

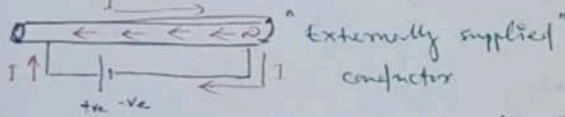
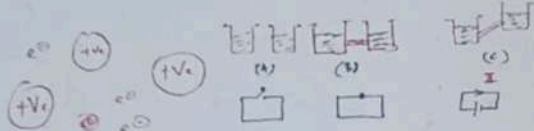
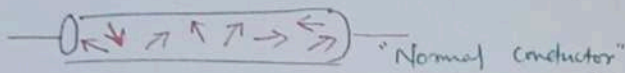
## Basic Electrical Engg.

### \* Current (Start with Atomic Structure)

The rate at which  $e^-$  flows through a conductor cross section of a conductor/wire is called current.

Symbol:  $I, i$

Unit: "Ampere"  
(French)



Conventional 'I' is opposite to  $e^-$  flow direction because - it was assumed prior to "Electron theory". Franklin Assumed

### \* Source

An electric source is that which can supply electric power to any load.

ex- Voltage Source, Current Source.



### \* Load

Anything in electric circuit which consume power is known as Load.

ex- Resistor, Inductor, Capacitor

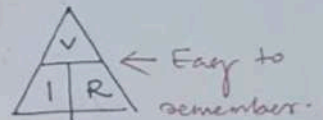
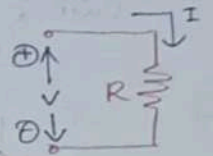
### \* Ohm's Law [George Simon Ohm]

The current flowing through a conductor is directly proportional to the potential difference maintained across it both ends, provided the temperature & other physical conditions constant.

$$I \propto V$$

$$\Rightarrow IR = V$$

$$\Rightarrow I = \frac{V}{R}$$



### \* Electric potential (After Current)

Work done to carry a unit charge from one point to another point <sup>(Energy)</sup> against an electric field.  $V = \frac{\text{Work Done}}{Q \text{ charge}}$

### \* Potential difference

The difference in potential between two points of a circuit.

Unit - Volt (Alessandro Volta)  
(Italian) - Battery Invented

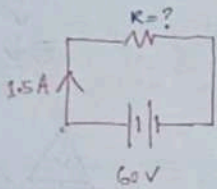
\* Resistance

It is the property of a substance which opposes the flow of electric current through it.

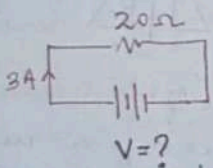
Symbol: 

Unit:  $\Omega$  (Ohm)  
(George Simon Ohm)  $\rightarrow$  German

(2)



(2)

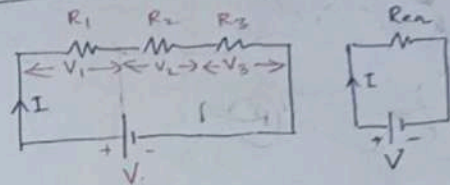


\* Resistance depends upon -

- ①  $R \propto l$
- ②  $R \propto \frac{1}{a}$
- ③  $R \propto$  nature of materials
- ④  $R$  depends upon temperature.

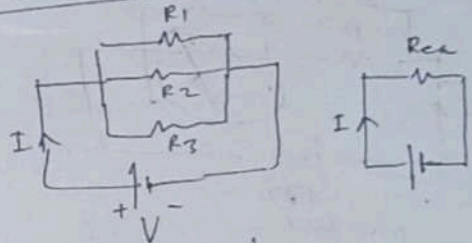
$R \propto \frac{l}{a} \Rightarrow R = \rho \frac{l}{a}$   
Resistivity  $\leftarrow$

"R" connected in series



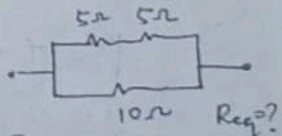
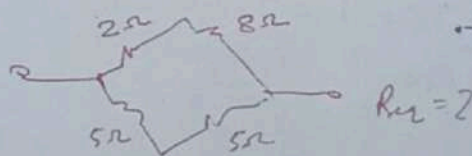
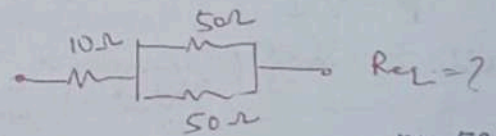
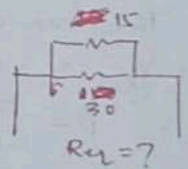
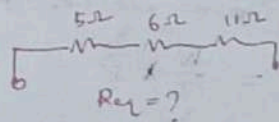
$R_{eq} = R_1 + R_2 + R_3 + \dots$

"R" connected in parallel

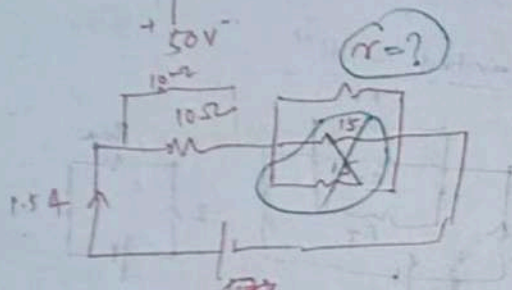
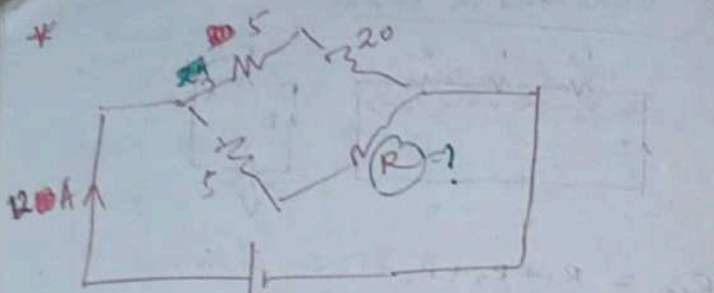


$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$

(Ex)



\* Note: current & voltage in parallel circuit



**POWER**  $= 20V$

The rate of at which energy is consumed in a electric circuit

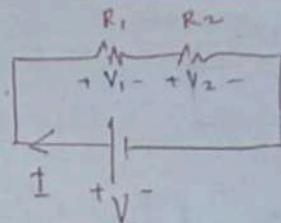
$$P = \frac{\text{Energy}}{\text{Time}} = \frac{W}{Q} * \frac{Q}{t} = \frac{W}{t}$$

$$P = VI$$

Unit = Watt (James watt - Steam engine) (mechanical engineer) to make industrial meter

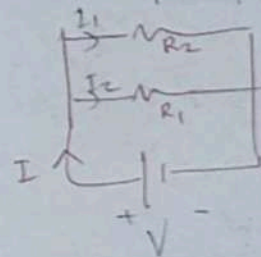
$$P = I \cdot IR = I^2 R$$

$$P = V^2 / R$$



$P =$  Power delivered/supply by cell  $= VI$   
 $P_1 =$  Power consumed by  $R_1 = IV_1 = I^2 R_1$   
 $P_2 = \dots R_2 = IV_2 = I^2 R_2$

$$P = P_1 + P_2$$



$$P = VI$$

$$P_1 = I_1 V = V^2 / R_1$$

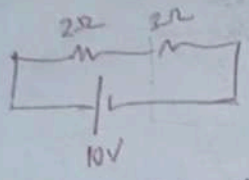
$$P_2 = I_2 V = V^2 / R_2$$

$$P = P_1 + P_2$$

$$\boxed{\sum P_{\text{supply}} = \sum P_{\text{consumed}}}$$

Kirchoff's current law & KVL

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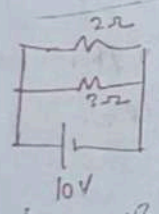


Find  $P_{2\Omega}$  &  $P_{10V}$

$$I = \frac{10}{2+2} = 2.5$$

$$P_{2\Omega} = I^2 R_{2\Omega} = 2.5^2 \cdot 2 = 12.5$$

$$P_{10V} = 12.5 + 12.5 = 25$$



$$P_{2\Omega} = I_{2\Omega}^2 R_{2\Omega} = \frac{V^2}{R_{2\Omega}} = \frac{10^2}{2} = 50$$

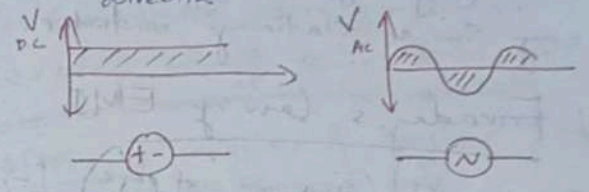
$$P_{2\Omega} = \frac{V^2}{R_{2\Omega}} = \frac{10^2}{3} = 33.33$$

$$P_{10V} = 50 + 33.33 = 83.33$$

That's why load are connected in parallel.

## AC Theory

DC  $\rightarrow$  Current flow in one direction  
 AC  $\rightarrow$   $e^-$  charge flows changes periodically  
 Both Voltage & Current changes direction



$\Rightarrow$  For transmitting over long distance DC was losing power. So, voltage drop along the length. (Thomas Edison)

$\Rightarrow$  AC could easily "step up" or "step down" So, with less loss using Transformers (Nicola Tesla)  
 Faraday's law of electromagnetic induction  
 "War of Currents"

- $\rightarrow$  Compas (1200)
- $\rightarrow$  Earth magnetism - 1600 (William Gilbert)
- $\rightarrow$  Volta (1800) Cu-Zn & HCl
- $\rightarrow$  Oersted (1820)  $I \rightarrow B$
- $\rightarrow$  Electro-magnet (1824)
- $\rightarrow$  Ohm's Law (1827)
- $\rightarrow$  Faraday's law of EMS (1831)
- $\rightarrow$  Lenz's law (1834)



Generation of Alternating EMF

When a conductor is rotated in magnetic field; emf is generated.  
 OR  
 A changing magnetic field in a stationary conductor generates emf in a stationary conductor.

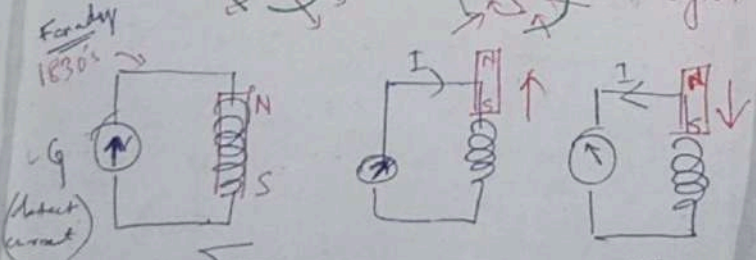
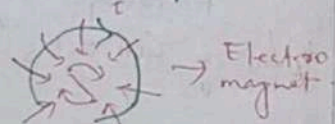
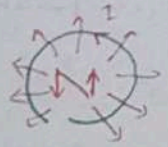
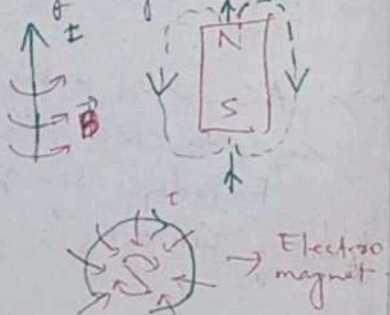
Faraday's Law of EMI

HC Oersted (Start from next page)  $I \rightarrow B$

In 1820, electric current in a wire from a battery caused a nearby compass needle to deflect.

So, electricity - magnetism are interrelated.

So, electric current create magnetic field.



[Faraday's Experiment]

→ Changing magnetic field produced induces emf in a circuit.

$emf \propto \frac{d\phi}{dt}$  (rate of change of flux magnetic)

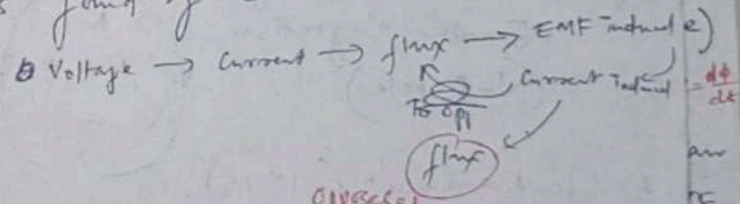
Application

→ Generator, transformer, motor  
 Two way  $\frac{d\phi}{dt}$  can be done

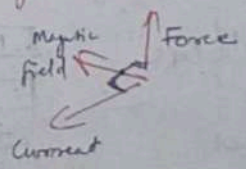
- ① Motion of conductor & constant flux. (Dynamically induced emf)
- ② Change in current leads to change in magnetic flux linked with stationary coil.

(Statically induced emf)  
 ∴ we can't see magnetic flux

→ The direction of induced emf is found by LENZ'S LAW.

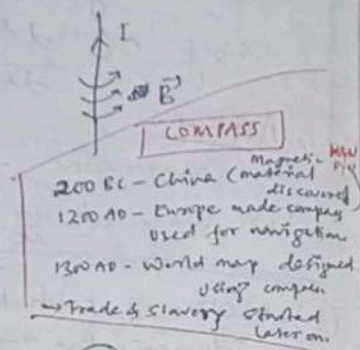
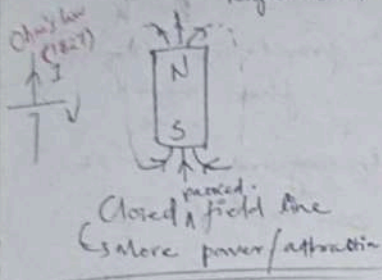


Fleming's right hand rule

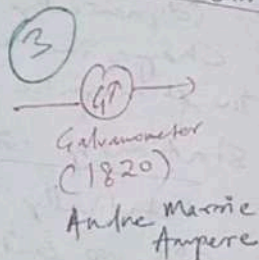
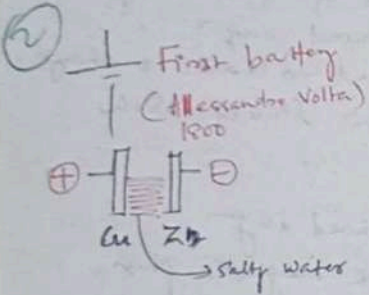


Oersted  $\rightarrow$  link bet<sup>n</sup>  $B$  &  $i$

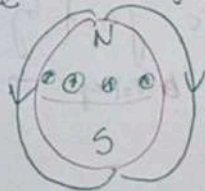
Right hand Thumb Rule



200 BC - China (Magnetic discussed)  
 1200 AD - Europe made compass used for navigation  
 1300 AD - World map designed using compass  
 $\rightarrow$  Trade & slavery started later on



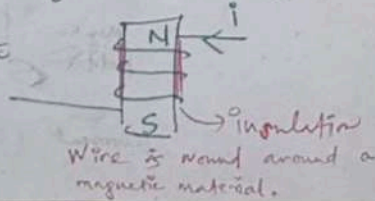
Father of Magnetism - William Gilbert (English)  
 1600 - De Magnete Earth Magnetism (N-S pole)



\* Electromagnet (1824)

William Sturgeon (British)

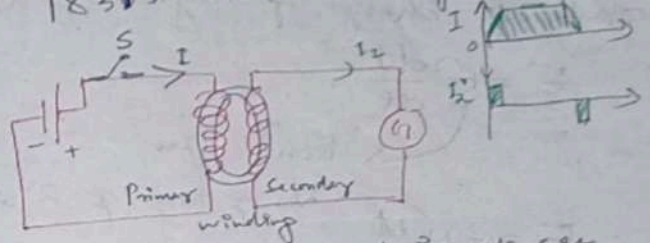
Iron, steel, nickel, cobalt. CORE



$\rightarrow$  Large magnet

## Faraday law of Electromagnetic Induction

1830's Michael Faraday



To see, the effect if we can generate magnetic electric field from magnetic field. (Opposite of Oersted)

$\rightarrow$  He saw transient current in  $G$  when he switch ON & OFF the supply. But during the supply; no deflection in  $G$  was observed. Change in magnetic flux =  $\frac{B}{A}$  (field line) induces an emf in 2<sup>nd</sup> coil. Next page  $\epsilon = \frac{d\phi}{dt}$

$\rightarrow$  Emil Lenz (1834) gave Lenz's law which describes the direction of induced emf & current resulting from electromagnetic induction.

$\rightarrow$  induced emf  $\rightarrow$  induced current  $\rightarrow$  flux (2<sup>nd</sup>) opposes the change in magnetic field (1<sup>st</sup> flux)

## Law of EMI

in a loop of wire is

The emf induced is given by the "rate of change of magnetic flux".

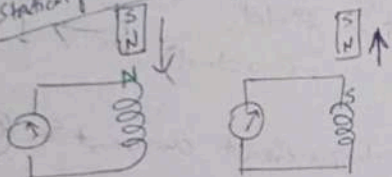
$$E = - \frac{d\phi}{dt}$$

Lenz's Law

$$E_i = -N \frac{d\phi}{dt}$$

Nos of turns of 2<sup>o</sup> coil.

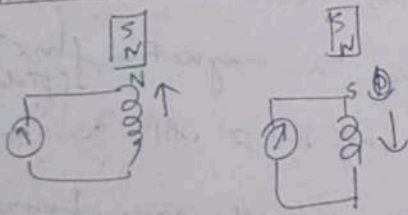
### II Statically induced emf



"Teach after" Lenz's Law

(Stationary conductor - change in  $\vec{B}$ )

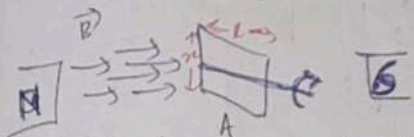
### I Dynamically induced emf



## Magnetic flux ( $\phi$ )

Unit - Weber

Nos of magnetic field line passing thro' a unit Area.



$$\phi = \vec{B} \cdot \vec{A}$$

Strength of magnetic field

Area of loop



$$\phi = \vec{B} \cdot \vec{A}$$

$$\phi = \vec{B} \cdot L \times b$$

length

breadth

But  $\epsilon = - \frac{d\phi}{dt} = - B L \frac{dx}{dt} = \vec{B} (L \vec{v})$

- $L \rightarrow$  length of conductor/loop.
- $v \rightarrow$  velocity of conductor
- $B \rightarrow$  magnetic field intensity.

When a conductor is moved in a magnetic field it induces an emf.

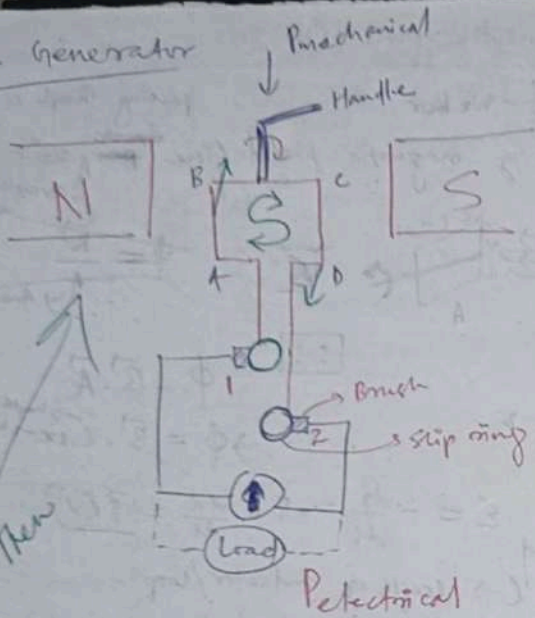
$$\epsilon = \vec{B} \cdot L \cdot \vec{v}$$

(Dynamically induced emf)

if  $\vec{B} \cdot \vec{v}$  has  $90^\circ$

The diagram shows a vector  $\vec{B}$  pointing vertically upwards and a vector  $\vec{v}$  pointing horizontally to the right, with a right-angle symbol between them.

# # AC Generator



Start with

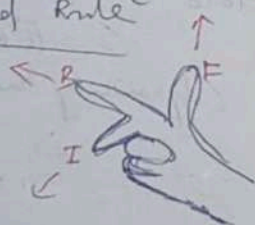
Fleming's Right Hand Rule (Lenz's + EMI)

Thumb:  
point to the direction of Force

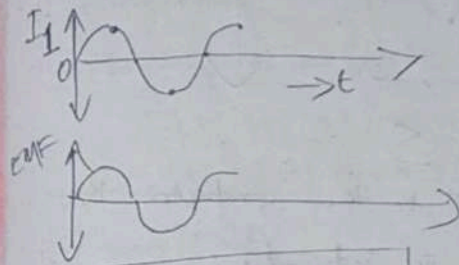
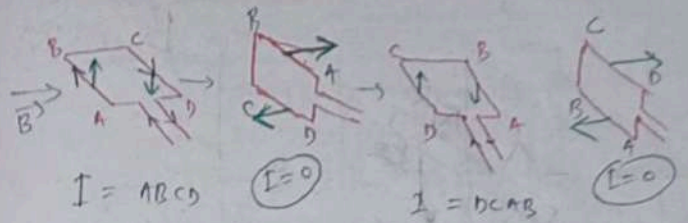
Index finger:  
point in the direction of magnetic field.

Middle finger:  
point the direction of flow of current

They are  $\perp$  to each other



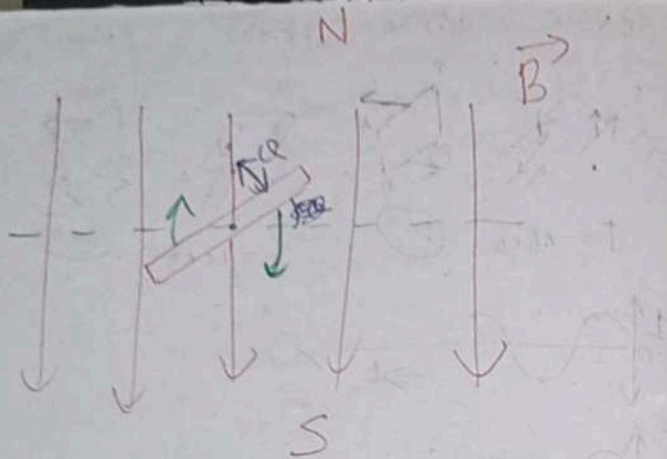
$B, \vec{v} = 90^\circ$      $B, \vec{v} = 0^\circ$      $B, \vec{v} = 90^\circ$      $B, \vec{v} = 0^\circ$



$$E = B l \vec{v} \sin \theta$$

$$E = E_{max} \sin \theta$$





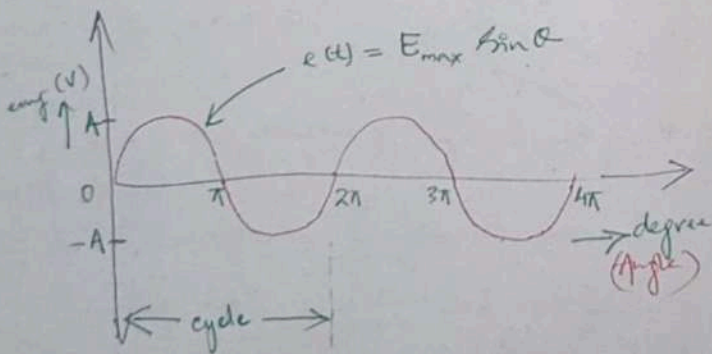
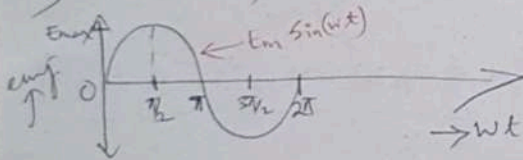
if  $\vec{B}$  is  $\perp$  to the conductor then maximum emf is induced.

$$E = Blv \sin \alpha$$

$$\alpha = \omega t$$

Angular speed.

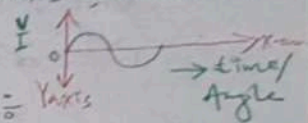
$$\Rightarrow E = E_{\max} \sin \alpha$$



### # Terminology

#### ① Waveform:-

The shape of curve of the voltage or current along Y-axis when plotted against time/angle along X-axis; is called waveform.



#### ② Instantaneous value:-

The voltage/current at any instant  $e(t), i(t)$  ← representation.

#### ③ Amplitude

The "maximum" value of the positive or negative half of ac wave.

#### ④ cycle

A sine wave represent one cycle. A combination of positive half & negative half cycle. A cycle spread over  $360^\circ$  or  $2\pi$  radian.

#### ⑤ Time period (T)

Time taken by an AC voltage/current to complete one cycle is ... Unit :- Second

$$T = \frac{1}{f}$$

#### ⑥ Frequency

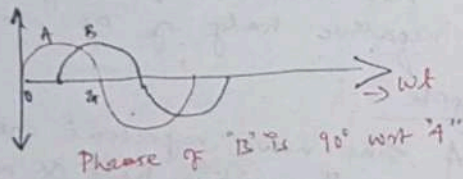
The nos of cycles passed through in one second. Unit - Hz (Hertz)

$$f = \frac{1}{T}$$

⑦ Angular velocity  $\omega$   
 It is the angular distance covered per second.  
 represented by  $\omega$  (Omega)  
 Unit  $\omega$ : rad/sec  
 $\omega = 2\pi f$  frequency

$\omega = \frac{\theta}{\text{time}}$

⑧ Phase diagram difference  
 It is the angular displacement of the phasor from a reference value.

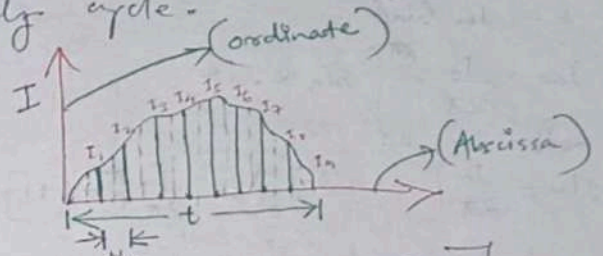


⑨ Phase difference  
 The difference between the phases of two alternating quantity.  
 90° phase difference between A & B.

AC	DC
① I change its magnitude & direction	① I doesn't change magnitude & direction
② e <sup>-</sup> flow is bidirectional	② e <sup>-</sup> flow in one direction
③ f = 50 Hz, India	③ f = 0 Hz
④ pf = 0-1	④ pf = 1
⑤ Z = jX + R	⑤ Z = R
⑥ AC generated by AC gen	⑥ DC generated
⑦ Represented by sine, triangle, square	⑦ Represented by straight line

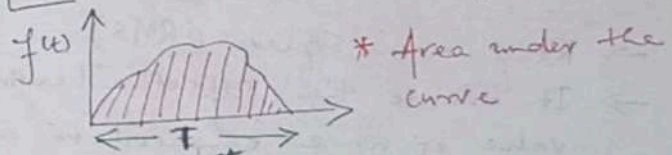
\* Average Value

It is the arithmetic mean of the ordinates at equal interval over a half cycle.



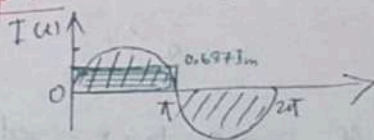
$$I_{av} = \frac{i_1 + i_2 + \dots + i_m}{m}$$

m → Nos of interval



$$I_{av} = \frac{1}{T} \int_0^T i \cdot dt$$

Half wave

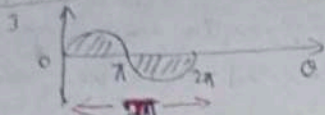


$$I_{av} = \frac{I_{max}}{\pi} \int_0^{\pi} \sin \theta \cdot d\theta$$

$$\Rightarrow I_{av} = \frac{I_{max}}{\pi} [-\cos \theta]_0^{\pi} = \frac{I_{max}}{\pi} [-\cos \pi - (-\cos 0)]$$

$$\Rightarrow I_{av} = \frac{I_{max}}{\pi} [1 + 1] = \frac{2}{\pi} I_{max} = 0.637 I_{max}$$

\* Full sine wave



$$i = I_m \sin \omega t$$

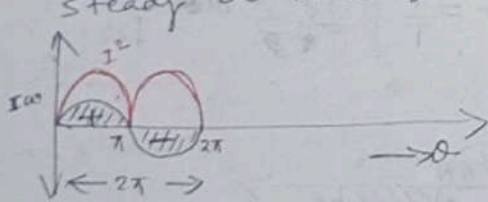
$$I_{av} = \frac{I_m}{2\pi} \int_0^{2\pi} \sin \omega t \cdot d\omega t$$

$$\rightarrow I_{av} = \frac{I_m}{2\pi} [-\cos \omega t]_0^{2\pi} = \frac{I_m}{2\pi} [-1 + 1] = 0$$

∴ Area under curve over a one cycle is zero.

\* RMS value

- Root mean Square (RMS)
- It indicate the effective heating value of wave compared to a steady DC value.



$$E_w = I^2 R t$$

→ "Amount of AC power that produces the same heating effect as an equivalent DC power".

→ Square root of the mean of the square of instantaneous value.

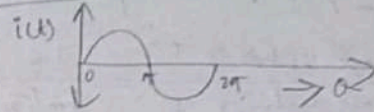
$$I_{rms} = \sqrt{\frac{i_1^2 + i_2^2 + \dots + i_n^2}{n}} = \sqrt{\frac{1}{T} \int_0^T i^2 dt}$$

n → nos of interval.



$$I_{rms} = \sqrt{\text{Mean of } i^2}$$

Sine Wave



$$i(t) = I_{max} \sin \omega t$$

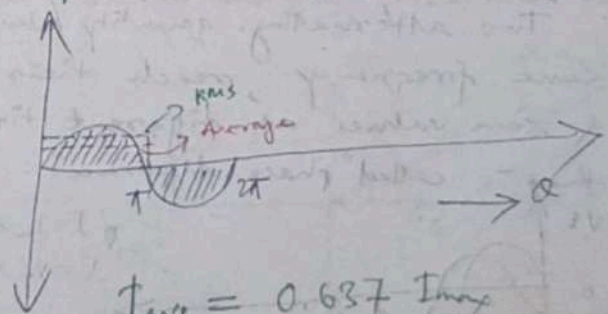
$$I_{rms} = \sqrt{\frac{I_{max}^2}{2\pi} \int_0^{2\pi} \sin^2 \omega t \cdot d\omega t}$$

$$= \sqrt{\frac{I_{max}^2}{2\pi} \int_0^{2\pi} \left[ \frac{1 - \cos 2\omega t}{2} \right] d\omega t}$$

$$= \sqrt{\frac{I_{max}^2}{2\pi} \left[ \frac{\omega t}{2} - \frac{\sin 2\omega t}{4} \right]_0^{2\pi}}$$

$$= \sqrt{\frac{I_{max}^2}{2\pi} \left[ \frac{2\pi}{2} - \left( \frac{\sin 2 \cdot 2\pi}{4} - \frac{\sin 0}{4} \right) \right]}$$

$$I_{rms} = \sqrt{\frac{I_{max}^2}{2}} = \frac{I_{max}}{\sqrt{2}} = 0.707 I_{max}$$



$$I_{avg} = 0.637 I_{max}$$

$$I_{RMS} = 0.707 I_{max}$$

# Form factor

$$FF = \frac{\text{Rms value of } I}{\text{Average value of } I} = \frac{0.707 I_m}{0.637 I_m} = 1.11$$

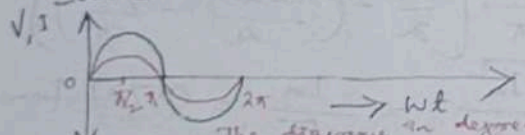
Sine Wave

# Peak factor / Amplitude factor

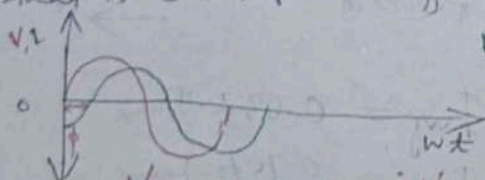
$$PF = \frac{\text{Max value of } I}{\text{RMS value of } I} = \frac{I_m}{I_m/\sqrt{2}} = \sqrt{2} = 1.414 \text{ Sine wave}$$

\* Phase & Phase Sequence

Two alternating quantity are said to be in "phase" when they reach their maximum & zero values at the same time.



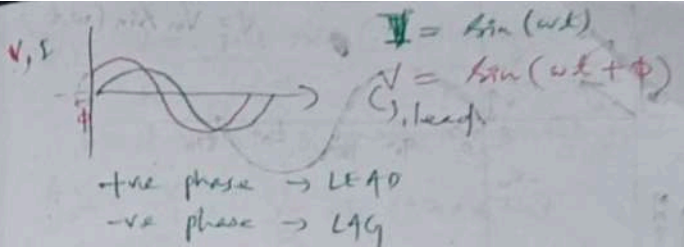
The difference in degree/radian when two AC quantity reach their maximum or zero values. Two alternating quantity wave with same frequency, reach their maximum & zero values at different time first that is called "phase difference".



V leads I by  $\phi$  phase angle.  
OR I lags V by  $\phi$  phase angle.

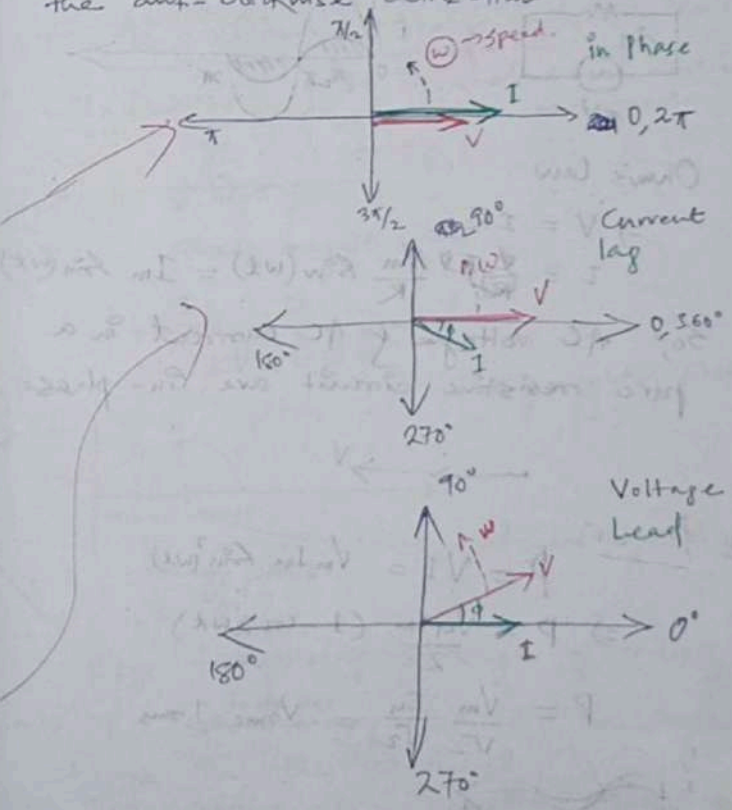
$$I = I_m \sin(\omega t + \phi)$$

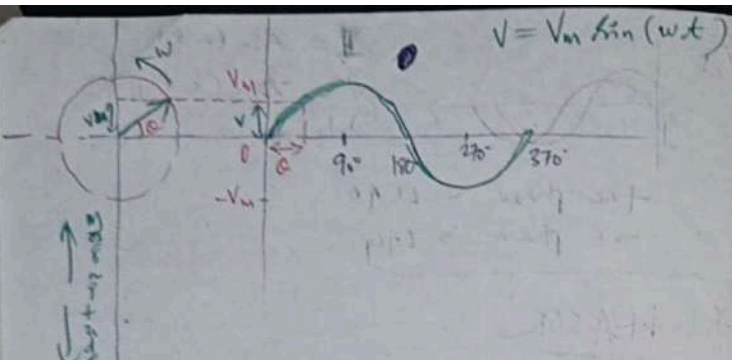
$$V = V_m \sin(\omega t)$$



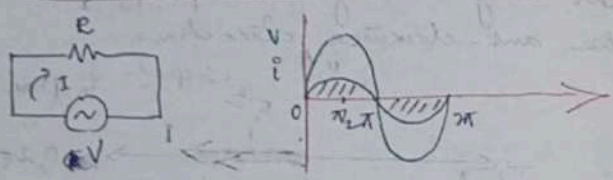
\* PHASOR

It is a rotating vector which has uniform angular speed  $\omega$  in the anti-clockwise direction.





\* AC through purely Resistive Circuit

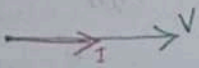


Ohm's Law

$$\Rightarrow V = IR$$

$$I = \frac{V}{R} = \frac{V_m \sin(\omega t)}{R} = I_m \sin(\omega t)$$

So, AC voltage & AC current in a pure resistive circuit are in-phase,



# Power

$$P = VI = V_m I_m \sin^2(\omega t)$$

$$\Rightarrow P = \frac{V_m I_m}{2} (1 - \cos 2\omega t)$$

$$P = \frac{V_m}{\sqrt{2}} \frac{I_m}{\sqrt{2}} = V_{rms} I_{rms}$$



Q.  $V = 141 \sin(314t + \pi/3)$

$R = 10 \Omega$

Find RMS & maximum value of current

Ans  $i = \frac{V_m}{R} \sin(314t + \pi/3)$

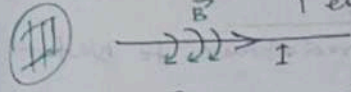
$\Rightarrow i = 14.1 \sin(314t + \pi/3)$

$I_m = 14.1 \text{ Amp}$

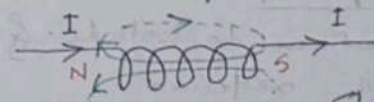
$I_{rms} = \frac{14.1}{\sqrt{2}} = 10 \text{ Amp}$

\* AC through purely inductive circuit

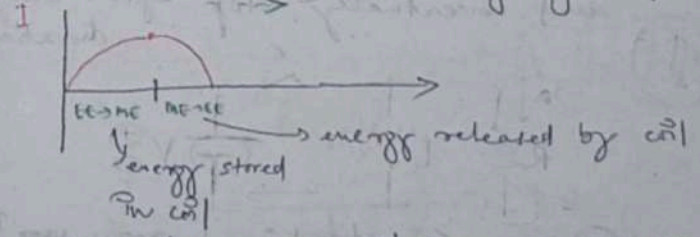
Inductor } It is a electrical device which store magnetic energy.



Small magnetic field



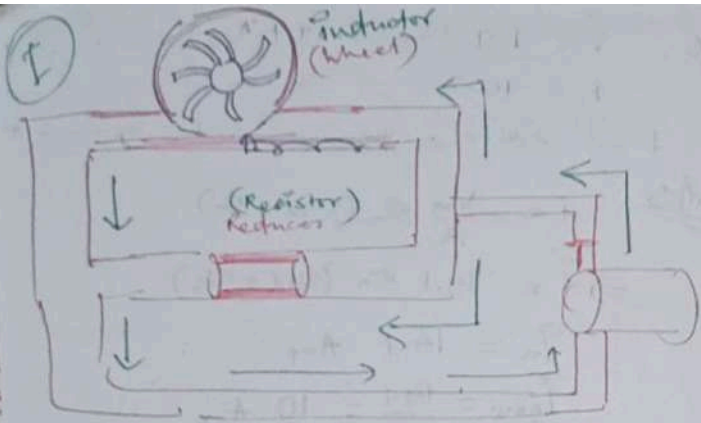
Strong magnetic field



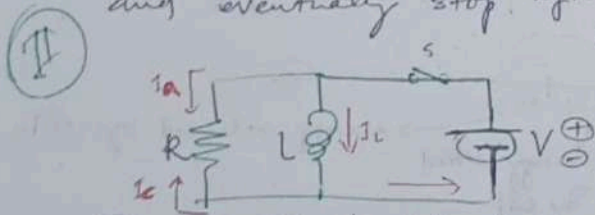
So, temporary storage of energy.

The inductor stored energy opposes the sudden change in the current.

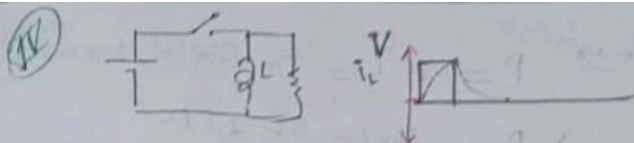
This opposing force is called back EMF



- @ initial time (Resting wheel)  
Wheel offer high resistance to water flow
- @ At max speed of wheel  
It offer no resistance to water
- One pump stop  
Wheel continue to rotate & flow water through restrictor, and eventually stop after short duration.



- When S is closed; L opposes I to flow.
- After some time; L allow I without resistance.
- When S is opened; L deliver current to R for some time but it collapse.



$\mathcal{E}_m = -L \frac{di}{dt}$  but;  $\mathcal{E} = V_m \sin(\omega t)$   
 back emf (induced emf)  $\mathcal{E} = V_m \sin(\omega t)$  opposing

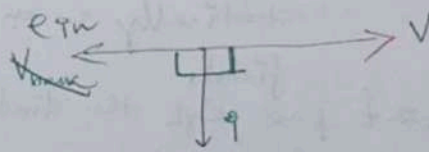
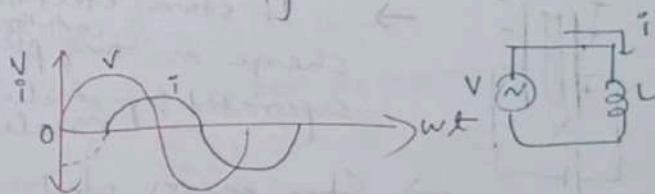
$$\Rightarrow \frac{di}{dt} = \frac{+e}{L} \Rightarrow q = \frac{+1}{L} \int e dt$$

$$\Rightarrow i = \frac{+1}{L} \int V_m \sin(\omega t) dt$$

$$\Rightarrow i = \frac{V_m}{L} [-\cos \omega t]$$

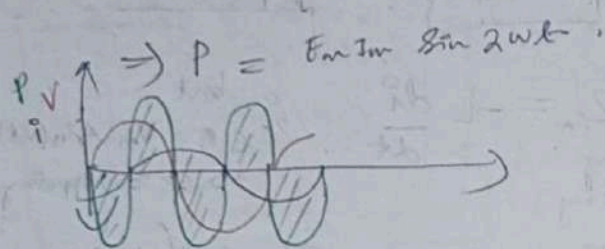
$$\Rightarrow i = \frac{V_m}{\omega L} \sin(\omega t - \frac{\pi}{2})$$

$$\omega L = 2\pi f L \rightarrow \text{inductive reactance}$$



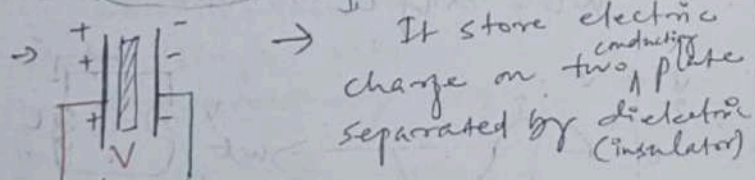
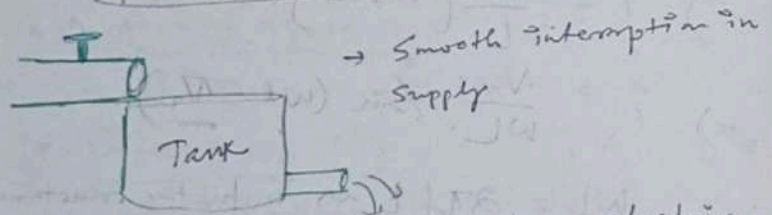
Current lag behind Voltage by  $90^\circ (\frac{\pi}{2})$

Power  $P = e \cdot I = E_m \sin \omega t \cdot I_m \sin(\omega t)$



$\Rightarrow$  Average power consumed in pure inductive ckt is ZERO.

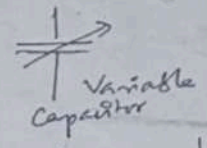
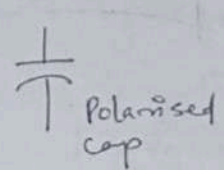
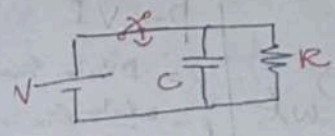
\* AC through pure capacitor



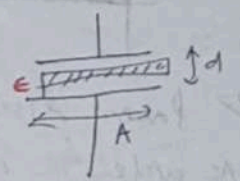
$\rightarrow$  It store electric charge on two <sup>conducting</sup> plate separated by dielectric (insulator)

$\rightarrow$  Store energy electrostatically in an electric field.

$\rightarrow$   $e^-$  that pass thgh the dielectric medium.



$$C = \frac{\epsilon_0 A}{d}$$



Capacitance in "Farad"  
Voltage  $\Rightarrow$  Max voltage that cap can handle.

$$C = \frac{Q}{V} \rightarrow \begin{matrix} \text{charge stored} \\ \text{voltage developed} \end{matrix}$$

$$\Rightarrow Q = CV$$

$$\Rightarrow \frac{dQ}{dt} = C \frac{dV_m \sin(\omega t)}{dt}$$

$$\Rightarrow i = \omega C V_m \cos(\omega t)$$

$$\Rightarrow i = I_m \sin(\omega t + \pi/2)$$

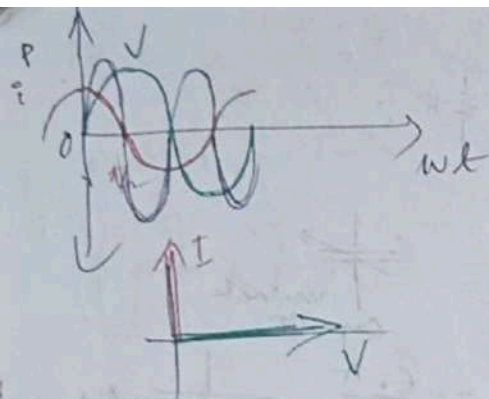
why  $I_m = V_m \cdot \omega C = \frac{V_m}{X_c}$

Capacitive reactance

$$X_c = \frac{1}{\omega C}$$

$$X_L = \omega L$$

$\Rightarrow$  Current lead  $90^\circ$  w.r.t supply voltage.



$$P = VI$$

$$P = V_m I_m \sin \omega t \cos \omega t$$

$$P = \frac{V_m I_m}{2} \sin 2\omega t$$

Power dissipation over a complete AC cycle in a capacitive ckt is zero.

Q A  $V = 141 \sin(314t + \frac{\pi}{3})$  is applied to a  $10 \mu F$  capacitor. Find  $X_c$ ,  $I$ ,  $I_{rms}$ ,  $I_{max}$ .

$$X_c = \frac{1}{\omega C} = \frac{1}{(314)(10) \times 10^{-6}} = 318.47 \Omega$$

$$i = I_m \sin(\omega t + \pi/2)$$

$$i = \frac{141}{318.47} \sin\left(314t + \frac{\pi}{3} + \frac{\pi}{2}\right)$$

$$I_{max} = 0.443$$

$$I_{rms} = \frac{0.443}{\sqrt{2}} = 0.313 \text{ Amps}$$

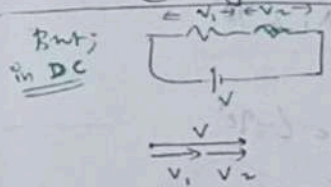
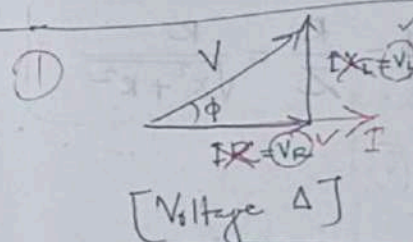
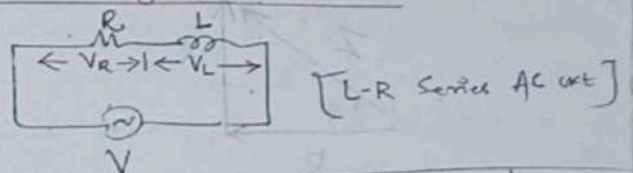
\* Reactance

In AC circuit the opposition to the current offered by inductive & capacitive load.

$$X_L = \omega L \rightarrow \text{Inductive reactance}$$

$$X_C = \frac{1}{\omega C} \rightarrow \text{Capacitive reactance}$$

\* AC through R-L ckt



$$V_R = IR$$

$$V_L = IX_L$$

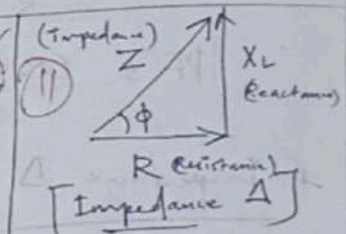
$$V = \sqrt{V_R^2 + V_L^2}$$

$$\Rightarrow V = \sqrt{(IR)^2 + (IX_L)^2}$$

$$\Rightarrow V = I \sqrt{R^2 + X_L^2}$$

$$\Rightarrow I = V/Z$$

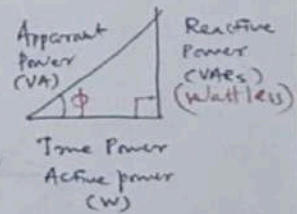
$Z \rightarrow$  Impedance



$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z = R + j(X_L - X_C)$$

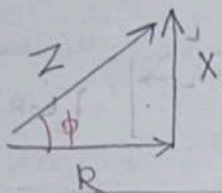
Power Δ (later)





Power Factor (PF)  $e^{i\theta} = \cos(\theta) + i \sin(\theta)$

③ It is the cosine of the angle of lead/lag between applied voltage & current in a AC circuit.

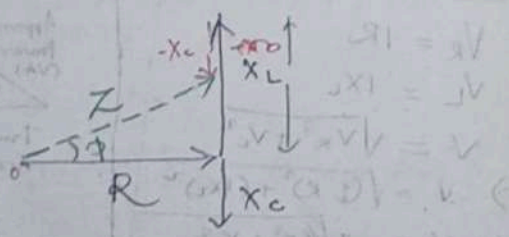


$$PF = \cos \phi = \frac{R}{Z} = \frac{R}{\sqrt{X^2 + R^2}}$$

\* Impedance Δ ④

Inductance:  $X_L = \frac{V}{I} \angle 90^\circ = X_L \angle 90^\circ$

Capacitance:  $X_C = \frac{V}{I} \angle -90^\circ = X_C \angle -90^\circ$



\* Impedance  
The effective Resistance of an electric circuit to AC arising from the combined effects of Ohmic resistance & reactance.

① Active power =  $VI \cos \phi = ZI^2 \cos \phi$

$$\Rightarrow P_a = I^2 R$$

② Reactive power =  $VI \sin \phi = ZI^2 \sin \phi$

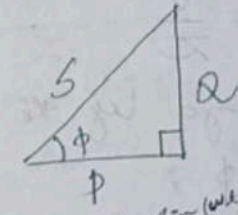
$$\Rightarrow Q = I^2 X$$

Unit - VAR

Apparent power (S) =  $VI = I^2 Z$

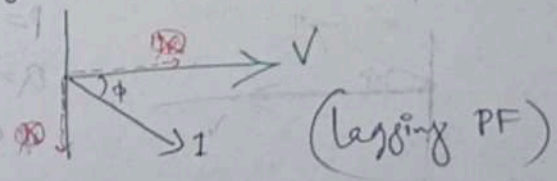
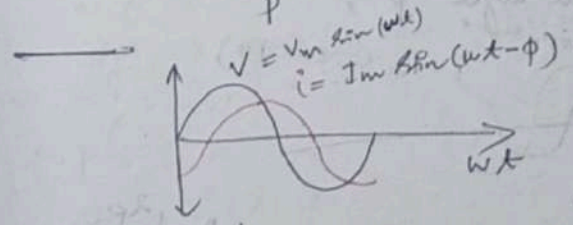
$$S = I^2 Z$$

Combination of P & Q ; VA ← Unit Transformer



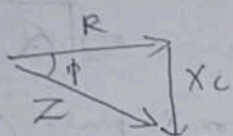
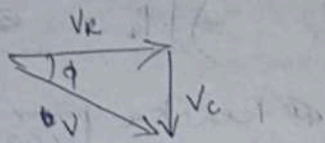
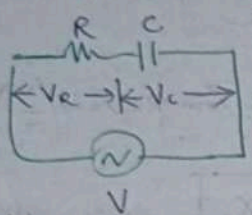
$$S = \sqrt{P^2 + Q^2}$$

$$Z = \sqrt{R^2 + X^2}$$



\* Reactance  
The non-resistive component of impedance in AC ckt, arising from the effect of L or C or both; causing the current to be out of phase with the supply voltage.

### \* AC through R-C circuit



$$V_R = IR$$

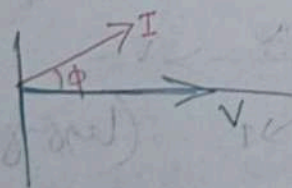
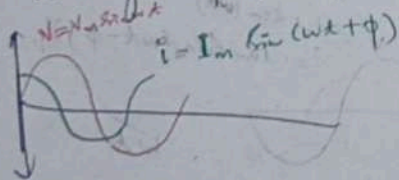
$$V_C = IX_C$$

$$V = \sqrt{V_R^2 + V_C^2}$$

$$\Rightarrow V = I \sqrt{R^2 + X_C^2}$$

$$\Rightarrow I = \frac{V}{\sqrt{R^2 + X_C^2}} = \frac{V}{Z}$$

Applied voltage lags the current by an angle  $\phi$ ;

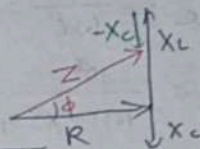
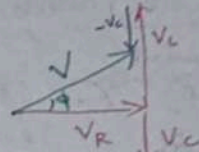
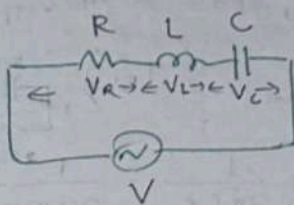


$$P = I^2 R$$

$$Q = I^2 X_C$$

$$S = I^2 Z$$

### \* AC through R-L-C



$$V = \sqrt{V_R^2 + (V_L - V_C)^2}$$

$$\Rightarrow V = I \sqrt{R^2 + (X_L - X_C)^2}$$

$$\Rightarrow I = \frac{V}{Z}; Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$\therefore$  In series R-L-C ckt;

if  $X_L > X_C$  then I lags V by  $\phi$

if  $X_C > X_L$  then I leads V by  $\phi$

$$P = I^2 R$$

$$Q = I^2 (X_L - X_C)$$

$$Z = I^2 Z$$

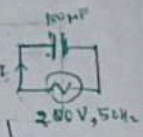
**\* Problems**

Ex-6.14  
Page-185

A capacitor of  $100 \mu\text{F}$  is connected across  $200\text{V}$ ,  $50\text{Hz}$  AC supply.

Calculate

- (i)  $X_c$  (ii)  $I_{RMS}$  (iii)  $I_{Max}$



$$X_c = \frac{1}{\omega C} = \frac{1}{2\pi f C} = \frac{1}{2(3.14)(50)100 \times 10^{-6}}$$

$$\Rightarrow X_c = \frac{10^6}{10000 \times 3.14} = 31.8 \Omega$$

$$I_{RMS} = \frac{V_{RMS}}{X_c} = \frac{200}{31.8} = 6.29 \text{ Amp.}$$

$$I_{Max} = I_{RMS} \sqrt{2} = 6.29 \times 1.41 = 8.87 \text{ Amp.}$$

$$V = 100 \sin(314t)$$

$$* V_{RMS} = \frac{100}{\sqrt{2}}$$

$$* V_{Max} = 100$$

$$* \omega = 314 \Rightarrow 2\pi f = 314$$

$$\Rightarrow f = \frac{314}{2 \times 3.14} = 50 \text{ Hz}$$

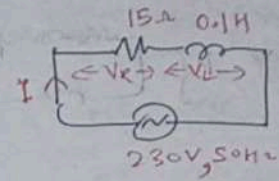
$$T = \frac{2\pi}{\omega} \rightarrow \text{one cycle} = \frac{2\pi}{314}$$

Ex 7.1 (202 page)

$L = 0.1 \text{ H}$   
 $R = 15 \Omega$

$230\text{V}$ ,  $50\text{Hz}$

Find  $I_{RMS}$



- (i)  $I = ?$   
(ii)  $\text{PF} = \cos \phi$   
(iii)  $V_R$   
(iv)  $V_L$

$$I_{RMS} = \frac{V_{RMS}}{Z} = \frac{230}{\sqrt{R^2 + X_L^2}}$$

$$X_L = \omega L = 2 \times 50 \times 0.1 = 31.4 \Omega$$

$$I_{RMS} = \frac{230}{\sqrt{15^2 + 31.4^2}} = \frac{230}{34.85} = 6.6 \text{ A}$$

$$\text{PF} = \cos \phi = \frac{R}{Z} = \frac{15}{34.85} = 0.43$$

$$V_R = I(R) = 6.6 \times 15 = 99 \text{ V}$$

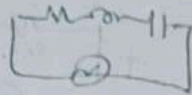
$$V_L = I(X_L) = 6.6 \times 31.4 = 207.4 \text{ V}$$

*Faint handwritten notes and scribbles at the bottom of the page.*

Q. A  $R=20\ \Omega$ ;  $L=0.2\ H$ , &  $C=150\ \mu F$  are connected in series. find from

230V, 50Hz supply.

Find:  $X_L, X_C, Z, Y, P_f$



$V_{rms} = 230V$

①  $X_L = \omega L = 2 \times 3.14 \times 50 \times 0.2$   
 $\Rightarrow X_L = 62.8\ \Omega$

②  $X_C = \frac{1}{\omega C} = \frac{10^6}{314 \times 150} = 21.23\ \Omega$

③  $Z = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{20^2 + 41.57^2}$   
 $= 46.13\ \Omega$

④  $Y = \frac{1}{Z} = 0.0217$

(Admittance)

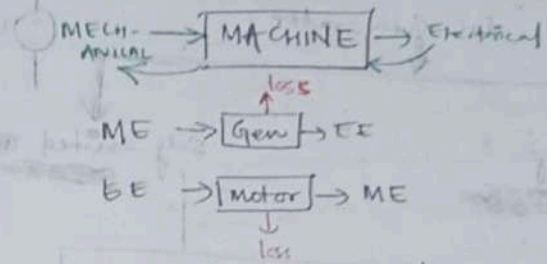
⑤  $P_f = \frac{R}{Z} = \frac{20}{46.13} = 0.433$

⑥ Armature - Armature winding are placed on it. It complete low reluctance path for magnetic flux. Made up of Silicon steel. Laminated to core.

⑦ Commutator - It is a rotating switch. AC to DC in DC generator & DC to AC in DC motor.

⑧ Brush - Brush carry current from commutator. Made up of hard drawn copper. Armature commutator winding. Made up of carbon material.

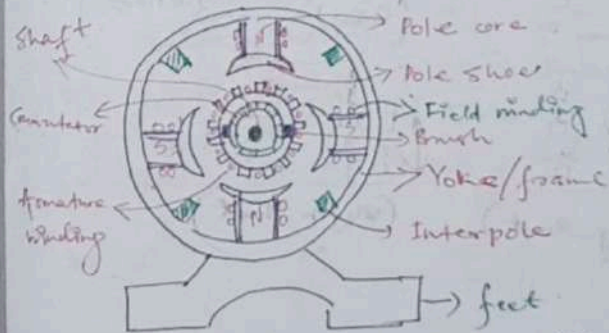
## CONVERSION OF ELECTRICAL POWER



A part of energy lost as heat during the process.

\* Main part of DC machine

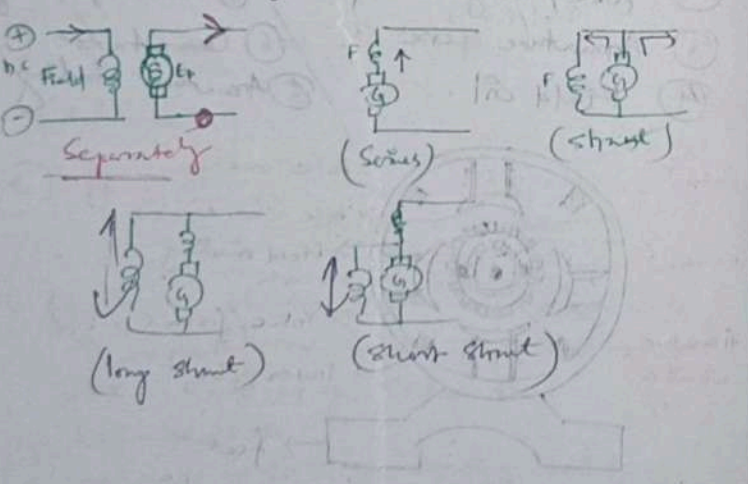
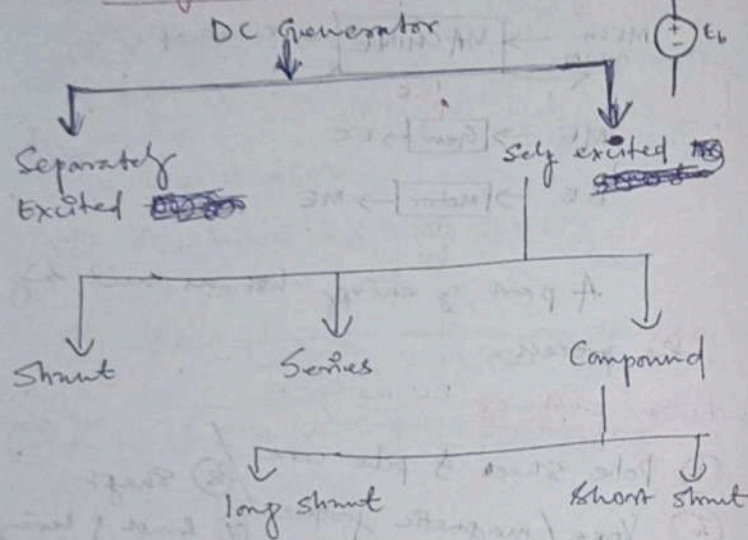
- |                                      |                    |
|--------------------------------------|--------------------|
| ① Pole shoes & pole core             | ⑥ Shaft            |
| ② Yoke / magnetic frame (Steel/iron) | ⑦ Brush & bearing  |
| ③ Armature core                      | ⑧ Commutator       |
| ④ Field coil.                        | ⑨ Armature winding |



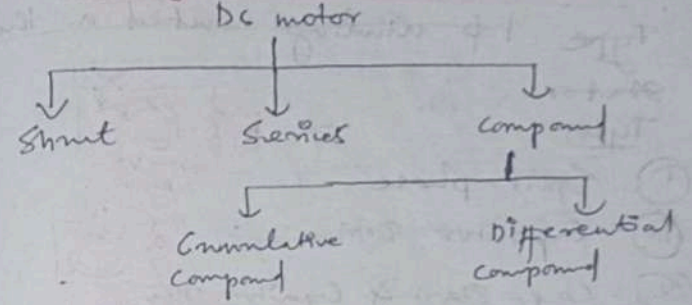
① Yoke - Protect internal part of machine. Provide return path for magnetic flux.

② Pole & pole shoes - It is use to provide housing to the field winding. When excited it behave like a magnet. Pole shoes provide mechanical support to the field winding.

\* Classification of DC generator :-



\* Classification of DC motor :-

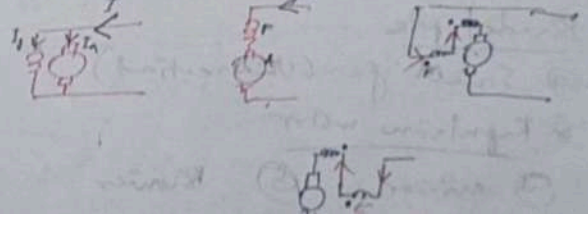


\* Uses of DC Generator

- (i) Lighting & Power supply
- (ii) Charging batteries
- (iii) Booster

\* Uses of DC motor

- (I) Constant speed drive → system employed for motion control.
- (ii) Drilling machine, (ix) Fan
- (iii) Water pump (viii) Cutting machine
- (iv) Elevator (vii) Crane
- (v) Traction (vi) Printing machine



## \* 1 Phase Induction motor

Type 1- $\phi$  winding, mounted on the stator

Types

① Split-phase

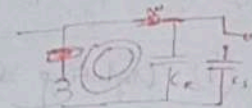
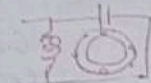
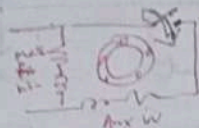
② Capacitor start

③ Cap-start & Capacitor run

④ Shaded pole

X ⑤ Repulsion

⑥ Capacitor run



## # Uses

① Split phase

① Small pump

② Grinder

② Capacitor start

① Pump

② Compressor

③ Cap-start-run

① AC compressor

② Water cooler

④ Shaded pole

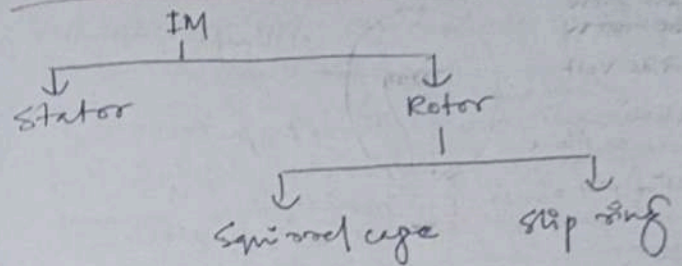
① Small fan (Unidirectional)

⑤ Repulsion motor

① mixer

② Blower

## Parts of Induction motor



## # LUMEN (Teach after LED bulb)

Total amount of visible light emitted by a source per unit time.

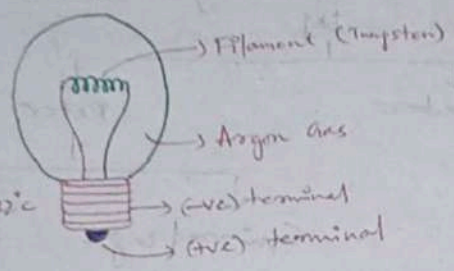
Lumen	400	(lumen/watt)
Filament $\rightarrow$	40W	10
CFL $\rightarrow$	9W	44
LED $\rightarrow$	6W	67

## \* Types of Lamp

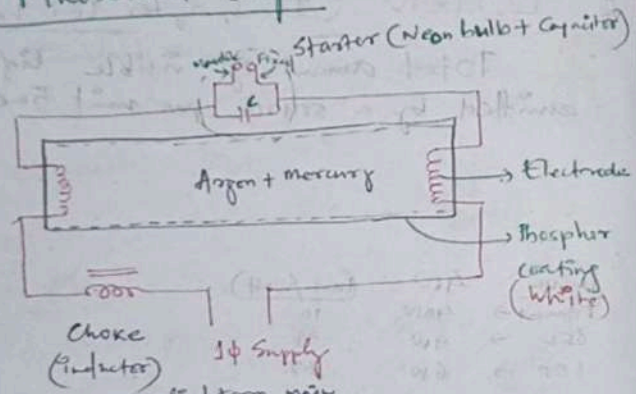
① Filament Bulb -

- $\rightarrow$  Thin filament wire with high melting point. When exposed to  $O_2$ , it gets oxidized and burns. (Biz for burning  $O_2$  is required)
- $\rightarrow$  So, inert gas (Noble gas) is put inside the glass casing and it provides suitable environment for the glow of filament.
- $\rightarrow$  But, 10% of energy is light energy & 90% is lost as heat energy.

(But generally 100W)  
 25-250W  
 → 60-100W  
 ~ 220 Volt  
 → 2500°C heat @ filament  
 melting point = 3412°C



② Fluorescent lamp



When electrical contact in starter is open; starter spark  
 Starter open & close rapidly. bcz of bimetallic contact.  
 ① 220V supplied with produces a spark & filament get heated & movable contact to bend & touch the fixed contact (i.e. closed)  
 ② as a result spark reduces and temp of filament comes down & movable contact get open  
 ③ Arc can follow by step ①

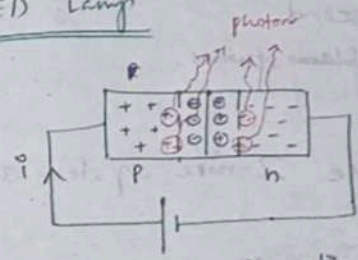
→  $e = L \frac{di}{dt}$  becomes large;  
 Voltage across choke increases to several folds.  
 → It heat the tungsten filament (electrode)

→ Due to high voltage Argon gets ionised and mercury gets vaporised. and they form a conducting path.

→ UV rays are emitted <sup>from mercury</sup> but they are not visible, so phosphor coating produce visible light. excited by UV light produce visible radiation.

→ starter gets inactive during fluorescent lamp glowing. About 80% efficient lamp glowing. But ~~harmful~~ (bcoz mercury)

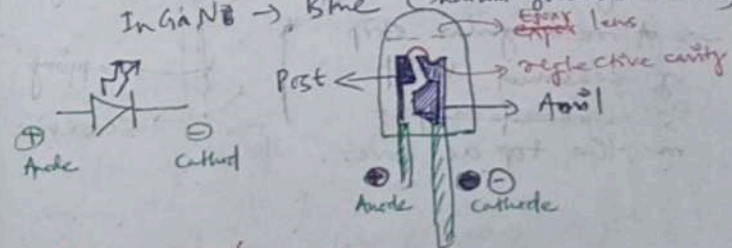
③ LED Lamp



- + → free e<sup>-</sup> & hole  
 ⊕ ⊙ → immobile ion  
 ⊕ ⊙ → recombination

→ When a P-N junction is forward biased; e<sup>-</sup> & holes recombine at depletion layer and light / photon are emitted in all direction.

Ex - AlGaAs → red (Al Ga Arsenic)  
 AlGaP → Green (Al Ga Phosphide)  
 InGaNB → Blue (Indium gallium nitride)



→ About 90% efficient

## \* WIRING & POWER BILLING

→ The process by which electric supply is made available to various load point through a network of conductor

### # factors affecting the choice of wiring.

- (i) Life of Installation
- (ii) Future extension
- (iii) Construction of building.
- (iv) Fire hazard
- (v) Corrosive fumes.
- (vi) Dampness.
- (vii) Cost

\* Single phase 2-wire system used in household.

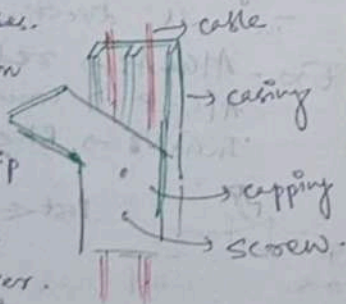
### # Types of wiring -

#### ① Wooden casing & capping

→ casing is fixed on wall with the help of screws & gutties.

→ wires are placed on the grooves.

→ A rectangular strip of seasoned wood is covered on top in the top as cover.



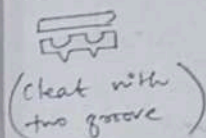
### Advantages

- Excellent protection
- Easy inspection
- Easy to receive.

### Disadvantages

- Fire risk
- Not suitable for damp situation.

#### ② Cleat wiring



→ cable run in groove of porcelain cleat which are fastened in wooden plug on the wall.

#### \* Advantages

- Cheapest
- Little skill required
- Can be dismantled easily with little waste

#### \* Disadvantages

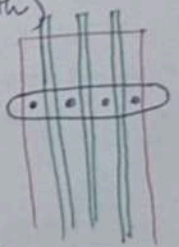
- No protection against mechanical injury (fire, fume, water)
- Not good looking.
- Temporary (short life)

#### ③ CTS (Cable Tyre Sheath)

→ TRS (Tough Rubber Sheath)

- conductor run on the wooden batten on the wall.
- width of batten is depend upon the nos of wires.

→ Hybrid of cleat & casing capping.





Adv	Disadv
→ Easy installation and repair	→ prone to mechanical injury
→ Nice appearance	→ Take more time for installation

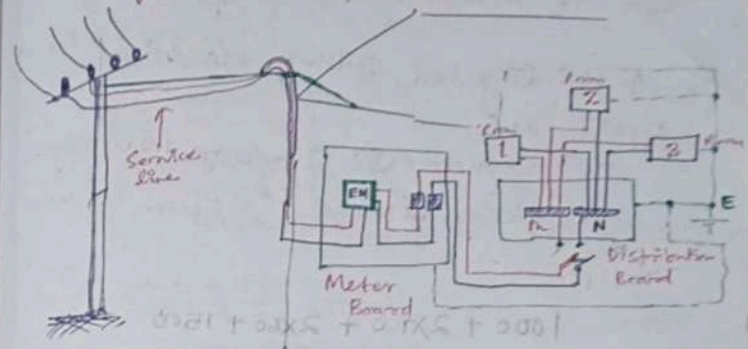
④ Lead sheath wiring

⑤ Conduit wiring

- (a) Surface conduit wiring
- (b) Concealed conduit wiring

Adv	Disadv
① Neat & attractive appearance	① Costly
② Good protection against fire, mechanical damage, moisture	② Skilled technician required
③ High durability	③ More time taking

Layout of household EE wiring



\* Protective Devices used in wiring

- ① Fuse - It is a electrical safety device which operate to provide overcurrent protection  
 $I > I_{rating}$ 
  - One time use
- ② MCB (Miniature circuit Breaker) -  
 since it operate when overload condition when, break back to normal condition;  
 Reusable
- ③ Lightning Arrestor -  
 It protect house from the damaging effect of lightning. It is projected on the top place of house & connected to the earth.
- ④ Earthing -  
 The body / chassis / covering of machine electrical devices are connected to the earth by the help of low resistance wire for transferring immediate electrical discharge.

Calculation of energy in small household installation.

Q. A building has following electrical appliances.

- ① 1 kW motor
- ② 2 bulbs of 100 W each.
- ③ 2 fan of 60 W each
- ④ heater 1.5 kW

Total power?

$$1000 + 2 \times 100 + 2 \times 60 + 1500$$

$$= 2820 \text{ W}$$

$$= 2.82 \text{ kW}$$

Q. Energy = Power \* Time

1 HP motor for 5 hr/day,

3 → 80 W fan for 10 hr/day

4 tube of 40 W for 15 hr/day

Calculate the bill for November if unit cost of bill is 2.5 Rs.

1 unit = 1 kWh

$$1 \text{ HP} = 746 \text{ W}$$

$$\text{Energy} = 746 \times 5 + 80 \times 3 \times 10 + 4 \times 40 \times 15$$

$$(\text{per day}) = 3730 + 2400 + 2400$$

$$= 8530 \text{ Wh}$$

$$\Rightarrow (\text{E/day}) = 8.53 \text{ kWh}$$

$$\text{Total energy cost for month} = 8.53 \times 30 \times 2.5 = 255.75$$

$$\text{Monthly bill} = \text{Rs. } 639.75$$

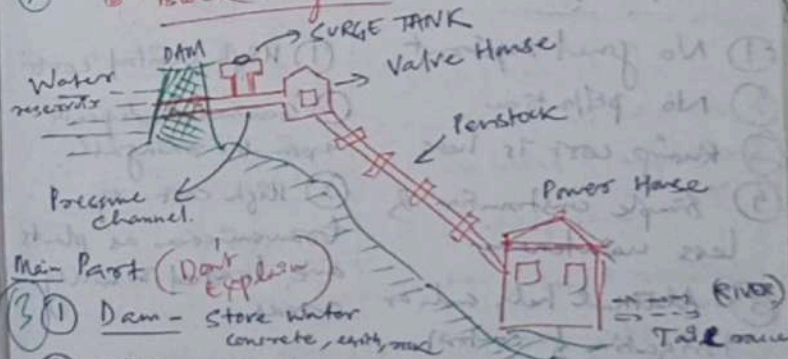
## Generation of Electrical Power

### # HYDRO -

#### • Choice of site

- ① Availability of water - Huge quantity of water at good height
- ② Water Storage - Dam constructed to store water.
- ③ Cost of type of land - To withstand of load weight of equipments to be installed.
- ④ Transportation facility

#### ② • Block diagram



- ① Dam - Store water concrete, earth, etc.
- ② Surge Tank - In abnormal condition; water in penstock may surge the conduit/pipe. Surge tank act as protection.
- ③ Penstock - This is conduit which carry water to turbine. Reinforced concrete/steel.

- ④ Valve House - It control the amt of water to be flow thugh the penstock
- ⑤ Power House
  - ① Turbine - It convert ~~the~~ <sup>energy of</sup> falling water into mechanical energy.
  - ② Alternator / Generator (A/G)  
ME  $\rightarrow$  EE
- ⑥ Spillway - when water storage limit exceed; surplus water is removed from the storage reservoir into river on the down stream side.

Advantage

- ① No fuel requirement
- ② No pollution
- ③ Running cost is less
- ④ Simple construction & less maintenance
- ⑤ Additional help such as irrigation & control of flood.

Disadvantage

- ① High capital cost
- ② Generation depends upon the rainfall
- ③ High cost of transmission as plants are located in hilly areas.

- Working (Before & After)
- (i) When water from reservoir is allowed to pass through pressure channel; it reaches valve house
  - (ii) Surge tank is provided in order to safeguard the extra-back thrust of water causing heavy force to penstock.
  - (iii) Valve house control the amt of water will flow to the turbine thugh penstock
  - (iv) Inside power house; turbine convert & convert fall of water into mechanical energy & and Alternator convert ME into EE.

STEAM / THERMAL POWER PLANT

- # Choice of site
- ① Supply of coal (fuel)
  - ② Availability of water - used in condenser
  - ③ Transport facility - material & machinery
  - ④ Cost & type of land - cheap land
  - ⑤ Nearness to load centre - low transmission loss.
  - ⑥ Distance from populated area - pollution

# Main unit

- (A) Coal storage pit
- (B) Coal Handling pit (pulverization)
- (C) Ash storage pit
- (D) Ash Handling pit
- (E) Boiler - wet steam is produced
- (F) Superheater - wet steam to dry steam
- (G) Economiser - feed water heater & derive heat from flue gases.
- (H) Air pre-heater - increase temperature of air supplied for coal burning.
- (N) FD fan - forced draught fan (draw air from atmosphere)
- (I) ID fan - draw flue gases & send to chimney (induced draught)
- (J) Steam turbine - Steam into ME
- (K) Alternator - ME into EE
- (L) Condenser - exhausted steam from turbine is condensed & fed back to boiler through cooling tower.
- (M) Cooling tower - Possible cooling arrangements for feed water to be recycled in boiler

# Working

- (i) When water from condenser is fed to the boiler through economiser it remain little wet.
- (ii) Boiler is extremely heated chamber bcz of continuous burning of coal in the presence of air injected by FD fan through air preheater.

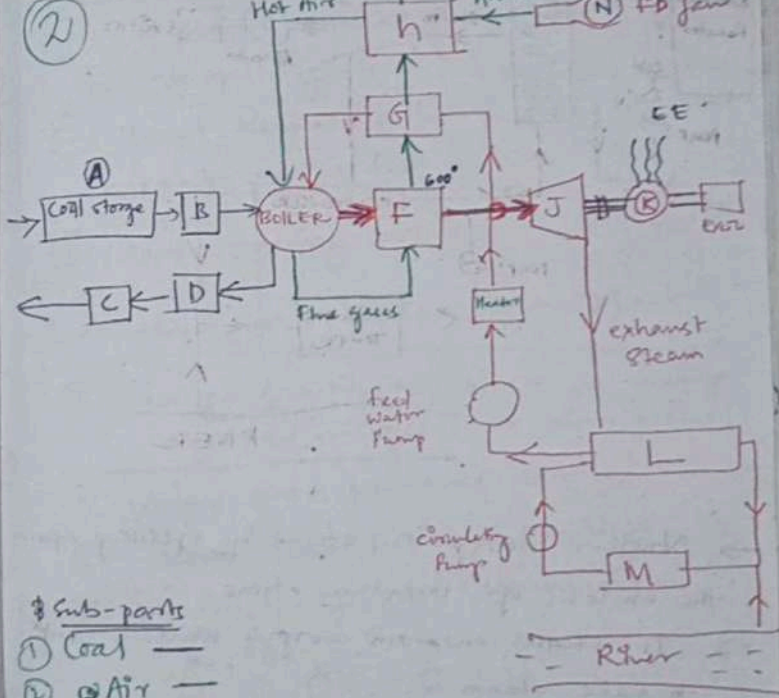
Air, Coal → Steam (dry)

# Advantage

- (1) Coal is cheap
- (2) less initial cost
- (3) Can be install at any place
- (4) required less space than Hydel.

# Disadvantage

- (1) Pollute Air due to fumes/smoke
- (2) Running cost is higher

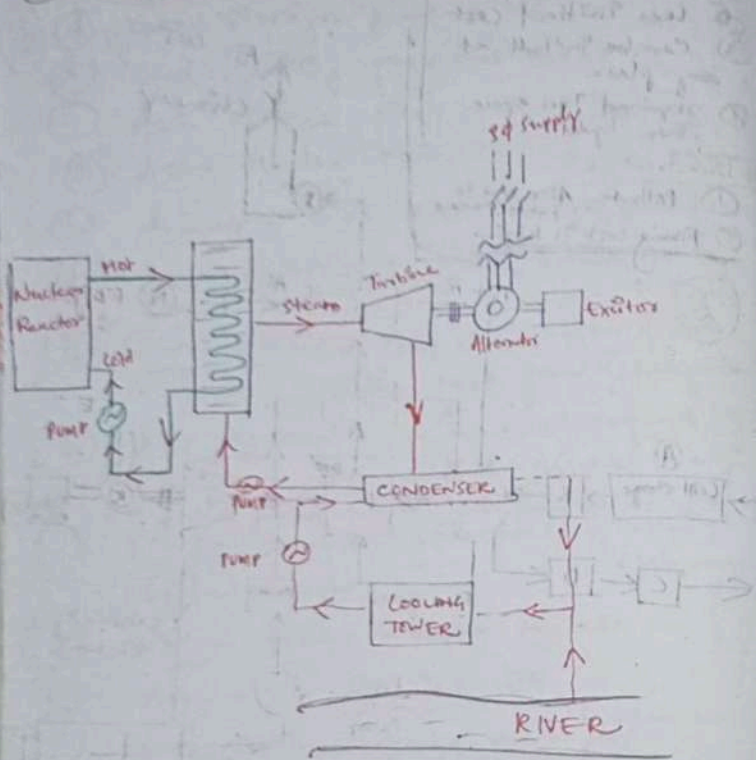


# Sub-parts

- (1) Coal
- (2) Air
- (3) Water

- (iii) So, water get converted into steam (High Press & high temp), and reaches to turbine through superheater (which draw the wet steam).
- (iv) Internal energy of steam → ME by turbine & Alternator → ME → EE.

## 3 Nuclear Power Plant



→ Nuclear energy is produced by splitting apart the nucleus of uranium atoms.

→ It releases enormous energy which is used to make steam.

→ Steam runs the turbine & ME is converted into EE.

## Advantages

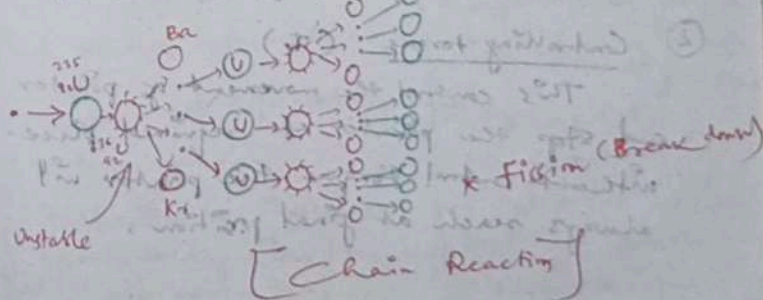
- ① No pollution.
- ② Does not contribute to global warming.
- ③ Most reliable energy source.
- ④ Large amount of energy is produced.
- ⑤ Low starting cost.

## Disadvantages

- ① Waste is radioactive and its disposal is very difficult.
- ② Local thermal pollution from wastewater affects marine life.
- ③ Large running cost.

## Location for Nuclear power plant

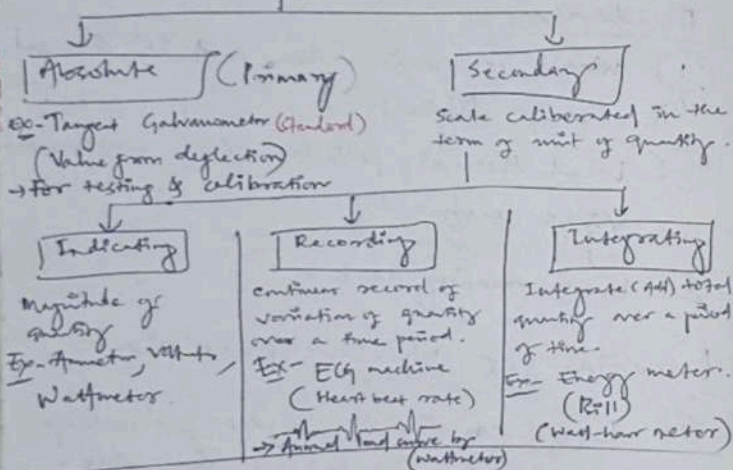
- ① Large quantity of water for cooling is required. Coastal or riverside.
- ② Away from populated place.
- ③ Transportation facility.
- ④ Supply of fuel (uranium).



## MEASURING INSTRUMENTS

The instruments which are used to measure electrical quantities like current, voltage, power, energy, etc are called electrical measuring instruments.

### Measuring Instruments



### # Torque in instruments

① Deflecting torque ( $T_d$ )  
 it deflect/move the pointers. else pointer will always fine at zero.

② Controlling torque ( $T_c$ )  
 This control the movement of pointer and stop the pointer at required place. without control torque the pointer will always reach at final position.

### ③ Damping Torque

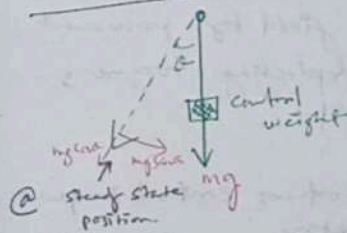
Without damping torque the pointer make oscillation about the steady state position (equilibrium).

This oscillation are damped out by means of damping torque.

Damping torque is present when the pointer move and it becomes zero when the pointer is at steady state position.

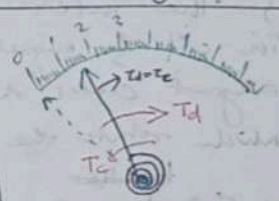
### Types of controlling torque

① Gravity control



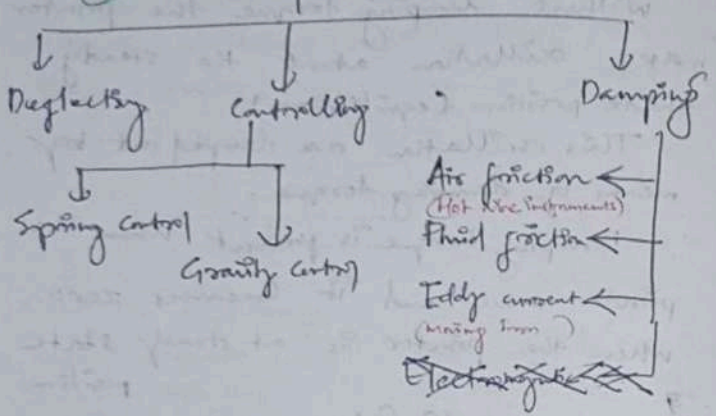
- cheap
- No fatigue
- Reading affected by height
- It is not affected by temperature.
- Position of instrument affect reading (Panel mounting)
- Scale non-uniform

② Spring control



- Spring made up of phosphorus-bronze.
- costly.
- affected by fatigue (stress)
- Not affected by lateral
- Affected by temperature
- Position not affect reading (Portable)
- Scale uniform

# ① Torque



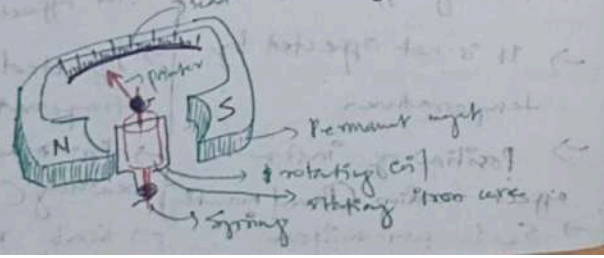
## # PMMC (Permanent magnet moving coil)

→ The interaction between current in coil & magnetic field by permanent magnet causes a deflecting torque, which rotate the coil.

→ Spiral spring produces control torque

→ Eddy current <sup>setting</sup> on the metal frame core due to movement of coil which opposes the movement.

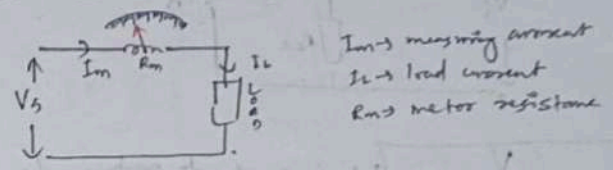
→ Eddy current damping.



## ② Use of PMMC

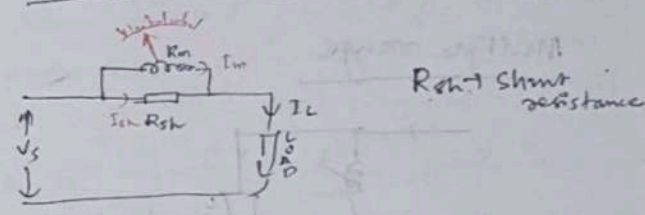
① PMMC as an Ammeter (meter connected in series with load)

④ For low range



$I_m$  → measuring current  
 $I_L$  → load current  
 $R_m$  → meter resistance

⑤ For high range



$R_{sh}$  → shunt resistance

$$R_m \gg R_{sh}$$

$$I_m \ll I_{sh} \quad ; \quad I_{sh} = I_L - I_m$$

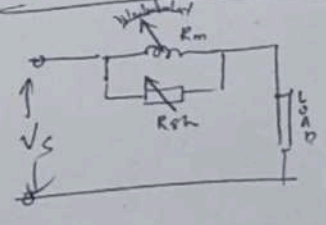
$$I_m (R_m) = (I_L - I_m) R_{sh}$$

$$\Rightarrow R_{sh} = \frac{I_m}{I_L - I_m} R_m$$

$m = \frac{I}{I_m}$   
 multiplication factor

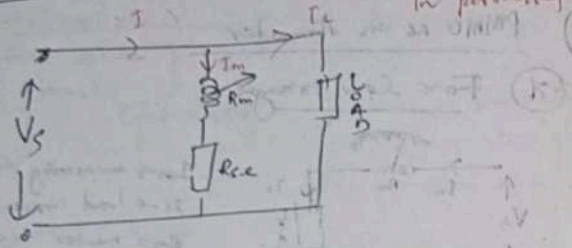
$$\Rightarrow R_{sh} = \left( \frac{1}{m-1} \right) R_m$$

⑥ Multiple range



② AMMC as Voltmeter

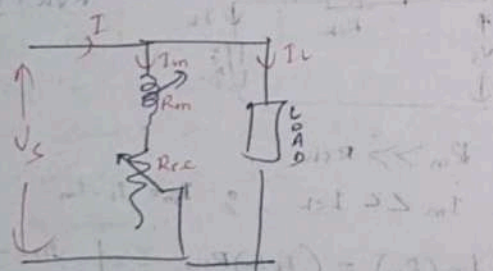
(meter connected across load in parallel)



$$I_m = \frac{V}{R_m + R_L}$$

We want to reduce  $I_m$  so that  $I_L$  is large.

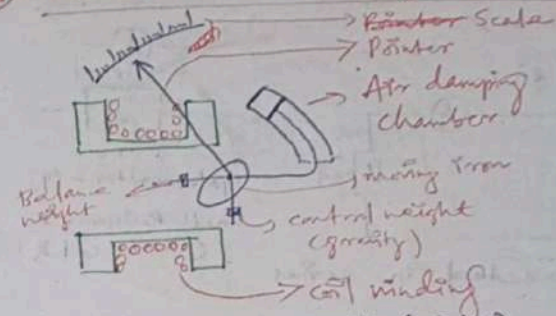
Multiple range



$$R_{se} = (m-1)R_m$$

$$m = \frac{V}{V_m} = \frac{R_m + R_{se}}{R_m} = 1 + \frac{R_{se}}{R_m}$$

⑤ MOVING IRON (MI) type instruments



Control torque  $\rightarrow$  gravity (weight)  
Damping torque  $\rightarrow$  Air damping (pneumatic)

When current flows through the coil it produces a magnetic field. The soft iron piece inside the coil is attracted due to magnetic field & produces a deflecting torque.

$$T_d \propto I^2$$

$$T_c \propto \sin \alpha \quad (\text{due to gravity control})$$

$$\sin \alpha \propto I^2$$

@ equilibrium

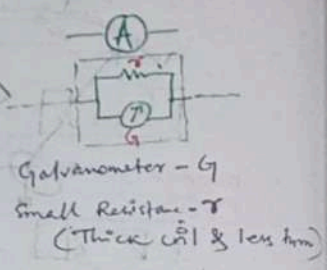
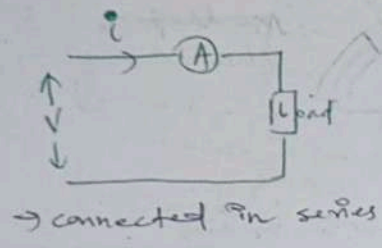
Remarks

- ① Non-uniform scale
- ② Use for both AC & DC
- ③  $T_d \propto I^2$ . So, RMS quantity is required.
- ④ It is both Ammeter & Voltmeter



\* Connection diagram

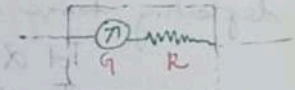
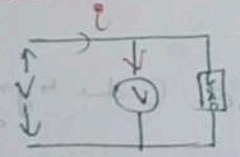
① Ammeter



Galvanometer - G  
Small Resistor - R  
(Thick coil & less turn)

→ connected in series

② Voltmeter

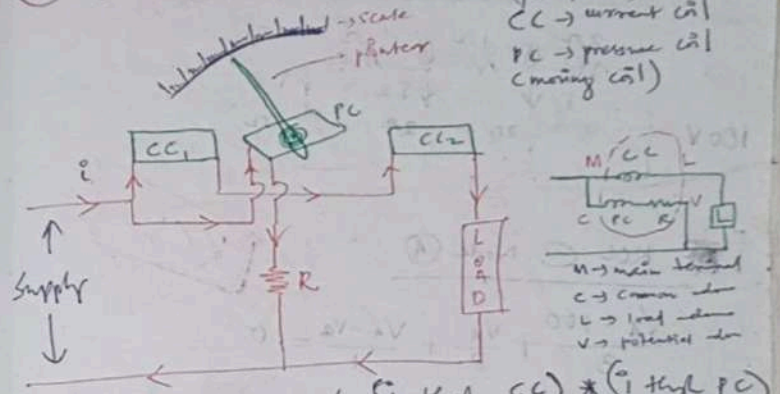


R → large resistance  
(Thin coil & large turns)

→ PMMC with low small current high  $\Omega$ .

→ connected in parallel.

③ Wattmeter



(fixed coil)  
CC → current coil  
PC → pressure coil  
(moving coil)

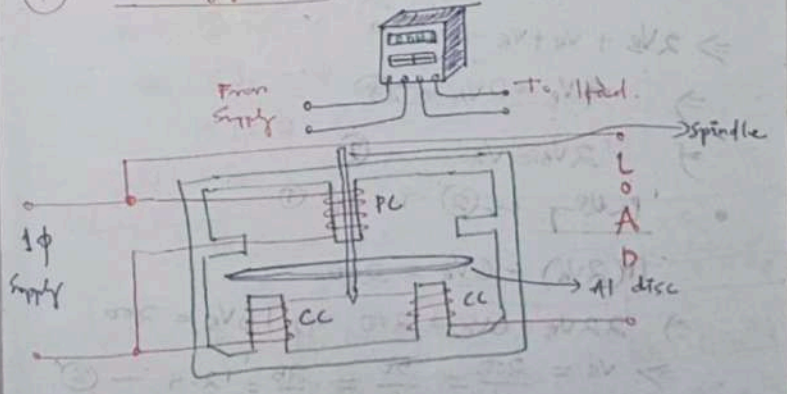
Deflecting torque  $\propto (i \text{ thru } CC) * (i \text{ thru } PC)$   
 $\Rightarrow \propto I_{CC} * V_{PC}$   
 $\Rightarrow \propto \text{Power}$

Both DC & AC measured

CC → few turns of thick wire (RWD)  
 PC → more turns of thin wire (RWD)

→ controlling torque is provided by spring.

④ Energy meter



## KIRCHHOFF'S LAW

### I) Kirchhoff's Current Law

{ Nodal Analysis }

It states that the algebraic sum of currents leaving (or entering) a node is equal to ZERO.

$$\sum_{m=1}^M I_m = 0$$

Node -

Where two or more circuit elements are connected.



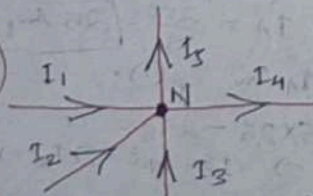
Circuit -

An electric circuit contains a closed path for providing a flow of electrons from a voltage/current source to loads which may be connected in series, parallel, or series-parallel.

Network -

It consists of active and passive (load) elements. It need not contain a closed path for providing a flow of e<sup>-</sup> from active to passive elements.

- $I_m$  is the m<sup>th</sup> (branch) leaving the node.
- $B$  is the number of branches connected to that node.



$$\sum_{m=1}^5 I_m = 0$$

$$\Rightarrow I_1 + I_2 + I_3 - I_4 - I_5 = 0$$

$$\Rightarrow I_1 + I_2 + I_3 = I_4 + I_5$$

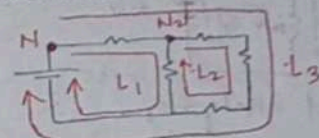
Problem next page

### II) Kirchhoff's Voltage Law

{ Mesh Analysis }

Algebraic sum of voltage around a loop or mesh is equal to ZERO.

Loop - It is a path that terminate at the same node where it started from.

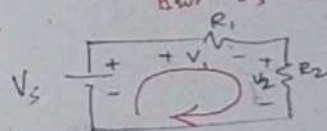


Mesh -

Mesh is a loop that does not contain any loop inside a loop.

$L_1, L_2$  are mesh

But  $L_3$  is not a mesh

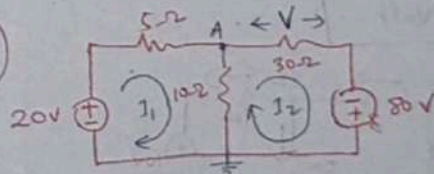


$$V = V_1 + V_2$$

$$\Rightarrow V_s - V_1 - V_2 = 0$$

$$\Rightarrow V_s = V_1 + V_2$$

Ex



$V_A = ?$

In loop 1:  $20 - I_1 \cdot 5 - (I_1 - I_2) \cdot 10 = 0$   
 $\Rightarrow 15 I_1 - 10 I_2 = 20$  — (1)

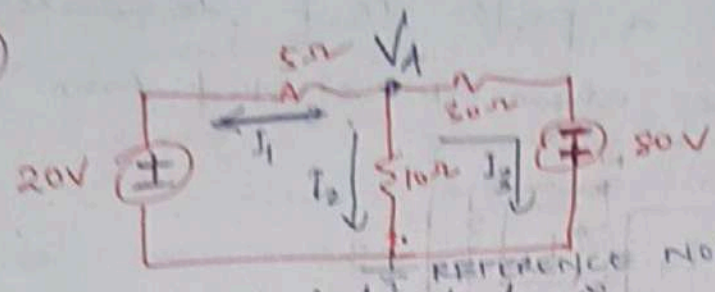
In loop 2:  $80 - 10(I_2 - I_1) - 30 I_2 = 0$   
 $\Rightarrow 40 I_2 - 10 I_1 = 80$  — (2)

Solving eqn (1) & (2), we get  
 $I_1 = 16/5 \text{ A}, I_2 = 14/5 \text{ A}$

$V_{80} = I_2 \times 30$   
 $\Rightarrow V_{80} = \frac{14}{5} \times 30 = 84 \text{ Volt}$   
 $\Rightarrow \boxed{V_{80} = 84 \text{ Volt}}$

$20V - I_1 \times 5 = V_A$   
 $\Rightarrow V_A = 20 - \frac{16}{5} \times 5$   
 $\Rightarrow \boxed{V_A = 4 \text{ Volt}}$

(EX)



Find node voltage  $V_A$

Using nodal analysis  
At node "A"

$$\frac{V_A - 20}{5} + \frac{V_A - 0}{10} + \frac{V_A + 80}{30} = 0$$

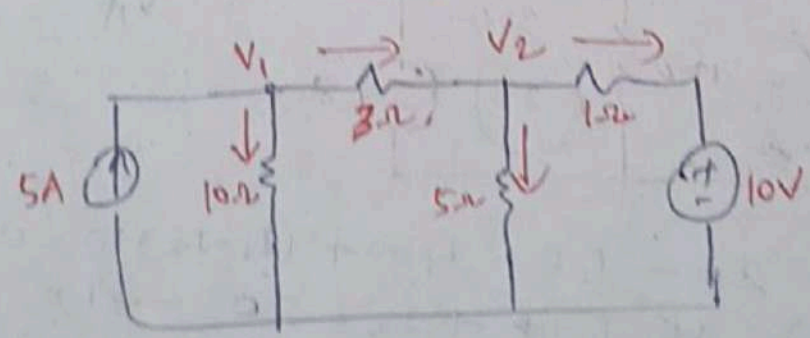
$$\Rightarrow \frac{V_A}{5} + \frac{V_A}{10} + \frac{V_A}{30} - 4 + \frac{8}{3} = 0$$

$$\Rightarrow \frac{6V_A + 2V_A + V_A}{30} - \frac{4}{3} = 0$$

$$\Rightarrow \frac{10V_A}{30} = \frac{4}{3} \Rightarrow V_A = \frac{4 \times 30}{5 \times 10} = 4 \text{ Volt}$$

$$\boxed{V_A = 4 \text{ Volt}}$$

(EX)



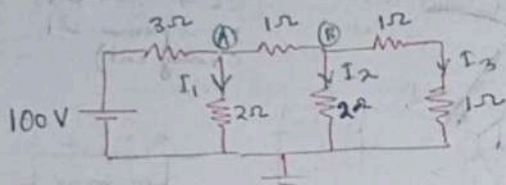
At node 1:

$$5 = \frac{V_1}{10} + \frac{V_1 - V_2}{3} \quad \text{--- (1)}$$

At node 2:

$$\frac{V_1 - V_2}{3} = \frac{V_2}{5} + \frac{V_2 - 10}{1} \quad \text{--- (2)}$$

\* KVL & KCL problem solving



**KCL @ Node A**

$$\frac{V_A - 100}{3} + \frac{V_A}{2} + \frac{V_A - V_B}{1} = 0$$

$$\Rightarrow \frac{V_A}{3} + \frac{V_A}{2} + V_A - \frac{100}{3} - \frac{V_B}{1} = 0$$

$$\Rightarrow 2V_A + 3V_A + 6V_A - 200 - 6V_B = 0$$

$$\Rightarrow 11V_A - 6V_B = 200 \quad \text{--- (1)}$$

**KVL @ Node B**

$$\frac{V_B - V_A}{1} + \frac{V_B}{2} + \frac{V_B}{2} = 0$$

$$\Rightarrow 2V_B + V_B + V_B - 2V_A = 0$$

$$\Rightarrow 4V_B = 2V_A \quad \text{--- (2)}$$

$$\Rightarrow 2V_B = V_A \quad \text{--- (2)}$$

Put eq (2) in eq (1)

$$11(2V_B) - 6V_B = 200$$

$$\Rightarrow 22V_B - 6V_B = 200 \Rightarrow 16V_B = 200$$

$$\Rightarrow V_B = \frac{200}{16} = \frac{50}{4} = \frac{25}{2} = 12.5 \quad \text{--- (3)}$$

Put (3) in (2)

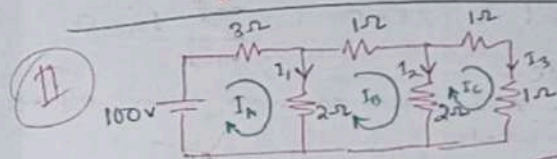
$$V_A = 2(12.5) = 25 \quad \text{--- (4)}$$

**KCL**

$$I_1 = \frac{V_A}{2} = \frac{25}{2} = 12.5 \text{ Amp}$$

$$I_2 = \frac{V_B}{2} = \frac{12.5}{2} = 6.25 \text{ Amp}$$

$$I_3 = \frac{V_C}{2} = \frac{12.5}{2} = 6.25 \text{ Amp}$$



**KVL @ Loop I**

$$100 - 3(I_A) - 2(I_A - I_C) = 0$$

$$\Rightarrow 100 - 5I_A + 2I_C = 0 \quad \text{--- (1)}$$

$$5I_A - 2I_C = 100$$

$$\Rightarrow 5I_C - 2I_C - 2I_A = 0 \quad \text{--- (2)}$$

$$3I_C - 2I_A = 0$$

$$\Rightarrow 4I_C - 2I_A = 0 \Rightarrow I_A = 2I_C \quad \text{--- (3)}$$

Put (3) in eq (1) & (2)

$$\Rightarrow 5I_C - I_C - 2I_C = 0$$

$$\Rightarrow 2I_C - 4I_C = 0 \quad \text{--- (4)}$$

$$2 \times (5I_C - 2I_C) = (100) \times 2 \quad \text{--- (5)}$$

$$8I_C = 200$$

$$\Rightarrow I_C = \frac{200}{8} = 25 \text{ Amp}$$

Put  $I_C$  in eq (3)

$$5 \times 25 - 2I_A = 100$$

$$\Rightarrow 125 - 100 = 2I_A \Rightarrow I_A = \frac{25}{2} \text{ Amp}$$

Put  $I_C$  in eq (3)

$$I_A = 2I_C \Rightarrow 25 \text{ Amp } I_C = \frac{25}{4} \text{ Amp} \Rightarrow I_C = I_3 = 6.25$$

**KVL**

$I_2 = I_C - I_C$
$I_2 = 12.5 - 6.25$
$I_2 = 6.25 \text{ Amp}$
$I_1 = I_A - I_C$
$I_1 = 25 - 12.5$
$I_1 = 12.5 \text{ Amp}$

$I_3 = I_C - I_C$
$I_3 = 25 - 19$
$I_3 = 6$