are offset by half of the tooth pitch.



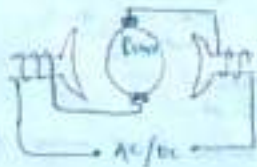
A⁺ supply :- 1, 5 North
 3, 7 South

So, 1-5 align with the rotor teeth of South polarity & 3, 7 align with the rotor teeth of North polarity

B⁺ supply :- 2, 6 - North & 4-8 South
Rotor 1 (South) align with 2-6 pole & Rotor-2 align with 4-8 pole.

Comparison

	Commutator	Reluctance	Hybrid
Step Angle	7.5° or large	1.8° or small	1.8° or small
Torque output	Moderate	Low	High
Detent torque	Yes	No	Yes
Pulse Rate / Speed	Low	High	High
Noise	Quiet	Loud	Quiet
Size	Yes	No	Yes
Design	Simple	Moderate	Complex



COMMUTATOR MOTOR

→ AC commutator motor has higher torque & higher speed than induction motor.
 → But not maintenance free as IM.

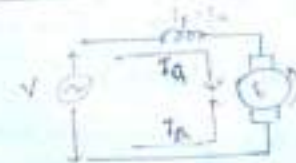
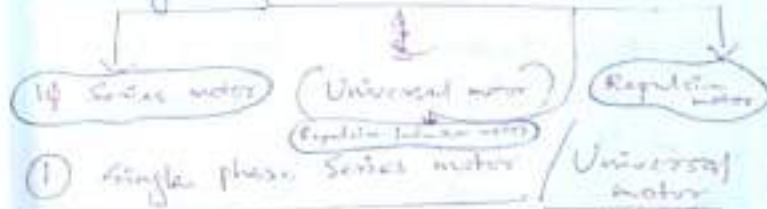
* Commutation

→ It is the process of converting AC current in armature winding into DC current after going through ~~the~~ commutator (in DC generator) (split ring & brush)

→ It is a rotating switch.



Classification



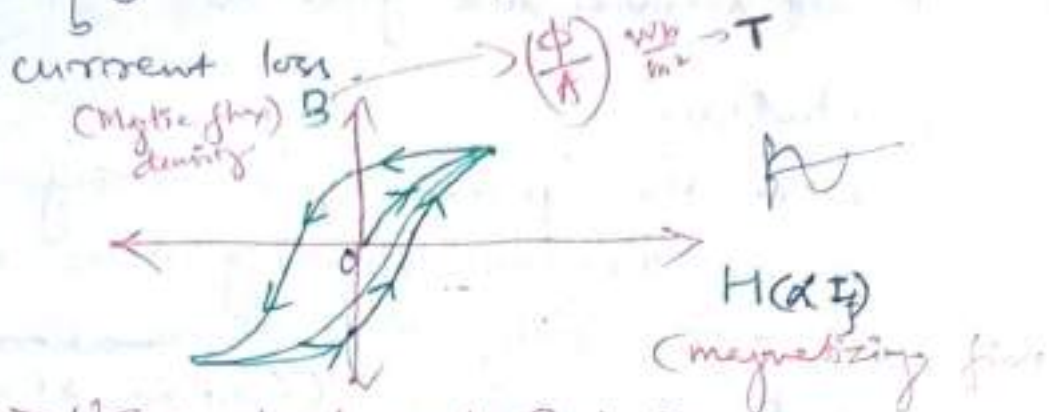
$$T = \phi I_a$$

→ By changing polarity, (I_a) or (ϕ) are reversed.
 ∴ Torque develops in same direction.
 → Motor continues to run in same direction.

So; series motor can operate on AC & DC.

Drawback when it is used with AC

① $\eta \downarrow$ due to hysteresis loss & eddy current loss



\rightarrow Using steel material in core.

• Eddy current

It produce due to relative motion between core & the magnetic flux.

Thin lamination of core stack together to reduce it.

② Power factor is low due to large reactance of the field & armature winding.

③ Sparking at brush is maximum (excessive)

Overcome these difficulties

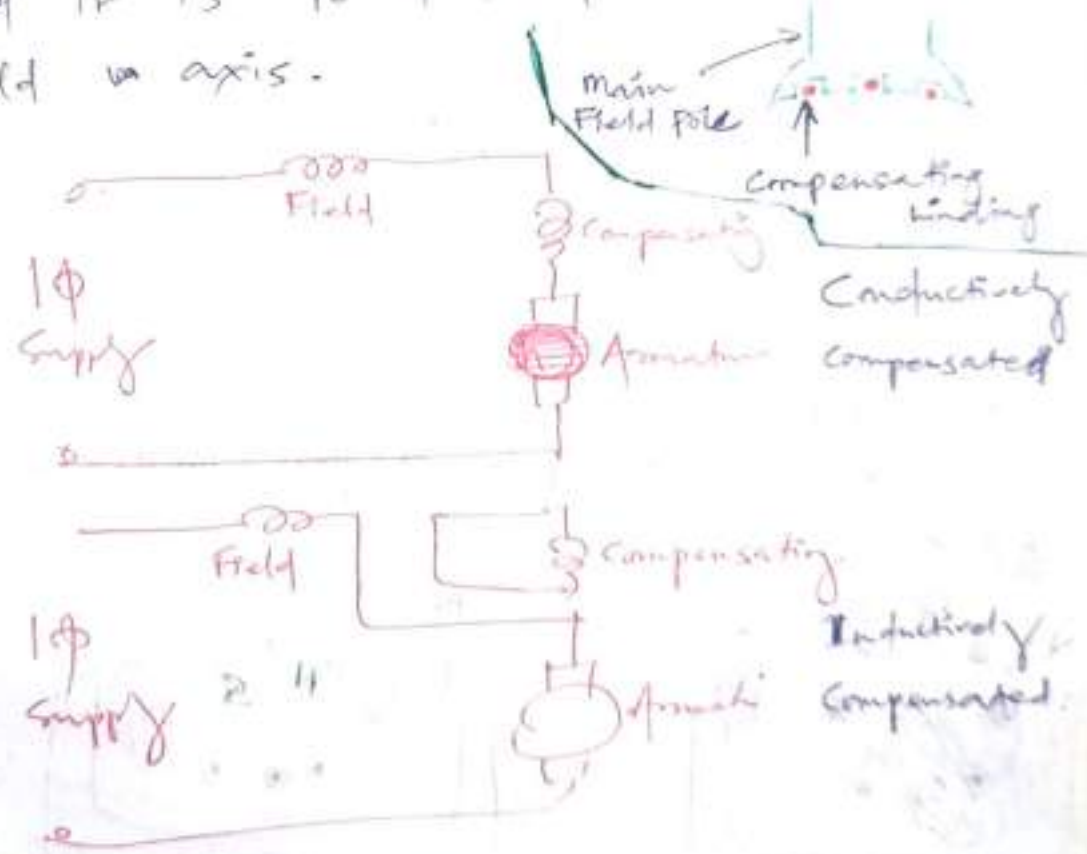
① Core constructed of magnetic material of having low hysteresis loss and laminated to reduce eddy current loss.

② Field winding of small number of turns (\therefore Flux reduces)

③ In order to get desired torque $\Phi \uparrow$; N ^{number of} armature conductors are increased.

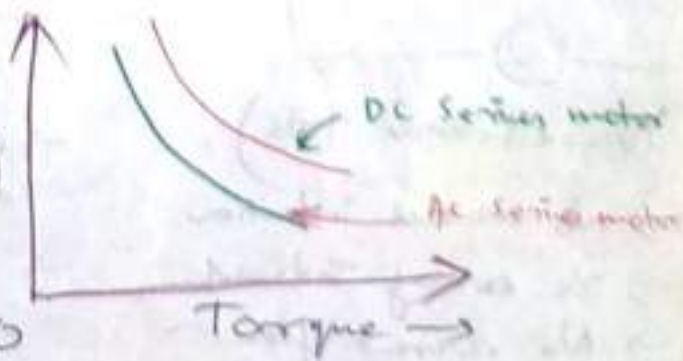
③ To counter effect of armature reaction (\rightarrow poor commutation), a compensating winding is used.

Placed in series with armature winding and it is 90° electrical with the main field axis.



Characteristics

Application



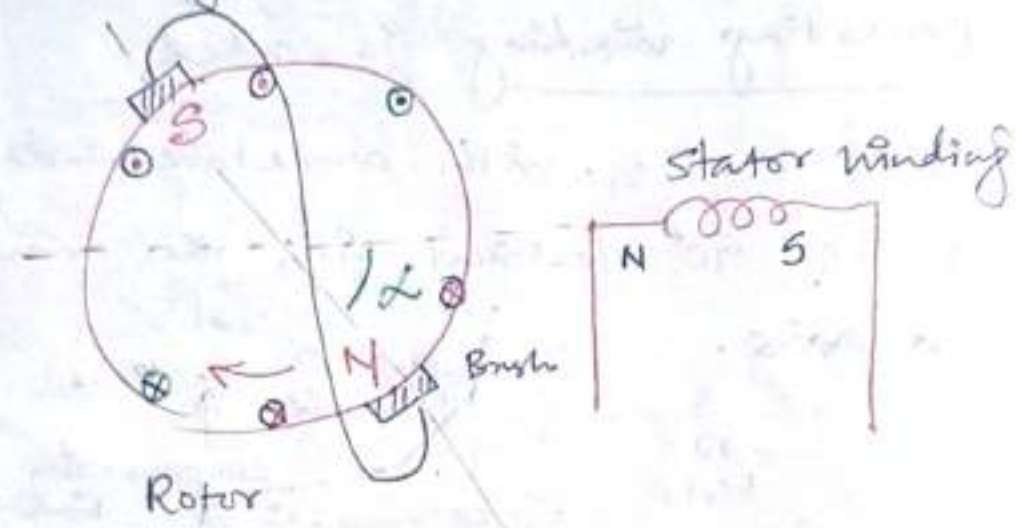
Hair dryer, drill, blower, Table-fan, etc., mixer

II Repulsion motor } To facilitate starting of 1 ϕ m.



Construction

- Stator is supplied with 1 ϕ AC
- Rotor end cut is short circuited through carbon brush.

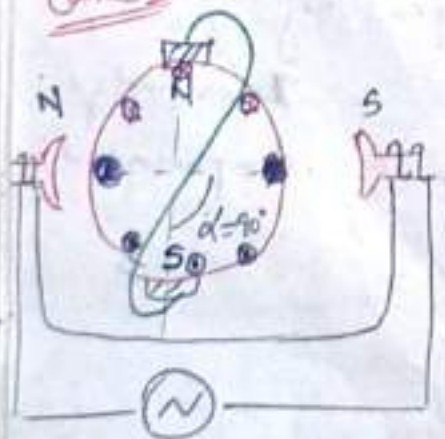


Working principle

- Similar pole repel each other i.e. North pole repels North pole.

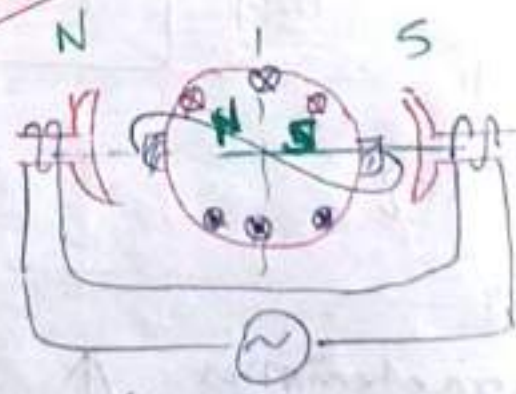
Case II

First Case I



(Quadrature Axis)

- No mutual induction
- No emf induced
- No current flow
- No torque develops



($\alpha = 0^\circ$)

- Maximum emf is induced across brushes.
- rotor & stator flux coincide & perfect mutual coupling between them
- No Tor.



Case III



→ Repulsion motor:

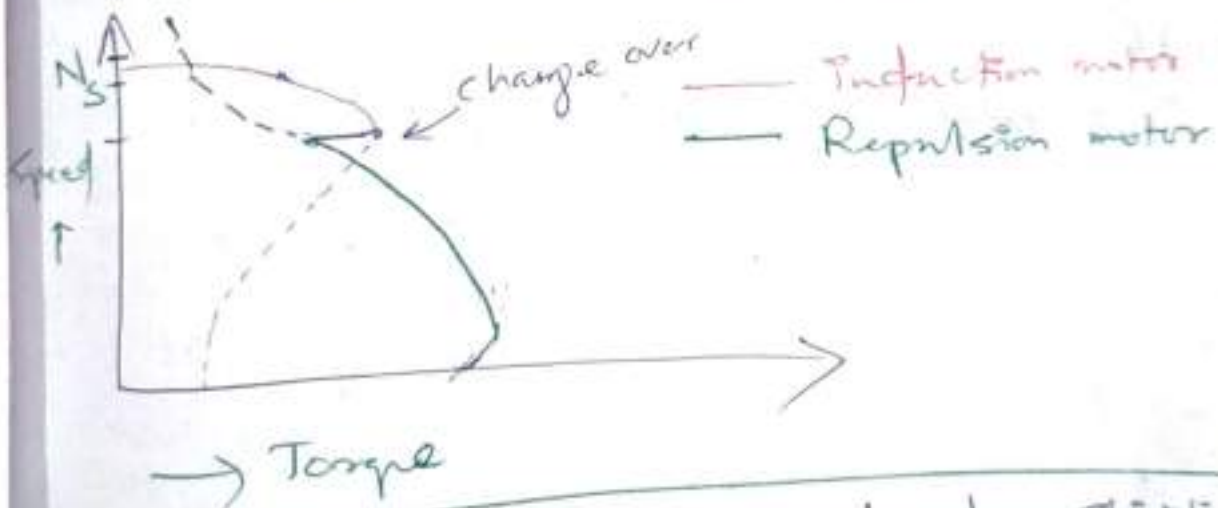
High starting torque & no
Speed regulation (may go beyond ω_{Ns})

→ Induction motor (IP)

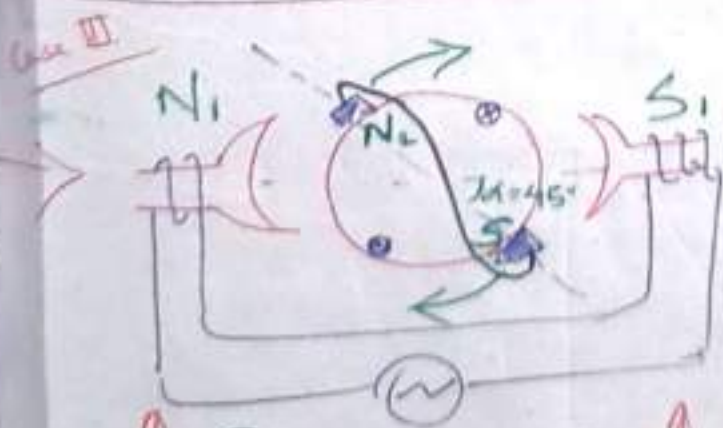
Low starting torque & good
 (0) speed regulation (constant speed with normal load)

Repulsion start - Induction run motor.

At about 80% transition from the
 repulsion motor to induction motor is done.
 (or At $T_{rep} \geq T_{ind}$) → Shifting the
 commutator



⊙ Reversal of motor is done by shifting
 the brush axis.



To oppose stator
 flux; rotor to
 brush induces pole.
 S_1 repel S_2 .
 motor rotate in
 clockwise direction



REVERSAL

Advantage of repulsion motor

- ① Self starting
- ② High Torque
- ③

Disadvantage

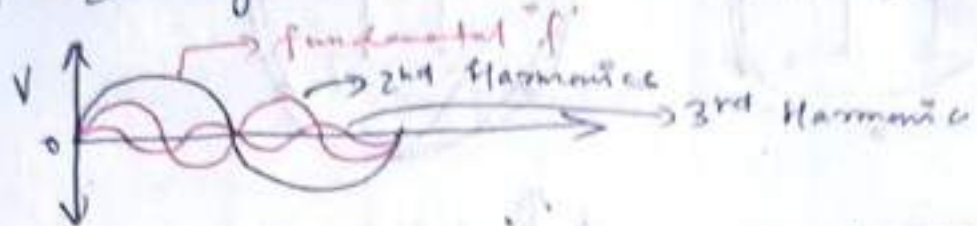
- ① May spark at brush.
- ② Commutator & brush wear out quickly.
- ③ Very high no load speed.

Application

- ① Hoist, mining equipment

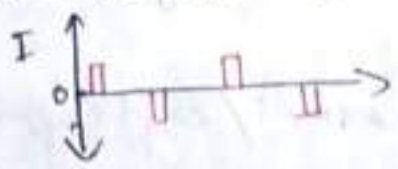
HARMONICS

In Electrical system, a harmonic of a voltage/current waveform is a sinusoidal wave whose frequency is an integer multiple of the fundamental frequency (i.e. 50Hz).



Causes of Harmonic production

- (i) Non-linear load, draw current in abrupt short pulses. This short pulse cause distortion in current waveform.



- (ii) Power electronics devices causes Harmonics.
- (iii) Magnetic saturation of transformer
- (iv) ^{core} CFL, Arc welders
- (v) Stat harmonics

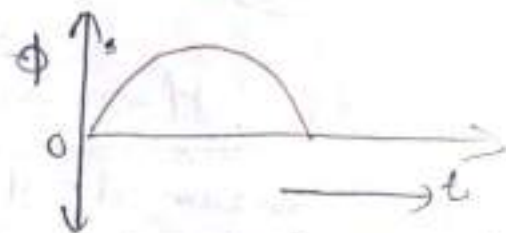
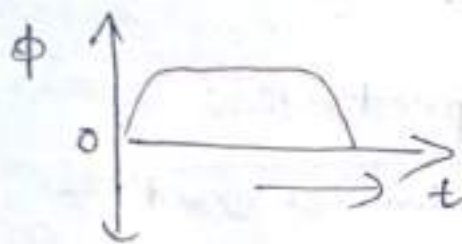
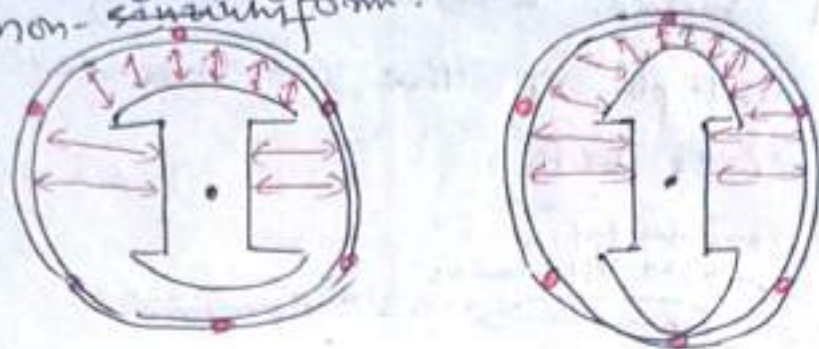
Harmonic (vi) Non-sinusoidal flux distribution in the air gap. ~~(vii)~~ $[V \propto \frac{d\Phi}{dt}]$

$$E \sin(\omega t) \leftarrow \cos(\omega t) \rightarrow \Phi = \frac{\text{MMF}}{R} = \frac{NI}{R} \rightarrow \text{constant}$$

$R \rightarrow \text{variable}$
 $\rightarrow \sin(\omega t)$

* Why non-sinusoidal flux distribution in air-gap?

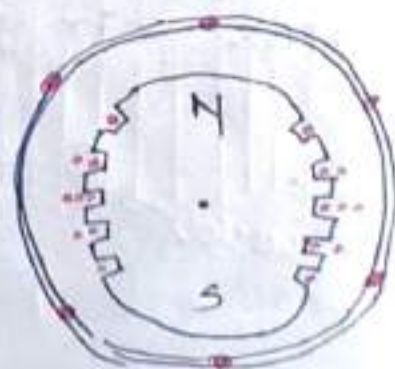
① In salient pole \rightarrow the air gap is non-uniform.



Solution \div "Chamfered pole" shape used to provide uniform flux distribution.

② In turbo-alternator / cylindrical-synchronous machine, the air gap is uniform.

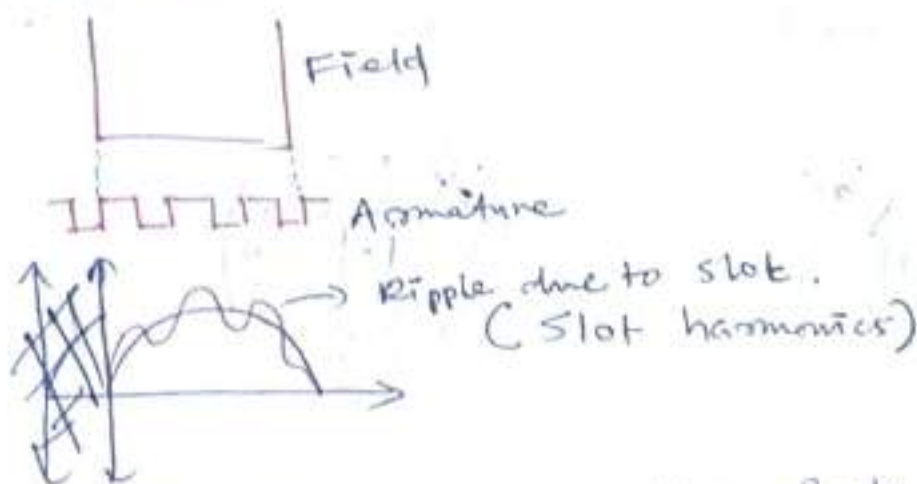
Solution \div To adjust the above factor the distribution of field windings should be done in such a way that it produces sinusoidal flux distribution.



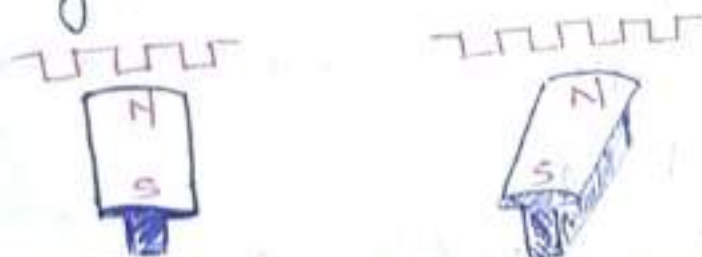
② Slot Harmonics

The stator where armature windings are mounted is not smooth rather it is slotted.

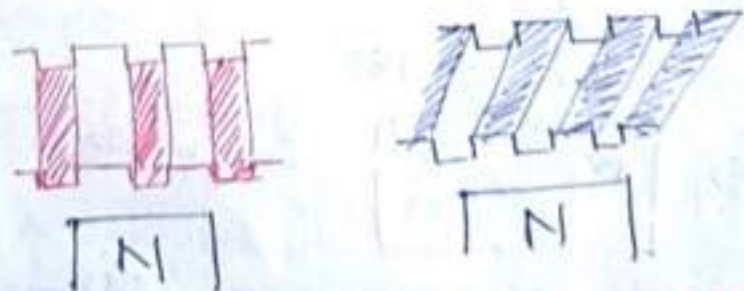
It causes in non-uniform flux distribution.



Solution: To reduce the ripple in generated emf - the ^{pole face} ~~slot~~ should be skewed.



(OR) skewing of armature slot, the harmonics can be ~~reduced~~ reduced.



The above methods should be followed to make the flux sinusoidal, but still it is not purely sinusoidal.

* Other solution at generated volt

emf end (Armature End)

① Distributed armature winding

The distributed winding along air-gap periphery tends to make generated emf waveform sinusoidal.



② Short pitch/Chorded coil

The n th harmonic can be eliminated if

$$K_p = \cos\left(\frac{n\alpha}{2}\right) = 0$$

$$\Rightarrow \frac{n\alpha}{2} = 90^\circ$$

$$\Rightarrow n\alpha = 180^\circ \dots$$

$$\Rightarrow \boxed{\alpha = \frac{180^\circ}{n}} \text{ Short pitch angle.}$$

→ The 3rd Harmonic is eliminated in line (°° Star connection)

→ 5th & 7th Harmonics are present in emf generated. So, $\alpha = 30^\circ$ should be made to reduce 5th & 7th Harmonics.

→ Higher order Harmonics are insignificant.

$$\alpha_1 = \frac{180^\circ}{5} = 36^\circ \rightarrow \text{For 5th Harmonic}$$

$$\alpha_2 = \frac{180^\circ}{7} = 25^\circ \rightarrow \text{For 7th Harmonic}$$

$$\alpha_{5+7} = \frac{36+25}{2} \approx 30^\circ \rightarrow \text{For 5th \& 7th Harmonic}$$

* Conclusion (How to remove Harmonics)

• First we tried to make flux sinusoidal

- ① Changed pole
 - ② Skewing pole in rotor to vary conductor length sinusoidally
 - ③ By increasing air gap \rightarrow Inductance Harmonics flux \downarrow
- (Improve stability of machine)

Modification on field side.

• On Armature side.

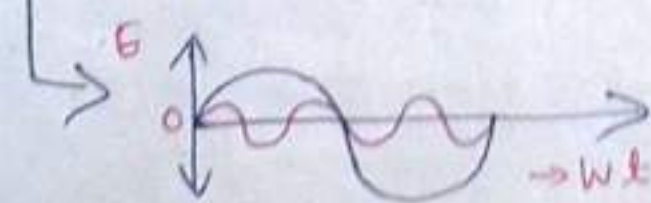
- ① Short pitching the windings
- ② Distributed winding
- ③ fractional slot
- ④ By skewing armature slot.

\rightarrow flux harmonics \rightarrow [Space Harmonics]

\rightarrow Emf harmonics \rightarrow [Time Harmonics]



$$B = B_1 \sin \alpha + B_2 \sin 3\alpha$$



$$E = E_1 \sin \omega t + E_2 \sin 3\omega t$$